## Search for a dark photon in the A' Experiment (APEX)

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                                                                                 (Dated: July 1, 2011)
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                          We present a search at Jefferson Lab for new forces mediated by sub-GeV vector bosons with weak coupling
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                       \alpha' to electrons. Such a particle A' can be produced in electron-nucleus fixed-target scattering, and then decay
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                       to an e^+e^- pair, producing a narrow resonance in the QED trident spectrum. Using APEX test run data, we
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searched in the mass range 175–250 MeV, finding no evidence for an  $A' \to e^+e^-$  reaction, and set an upper limit of  $\alpha'/\alpha \simeq 10^{-6}$ . Our findings demonstrate that fixed-target searches can explore a new, wide, and important range of masses and couplings for sub-GeV forces.

The strong, weak, and electromagnetic forces are mediated  $_{56}$  for very weakly coupled gauge bosons. A' masses in the have escaped detection only if their mediators are either heav-<sub>47</sub> run for the A' Experiment (APEX), which was proposed in <sub>63</sub> ( $\alpha = e^2/4\pi$ ), are remarkably weakly constrained [3]. 48 [1, 2] based on ideas presented in [3].

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pling to charged particles if it mixes kinetically with the pho-51 ton [4]. Indeed, quantum loops of heavy particles with elec- 67 liders [5, 10, 15–20]. Electron fixed-target experiments are  $_{52}$  tric and U(1)' charges can generate kinetic mixing and an ef-  $_{68}$  uniquely suited to probing the sub-GeV mass range because 53 fective coupling  $\epsilon e A'_{\mu} J^{\mu}_{\rm EM}$  of the A' to the electromagnetic 69 of their high luminosity, large cross-sections, and favorable 54 current  $J_{EM}^{\mu}$ , suppressed relative to the electron charge e by 70 kinematics. Electrons scattering off target nuclei can radiate

41 by vector bosons of the Standard Model. New forces could 57 MeV-GeV range have received renewed interest as a possi-58 ble explanation of various data anomalies related to dark matier than  $\mathcal{O}(\text{TeV})$  or quite weakly coupled. The latter possibil- 59 ter [6, 7] and of the discrepancy between the calculated and ity can be tested by precision colliding-beam and fixed-target 60 measured anomalous magnetic moment of the muon [8]. A''s experiments. This letter presents the results of a search for 61 in the same mass range arise in several theoretical propossub-GeV mediators of weakly coupled new forces in a test 62 als [9–11], and their couplings to charged matter,  $\alpha' \equiv \epsilon^2 \alpha$ 

The simplest scenario, in which the A' decays directly to A new U(1)' gauge boson, A', can acquire a small cou- 65 ordinary matter, can be tested in electron and proton fixed-66 target experiments [3, 12–14] and at  $e^+e^-$  and hadron col-<sub>55</sub>  $\epsilon \sim 10^{-2}-10^{-6}$  [5]. This mechanism motivates the search <sub>71</sub> an A', which then decays to  $e^+e^-$ , see Fig. 1. The A' would

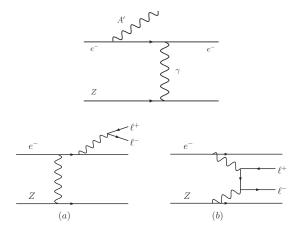


FIG. 1. Top: A' production from radiation off an incoming  $e^-$  beam incident on a target consisting of nuclei of atomic number Z. APEX is sensitive to A' decays to  $e^+e^-$  pairs, although decays to  $\mu^+\mu^$ pairs are possible for A' masses  $m_{A'} > 2m_{\mu}$ . Bottom: QED trident backgrounds: (a) radiative tridents and (b) Bethe-Heitler tridents. will update (thicker lines)

<sub>72</sub> then appear as a small, narrow resonance in the  $e^+e^-$  invariant mass spectrum, over the large background from quantum electrodynamics (QED) trident processes. APEX is optimized to search for such a resonance using Jefferson Laboratory's Continuous Electron Beam Accelerator Facility and the superior mass resolution attainable with the High Resolution Spectrometers (HRS) in Hall A [21].

The full APEX experiment will probe couplings  $\alpha'/\alpha \gtrsim 0^{-7}$  and masses  $\sim 50-550$  MeV, an enormous improvement in cross section sensitivity over all previous experiments. Other electron fixed target experiments are planned at Jefferson Laboratory, including the Heavy Photon Search (HPS) [22] and DarkLight [13]; at MAMI [23]; and at DESY (the HIdden Photon Search (HIPS) [24]).

We present here the results of a test run for APEX that took place July 2010. The layout of the experiment is shown in Fig. 2. The distinctive kinematics of A' production motivates the choice of configuration. The A' typically carries a large fraction of the incident beam energy  $E_{\rm b}$ , is produced forward at angles  $\sim (m_{A'}/E_{\rm b})^{3/2} \ll 1$ , and decays to an  $e^+e^-$  pair with a typical opening angle of  $m_{A'}/E_{\rm b}$ . A symmetric configuration with the  $e^-$  and  $e^+$  each carrying nearly half the beam energy mitigates QED background while maintaining high signal efficiency.

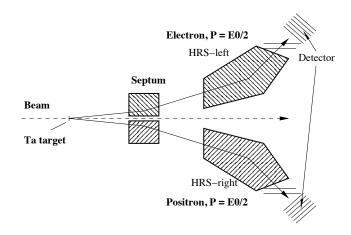


FIG. 2. The layout of the APEX test run. An electron beam (leftto-right) is incident on a thin Tantalum foil target. Two septa magnets of opposite polarity bend charged particles to larger angles into two vertical-bend high resolution spectrometers (HRS) set up to select electrons and positrons each carrying close to half the incoming beam energy. The HRS contain detectors to accurately measure the momentum, direction, and identity of the particles.

104 reduced the solid angle acceptance of each spectrometer from a nominal 4.3 msr to  $\simeq 2.8$  (2.9) msr for the left (right) HRS.

The two spectrometers are equipped with similar detector packages. Two vertical drift chambers, each with a U and V 108 plane, provide kinematic reconstruction of charged particles. 109 A segmented timing hodoscope and a gas Cherenkov counter (for  $e^+$  identification) are used in the trigger. A two-layer lead glass calorimeter provides further offline particle identification. A single-paddle scintillator counter is used for timing

Data was collected with several triggers: single-arm trig-115 gers produced by the hodoscope in either arm, a raw coin-116 cidence trigger produced by a 40-ns wide overlap between the hodoscope signals from the two arms, and a triple coincidence trigger of the previous coincidence signal and the Gas Cherenkov signal of the positron (right) arm. Single-arm trig-120 ger samples are used for optics and acceptance calibration, described below. The raw coincidence event sample, which is dominated by accidental  $e^-\pi^+$  coincidences, is used to check 123 the angular and momentum acceptance of the spectrometers. These  $e^-\pi^+$  coincidences are largely rejected in the triple co-125 incidence sample by the requirement of a Gas Cherenkov sig-126 nal in the positron arm.

The reconstruction of  $e^+$  and  $e^-$  trajectories at the target The test run used a  $(2.260 \pm 0.002)$  GeV electron beam with 128 was calibrated using the "sieve slit method" (see [21, 25]). an intensity up to 150 µA incident on a Tantalum foil of thick- 129 The "sieve slits" — removable Tungsten plates with a grid ness  $21.5 \text{ mg/cm}^2 (3.15 \times 10^{-3} \text{ radiation lengths})$ . The central 190 of holes drilled through at known positions — are inserted momentum was 1.131(2) GeV for the left (right) HRS with a 131 between the target and the septum magnet with a 1.131 GeV momentum acceptance from 1.079 to 1.181 GeV. Dipole sep- 132 incident electron beam. A reconstruction correction matrix tum magnets between the target and the HRS aperture allow 133 was obtained from  $e^-$  elastic scattering data taken with the the detection of  $e^{-1}$ 's and  $e^{+1}$ 's at central angles of 5° relative 134 sieve in place and using the ROOT package from [26], with to the incident beam. Collimators present during the test run 135 care taken to avoid "focusing" systematics [27]. A kinematic

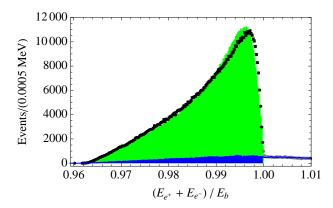


FIG. 3. The fraction of energy carried by the  $e^+e^-$  pair relative to the beam energy in the final coincidence sample (black, with error bars), the measured accidental component (blue), and Monte Carlo (green). Events rejected by the final kinematic selection  $E(e^+) + E(e^-) <$ 2.261 GeV are shown as gray dots, and the rejected accidental component by the blue line.

of the measured sieve holes are used in the final analysis.

coincidence events.

account for nucleus-electron kinematics, and to use the nu- 190 scale but does not affect the mass resolution. clear elastic and inelastic form-factors in [29]. We neglect the 191 few percent with data. Likewise, the shapes of momentum 195 coincident data. and angular distributions agree within 5-10% differentially 196 (see e.g. Fig. 3).

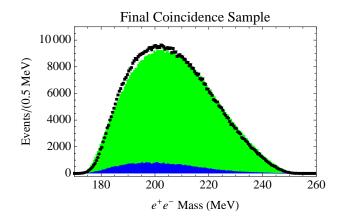


FIG. 4. The invariant mass spectrum of  $e^+e^-$  pair events in the final coincidence sample (black, with error bars), the measured accidental component (blue), and Monte Carlo (green).

171 Track measurement uncertainties contribute 0.28 (1.85) mrad 172 to the horizontal (vertical) angular resolution in the left HRS selection was applied, so that only events within the boundary 173 and 0.44 (1.77) in the right HRS, determined from the ob-174 served sizes of the sieve slit holes in the data. Magnetic op-The final coincidence event sample is selected from the 175 tics imperfections were found to contribute 0.10 (0.22) mrad triple coincidence sample by imposing a 12.5-ns timing win- 176 to the horizontal (vertical) angular resolution. The resultdow on the Gas Cherenkov and raw coincidence signals, re- 177 ing mass resolution was found to be 0.55 MeV from multiple quiring quality tracks in the vertical drift chambers of both 178 scattering in the target, and 0.59 (0.56) MeV from horizonarms, and the kinematic selection described above. Lastly, we 179 tal (vertical) angular reconstruction and optics errors, giving demand that the sum of  $e^+$  and  $e^-$  energies not exceed 2.261  $_{180}$  a combined mass resolution of  $\simeq 0.99$  MeV. Because cali-GeV, the beam-energy threshold for true coincidence events 181 bration of the magnetic optics was performed using only  $e^-$ , the effect of this cut on accidental coincidences is shown in  $_{182}$  and not  $e^+$ , there is a possibility of additional aberrations in Fig. 3). This final sample of 770,500 events consists almost 183 the positron arm. An upper limit for possible aberrations of entirely of true  $e^+e^-$  coincidence events with only 0.9% con- 184 0.5 mrad was obtained from angular correlations in H(e,e'p)tamination by meson background, and 7.4% accidental  $e^+e^-$  185 experiments with the HRS and the calculations of the septa 186 magnetic field. Accounting for these effects, we determine The experimental data was compared with a Monte Carlo 187 the combined mass resolution (rms) to be between 1.0 and calculation of the leading order QED trident process using 188 1.1 MeV. Finally, uncertainty in absolute angle between the MadGraph and MadEvent [28]. MadEvent was modified to 189 two sieve slits introduces 1% uncertainty in the absolute mass

The starting point for the  $A' \rightarrow e^+e^-$  search is the invariant effect of nuclear excitations on the kinematics in inelastic pro- 192 mass distribution of the final coincident event sample, shown cesses. Overall trident rates from the Monte Carlo for the test 193 in Fig. 4. To avoid possible bias, the analysis code was tested run configuration, accounting for acceptance, agree within a 194 and optimized on Monte Carlo and on a 10% sample of the

A linear sideband analysis is not tenable in light of the high 197 statistical sensitivity of the experiment and the appreciable The performance of APEX depends critically on precise re- 198 curvature of the invariant mass distribution. Such an analyonstruction of the invariant mass of  $e^+e^-$  pairs. The HRS 199 sis would suffer from O(1) systematic pulls, which can promomentum resolution is  $O(10^{-4})$  for the kinematics of the 200 duce false positive signals or overstated sensitivity. Instead, APEX experiment. The mass resolution is instead controlled 201 a polynomial background model plus a Gaussian signal norby three contributions to angular resolution: scattering of the 202 malized to S events ( $\sigma = 1.0$  MeV) is fit to a window brack- $^+e^-$  inside the target, track measurement errors by the HRS  $_{203}$  eting each candidate A' mass. The uncertainty in the polydetectors, and imperfections in the magnetic optics recon- 204 nomial coefficients incorporates the systematic uncertainty 205 in the shape of the background model. Based on extensive Multiple scattering in the target contributes 0.37 mrad to the 206 pseudo-experiment studies, a 7th-order polynomial fit over a vertical and horizontal angular resolutions for each particle. 207 30.5 MeV window was found to achieve near-minimum un-

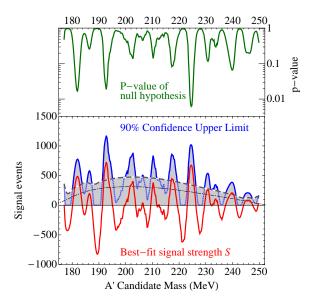


FIG. 5. **Top:** Background-model p-value versus A' mass. **Bottom:** Shaded gray region denotes 90% confidence, 50% power-constrained allowed region [30]. 90% confidence upper limit is shown in solid blue (dotted blue) when it is above (below) the expected limit (gray dashed). Red solid line denotes the best-fit for the number of signal events S. For comparison, thin dot-dashed line indicates contribution of statistical uncertainty to expected sensitivity, if background shape were known exactly.

mimic a signal), is derived from the lowest local p-value ob- 252 window  $\Delta m$  determine an upper limit on  $\alpha'/\alpha$ , served over the full mass range, and calibrated using pseudoexperiments. 225

We find no evidence of an A' signal. The p-value for the dence. The most significant excess, at 224.5 MeV, has a local 257 shown in Fig. 6. p-value of 0.6%; the associated global p-value is 36% (i.e. in 258 233 the absence of a signal, 36% of identically prepared experi- 259 signal of  $A' \to e^+e^-$  electro-production in the mass range ments would observe a more significant effect due to fluctua- 260 175–250 MeV. We established an upper limit of  $\alpha'/\alpha \simeq 10^{-6}$ 235 tions).

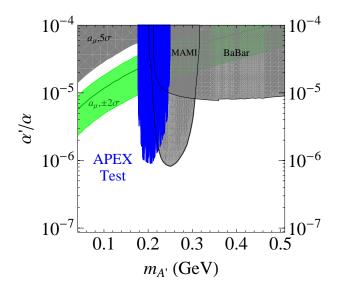


FIG. 6. 90% confidence upper limit on  $\alpha'/\alpha \times Br(A' \to e^+e^-)$ versus A' mass for the APEX test run (blue). Shown in grav are existing constraints from the muon anomalous magnetic moment  $(5\sigma)$  [8]. an approximate 90% confidence limit using BaBar results [3, 16, 31], and the 90% confidence limit reported by Mainz [23]. In the green  $2\sigma$  region, the A' can explain a possible discrepancy between the calculated and measured muon anomalous magnetic moment [8]. The full APEX experiment will roughly cover the entire area of the plot.

To translate the limit on signal events into an upper limit on certainty while maintaining a potential bias below  $0.1\sigma$  across 237 the coupling  $\alpha'$  with minimal systematic errors from accepthe mass spectrum. A symmetric window is used, except for 238 tance and trigger efficiencies, we use a ratio method, normalcandidate masses within 15 MeV of the upper or lower bound-  $^{299}$  izing A' production to the measured QED trident rate. The aries, for which a window of equal size touching the boundary 240 total QED trident background consists of radiative tridents is used. A binned profile likelihood ratio (PLR) is computed 241 (Fig. 1 (a)) and Bethe-Heitler tridents (Fig. 1 (b)) and their as a function of signal strength S at the candidate mass, using 242 interference diagrams (we caution the reader that this nomen-0.05 MeV bins. The PLR is used to derive a 90%-confidence <sup>243</sup> clature may not be standard). The A' signal and radiative upper limit on the signal and the local p-value at S=0 (i.e. 244 trident fully differential cross sections are simply related (see the probability of a larger PLR arising from statistical fluctua-  $^{245}$  [3]), and the ratio f of the radiative-only cross-section to the tions in the background-only model). We define the sensitivity 246 full trident cross-section can be reliably computed in Monte of the search in terms of a 50% power-constraint [30], and do 247 Carlo: f varies lineary from 0.21 to 0.25 across the APEX not regard a value of S as excluded if it is below this sensitiv- 248 mass range, with a systematic uncertainty of 0.01, which domity threshold. This procedure is repeated in steps of 0.25 MeV. 249 inates over Monte Carlo statistics and possible next-to-leading A global p-value, corrected for the "look-elsewhere effect", 250 order QED effects. The 50% power-constrained limit on sig-(the fact that an excess of events anywhere in the range can 251 nal yield  $S_{max}$  and trident background yield  $B_{\Delta m}$  in a mass

$$\left(\frac{\alpha'}{\alpha}\right)_{max} = \left(\frac{S_{max} / m_{A'}}{f B_{\Delta m} / \Delta m}\right) \times \left(\frac{2 N_{\text{eff}} \alpha}{3 \pi}\right), \quad (1)$$

background model and upper bound on the absolute yield  $_{253}$  where  $N_{
m eff}$  counts the number of available decay products of  $A' \to e^+e^-$  signal events (consistent with the data and 254 ( $N_{\rm eff}$  is 1 for  $m_{A'} < 2m_{\mu}$ , and increases to  $\simeq 1.6$  at background model) are shown in Fig. 5. The invariant-mass-  $^{255}$   $m_{A'} \simeq 250$  MeV). The resulting limit, accounting in addidependent limit is  $\simeq 200-500$  signal events at 90% confi- 256 tion for contamination of the background by accidentals, is

> In summary, the APEX test run data showed no significant 261 at 90% confidence. All aspects of the full APEX experiment

262 outlined in [1] have been demonstrated to work. The full ex- 293 periment will run at several beam energies, have improved 294 mass coverage and resolution from a long multi-foil target, 295 and acquire  $\sim 200$  times more data than this test run, dramatically extending our knowledge of sub-GeV force.

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