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| 1  | A Precision Measurement of the Neutron Twist-3 Matrix                                             |
|----|---------------------------------------------------------------------------------------------------|
| 2  | Element $d_2$ :                                                                                   |
| 3  | Probing Color Forces                                                                              |
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## Abstract

The double spin asymmetries and absolute cross-sections were measured at large Bjorken x, in both deep inelastic and resonance regions, by scattering longitudinally polarized electrons at beam energies of 4.74 and 5.89 GeV from a transversely and longitudinally polarized <sup>3</sup>He target. In this dedicated experiment, the spin structure function  $g_2$  of <sup>3</sup>He was determined with precision at large x, and the neutron  $d_2^n$  twist-three matrix element was extracted. Combining  $d_2^n$  and the twist-four matrix element,  $f_2^n$ , the average color electric and magnetic forces were extracted and found to be of opposite sign and of about 60 MeV/fm

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Over the past 50 years, a wealth of information critical to our understanding of sub-104 <sup>105</sup> atomic matter was obtained by probing the electromagnetic and spin structure of the nucleon through lepton (electron, muon an neutrino) scattering. More recently, the availability of 106 polarized lepton beams and targets enabled an intensive worldwide experimental program 107 of inclusive DIS measurements focused on the investigation of the nucleon spin structure 108 function  $g_1$ . This led to the test of the Bjorken sum rule [1, 2], a fundamental sum rule of 109 QCD, and the determination of the quarks spin contributions to the total nucleon spin[3]. 110 Further investigation of the nucleon spin structure through QCD has shown that both spin 111 structure functions  $(g_1 \text{ and } g_2)$  of the nucleon contain contributions from the elusive quark-112 gluon correlations [4–6] beyond the perturbative-QCD radiative corrections [7–9]. However, 113 <sup>114</sup> in stark contrast with the case of  $g_1$  where these correlations emerge at a higher order in the <sup>115</sup> perturbative expansion, and thus are suppressed by powers of the inverse of  $Q^2$  (the virtual <sup>116</sup> photon probe four-momentum transfer squared), in that of  $g_2$  they contribute at leading 117 order. These correlations manifest themselves in  $\bar{g}_2$ , a deviation of the measured  $g_2$  from the <sup>118</sup> so-called Wandzura-Wilczek value  $g_2^{WW}$  [10] expressed solely in term of the  $g_1$  spin structure 119 function:

$$\bar{g}_2(x,Q^2) = g_2(x,Q^2) - g_2^{WW}(x,Q^2);$$
 (1)

$$g_2^{\text{WW}}(x,Q^2) = -g_1(x,Q^2) + \int_x^1 g_1(y,Q^2) dy/y,$$
(2)

<sup>120</sup> where x is the fraction of longitudinal momentum carried by the struck quark in the DIS <sup>121</sup> process. At present there are no *ab initio* calculations of  $\bar{g}_2$  yet. However, using the operator <sup>122</sup> product expansion (OPE)[4, 6], the  $Q^2$  dependent quantity

$$d_2 = 3\int_0^1 dx x^2 \bar{g}_2(x) = \int_0^1 dx x^2 \left[ 3g_2(x) + 2g_1(x) \right]$$
(3)

<sup>123</sup> is shown to be related to a specific matrix element of *local* operators of quark and gluon <sup>124</sup> fields[17, 19] and is calculable in lattice QCD [26]. Insight into the physical meaning of  $d_2$  was <sup>125</sup> articulated by Filippone and Ji [11] where  $d_2$  is expressed in terms of a linear combination <sup>126</sup> of  $\chi_E$  and  $\chi_B$  dubbed the electric and magnetic "color polarizabilities" respectively,

$$\chi_E \vec{S} = \frac{1}{2M^2} \langle P, S | q^{\dagger} \vec{\alpha} \times g \vec{E} q | P, S \rangle, \tag{4}$$

$$\chi_B \vec{S} = \frac{1}{2M^2} \langle P, S | q^{\dagger} g \vec{B} q | P, S \rangle,$$
<sup>(5)</sup>

<sup>127</sup> where P and S are the nucleon momentum and spin, q and  $q^{\dagger}$  are the quark fields,  $\vec{E}$  and <sup>128</sup>  $\vec{B}$  the average color electric and magnetic fields seen by the struck quark,  $\vec{\alpha}$  the velocity of  $_{129}$  the struck quark and g the strong coupling parameter.

<sup>130</sup> More recently Burkardt [12] identified  $d_2$  as proportional to the instantaneous average sum <sup>131</sup> of the transverse electric  $F_E^y(0)$  and magnetic  $F_B^y(0)$  color forces the struck quark experiences <sup>132</sup> at the instant it is hit by the virtual photon due to the remnant di-quark system in the DIS <sup>133</sup> process. The net average force contributes in part to what is called the "color lensing" <sup>134</sup> effect in semi-inclusive DIS where the struck quark feels color forces along its path out <sup>135</sup> before turning into an outgoing hadron [12, 13]. The relations between color forces, color <sup>136</sup> polarizabilities and the matrix elements of quark-gluon correlations are given by:

$$F_E^y(0) = -\frac{M^2}{4}\chi_E = -\frac{M^2}{4} \left[\frac{2}{3}\left(2d_2 + f_2\right)\right],\tag{6}$$

$$F_B^y(0) = -\frac{M^2}{2}\chi_B = -\frac{M^2}{2} \left[\frac{1}{3}\left(4d_2 - f_2\right)\right],\tag{7}$$

<sup>137</sup> where  $f_2$  is the other quark-gluon correlations matrix element, known as the twist-4 matrix <sup>138</sup> element, and is related to the  $x^2$  moment of the  $g_3$  structure function. The twist-4 matrix <sup>139</sup> element has never been directly measured but rather extracted by taking advantage of the <sup>140</sup>  $Q^2$  dependence of  $g_1(x, Q^2)[14, 15]$ , since it appears as a higher order contribution suppressed <sup>141</sup> by  $1/Q^2$  in the first moment of  $g_1$  namely  $\Gamma_1 = \int_0^1 dx g_1(x, Q^2)$ .

In fact,  $d_2$  was calculated in different nucleon structure models [17, 18, 20–25] including 143 lattice QCD calculations [26]. Consistently the different calculations give either zero or a 144 small negative value deviating from the world measured *positive* value by about 2 standard 145 deviations from zero [27, 28]. At the primordial level the forces represented in  $d_2$  are in 146 part responsible for the confinement of the constituents, measuring them and confirming 147 our understanding of QCD is one of the important goals of hadronic physics. This situation 148 called for a dedicated experiment in the case of the neutron.

The E06-014 experiment was performed at Jefferson Lab (JLab) in Hall A and ran from <sup>150</sup> February to March of 2009. The experiment consisted of inclusive scattering of a longi-<sup>151</sup> tudinally polarized electron beam off a transversely and longitudinally polarized <sup>3</sup>He tar-<sup>152</sup> get [30, 31] at two incident beam energies 4.74 GeV and 5.89 GeV. The scattered electrons <sup>153</sup> with momenta ranging from 0.7 to 2 GeV/c were detected in both the BigBite spectrometer <sup>154</sup> (BBS) and the left high resolution spectrometer (LHRS) [30, 31] set at a scattering angle <sup>155</sup> of 45°. The double spin asymmetries (DSA) were measured over the full momentum range <sup>156</sup> at once using the BBS due to its large momentum and angular acceptance while the unpo-<sup>157</sup> larized cross sections were obtained from the well understood LHRS by stepping over the <sup>158</sup> same momentum range in discrete momentum steps. The longitudinal (transverse) DSA is<sup>159</sup> defined as

$$A_{\parallel,(\perp)} = \frac{1}{P_t P_b D_{N_2}(\langle \cos \phi \rangle)} \frac{N^{\downarrow \uparrow (\Rightarrow)} - N^{\uparrow \uparrow (\Rightarrow)}}{N^{\downarrow \uparrow (\Rightarrow)} + N^{\uparrow \uparrow (\Rightarrow)}},\tag{8}$$

where N is the number of electrons,  $P_t$  is the target polarization,  $P_b$  is the electron polarization,  $D_{N_2}$  is the nitrogen dilution factor,  $\phi$  is the azimuthal angle relative to the electron scattering plane, the single arrows refer to the electron's helicity direction, and the double arrows refer to the target's spin direction. The orientation of the arrows are such that arrows pointing to the right (left) represent spins that are transverse to the electron's momentum and arrows pointing up (down) represent spins being parallel (anti-parallel) to the electron's momentum.

The incident electron beam polarization was measured using two independent polarimeters based on Møller and Compton scattering, whose combined analysis yeilded an electron beam polarization of  $71.87\% \pm 1.13\%$  [32]. The residual beam charge asymmetry was deterno mined to be smaller than 100 ppm through analysis of the Compton polarimeter data.

<sup>171</sup> A 40 cm long polarized <sup>3</sup>He [30] cell was filled at room temperature with ~ 8 atm of <sup>3</sup>He <sup>172</sup> and ~ 0.13 atm of N<sub>2</sub> (to reduce depolarization effects). The <sup>3</sup>He nuclei were polarized via a <sup>173</sup> double spin-exchange optical pumping of a Rb-K mixture. The polarization was monitored <sup>174</sup> by nuclear magnetic resonance (NMR) measurements approximately every 4 hours. The <sup>175</sup> NMR measurements were calibrated with electron paramagnetic resonance (EPR) measure-<sup>176</sup> ments and the longitudinal target polarization was cross-checked using known water NMR <sup>177</sup> measurements. The average target polarization achieved was 50.49%  $\pm$  3.64%.

The BBS consists of a large-opening dipole magnet in front of the detector stack, which 178 <sup>179</sup> included three sets of multi-wire drift chambers for charged-particle tracking; a lead-glass calorimeter divided into pre-shower and shower sections, used for electron identification; a 180 scintillator plane located between the pre-shower and shower layers, which provided addi-181 tional electron identification; and a newly installed heavy gas Cerenkov detector [34] po-182 sitioned between the second and third multi-wire drift chambers, which was used for pion 183 rejection. The optics software package used for the BBS was calibrated using various targets 184 at an incident energy of 1.2 GeV [34, 35]. The achieved angular and momentum resolutions 185 were approximately 10 mrad and 1%, respectively. To keep trigger rates compatible with a 186 <sup>187</sup> high live time of the data acquisition ( $\gtrsim 80\%$ ), the main electron trigger was formed from a <sup>188</sup> geometrical overlap between the total shower energy (with a threshold set to  $\sim 500 \text{ MeV}$ )

<sup>189</sup> and Cerenkov ADC sum (with threshold set to ~ 1.5 photoelectrons). Clean  $e^-$  identifica-<sup>190</sup> tion was achieved by placing cuts on the pre-shower energy, the scintillator energy, the ratio <sup>191</sup> E/p of the total shower energy to the momentum determined from optics reconstruction, <sup>192</sup> and Čerenkov timing. These cuts resulted in a pion rejection factor that was better than <sup>193</sup> 10<sup>4</sup>:1.

The LHRS detector package consisted of two vertical drift chambers used for charged-<sup>195</sup> particle tracking, two scintillator planes used for triggering and timing of charged particles, <sup>196</sup> a light gas Čerenkov detector, and lead-glass calorimeter used for electron identification. <sup>197</sup> Optics calibrations [35] for the HRS used the same targets that were used to calibrate the <sup>198</sup> BigBite optics. The LHRS achieved a pion rejection factor better than 10<sup>5</sup>:1, and measured <sup>199</sup> the  $e^{-}$ <sup>3</sup>He inclusive cross section to better than 4%.

The two main sources of background contamination of the electron sample were due to <sup>201</sup> produced charged pions and pair-produced electrons resulting from photons of  $\pi^0$  decay. The <sup>202</sup> BBS  $\pi^{\pm}$  contamination was estimated from the analysis of the pre-shower energy spectrum <sup>203</sup> and found to be less than 3% (6.5%) across the entire useful momentum acceptance for  $\pi^-$ <sup>204</sup> ( $\pi^+$ ). Weighting the measured  $\pi^{\pm}$  asymmetries by the pion contamination resulted in a <sup>205</sup> negligible  $\pi^{\pm}$  asymmetry contamination. The  $\pi^{\pm}$  contamination measured in the LHRS was <sup>206</sup> also found to be negligible.

The amount of pair-produced electron contamination was estimated through positron measurements. Assuming symmetry between the pair produced electrons and positrons, the electron background was directly measured by reversing the BBS and LHRS magnet polarities resulting in positrons, rather than electrons, being steered into the detectors. By switching the magnet polarity both electrons and positrons see the same acceptance which are drops out when forming the  $e^+/e^-$  ratio . The positron cross section was measured with the LHRS and subtracted from the electron cross section. We used the BBS measured and fitted  $e^+/e^-$  ratios, along with statistically weighted positron asymmetry measurements to determine the amount of pair production contamination in the electron sample. The final electron asymmetry was then computed from Eq. 9, where  $c_1$  is the  $\pi^-/e^-$  ratio;  $c_2$  is the  $\pi^+/e^+$  ratio;  $c_3$  is the  $e^+/e^-$  ratio;  $A^m_{\perp,\parallel}$  is the measured electron asymmetry defined in Eqs. 8; and  $A^{e^+}_{\perp,\parallel}$  is the measured positron asymmetry determined from Eqs. 8.

$$A_{\perp,\parallel}^{e^-} = \frac{A_{\perp,\parallel}^m - c_3 A_{\perp,\parallel}^{e^+}}{1 - c_1 - c_3 + c_2 c_3}.$$
(9)

The electromagnetic internal and external radiative corrections were performed on the 219 <sup>220</sup> unpolarized cross section  $\sigma_0$  using the formalism of Mo and Tsai [36, 37]. The elastic [36] and <sup>221</sup> quasi-elastic [41] radiative tails were subtracted using form factors from [39] and [40]. The inelastic corrections were evaluated using the F1F209 model [48] for the unmeasured cross 222 sections in the resonance and DIS regions. We followed the formalism of Akushevich et223 al. [43] to perform the radiative corrections on  $\Delta \sigma_{\parallel}$  and  $\Delta \sigma_{\perp}$ , the polarized cross section 224 differences. Here, the exact elastic polarized cross section difference tails were found to be 225 negligible. The quasi-elastic [44, 45], resonance [46], and deep inelastic regions [50] were 226 treated together using input from their respective models. The size of the total corrections 227 in all cases did not exceed 45% of the measured  $\sigma_0$ ,  $\Delta \sigma_{\parallel}$ , and  $\Delta \sigma_{\perp}$ . This resulted in an 228 absolute uncertainty on the radiative corrections on  $g_1$  and  $g_2$ , dominated by the input cross 229 <sup>230</sup> sections models dependence and the knowledge of thicknesses related to the target, of less than 5% at worst, thus smaller compared to their statistical uncertainty. 231

The DSA data were divided, in the Björken scaling variable x, into thirteen equally spaced bins of 0.05 bin width, while the cross sections were measured in about the same range but with different bin widths. The mean values of the x-bins ranged from 0.277  $\leq x \leq 0.873$ , covering a region from 0.25 to 0.90 in x. The corresponding  $Q^2$  values ranged from 2.04 GeV<sup>2</sup>  $\leq Q^2 \leq 4.88$  GeV<sup>2</sup> and 2.63 GeV<sup>2</sup>  $\leq Q^2 \leq 6.59$  GeV<sup>2</sup> for incident beam energies of 4.74 GeV and 5.89 GeV, respectively. The Born cross sections were found to agree to within ease 6% with those of F1F209 cross section model [48] allowing us to obtain cross sections at the using the F1F209 model.

We show in Fig. 1 the polarized spin structure function  $g_2$  on <sup>3</sup>He formed from the measured Born asymmetries and cross sections according to

$$g_{2}^{^{3}\text{He}} = \frac{MQ^{2}}{4\alpha^{2}} \frac{y^{2}\sigma_{0}}{(1-y)(2-y)} \times \left[ -A_{\parallel}^{e^{-}} + \frac{1+(1-y)\cos\theta}{(1-y)\sin\theta} A_{\perp}^{e^{-}} \right]$$
(10)

where  $\sigma_0$  is the <sup>3</sup>He Born cross section,  $\alpha$  the electromagnetic coupling constant,  $y = E - \frac{244}{E'/E}$  the fraction of the incident electron energy lost in the nucleon rest frame and  $\theta$  the electron scattering angle. Note the dramatic improvement of the statistical precision of our data (in panel a) ) compared to the existing world data at large  $x \ge 0.3$ . For clarity panel eq. b) is zoomed in by a factor of 10 and with most of the world data removed.

The measured DSAs and cross sections at each beam energy were used to evaluate  $d_2^{^{3}\text{He}}$ 249 at two mean  $\langle Q^2 \rangle$  values (3.21 and 4.32 GeV<sup>2</sup>) according to

$$d_{2}^{^{3}\text{He}} = \int_{0.25}^{0.90} dx \frac{MQ^{2}}{4\alpha^{2}} \frac{x^{2}y^{2}\sigma_{0}}{(1-y)(2-y)} \times \qquad (11)$$

$$\left[ \left( 3\frac{1+(1-y)\cos\theta}{(1-y)\sin\theta} + \frac{4}{y}\tan\frac{\theta}{2} \right) A_{\perp}^{e^{-}} + \left(\frac{4}{y} - 3\right) A_{\parallel}^{e^{-}} \right].$$

The upper integration limit of x = 0.90 was chosen in order to avoid the quasielastic peak and the  $\Delta$  resonance. In addition to using Eq. 12, the Nachtmann moments [55] were also used to evaluate  $d_2^{^{3}\text{He}}$ . The difference between the two approaches at our kinematics was found to be an order of magnitude smaller than the measured  $d_2^{^{3}\text{He}}$  value, and so Nachtmann moments were not used in our analysis. The neutron information was extracted from the d<sub>2</sub><sup>3</sup>He quantity through the expression

$$d_2^n = \frac{d_2^{^{3}\text{He}} - (2P_p - 0.014) d_2^p}{P_n + 0.056},$$
(12)

where  $P_p$  and  $P_n$  are the effective proton and neutron polarizations in <sup>3</sup>He, and the factors 257 0.056 and 0.014 are due to the  $\Delta$ -isobar contributions [33].  $d_2^p$  in Eq. 12, was calculated from 258 various global analyses [47, 50–54] using the x range covered by E06-014 at average  $\langle Q^2 \rangle$ 259 values of 3.23 and 4.32 GeV<sup>2</sup>.

The  $d_2^n$  values measured during E06-014 represent only partial integrals. The full integrals 260  $_{261}$  can be evaluated by including the low and high x contributions. The low x contribution is  $_{262}$  suppressed due to the  $x^2$  weighting of the  $d_2$  integrand, but was calculated by fitting existing  $_{263}\ g_1^n$  [49, 56–58] and  $g_2^n$  [27, 56, 59] data. The fits to both structure functions extended the  $_{264} x$  range to  $0.02 \le x \le 0.25$ . The low  $x d_2^n$  contribution was assumed to have the same  $Q^2$  $_{265}$  value as our measured  $d_2^n$  values. To account for the high x contribution, the elastic form  $_{266}$  factors  $G_E^n$  and  $G_M^n$  were computed from the Galster parameterization [60] and dipole model, <sup>267</sup> respectively. The contributions used to evaluate the total  $d_2^n$  integral are listed in Table I. The total values of  $d_2^n$  results from this experiment are shown as a function of  $Q^2$  in 268 269 Fig. 2 (left panel) along with the world data. We find that our  $d_2^n$  results are in agreement with lattice QCD prediction [26], as well as various bag [17, 22, 23] and chiral soliton 270 <sup>271</sup> models [24, 25], which predict a zero or a small and negative value of  $d_2^n$ . Note the general  $_{272}$  agreement in the sign of our measured  $d_2^n$  compared to various model predictions. Given the  $_{273}$  precision of our measurements, although not at the same  $Q^2$  value, we find a much smaller  $_{274}$   $d_2^n$  value than that reported by the SLAC E155 experiment.

| $\left< Q^2 \right>  [{ m GeV}^2]$ | Measured | Low x   | Elastic  | Total    |
|------------------------------------|----------|---------|----------|----------|
| 3.21                               | -0.00261 | 0.00038 | -0.00108 | -0.00331 |
| 4.32                               | 0.00004  | 0.00038 | -0.00069 | -0.00027 |

TABLE I. Our measured  $d_2^n$ , along with the low-x and elastic  $d_2^n$  contributions, which were used in evaluating the full  $d_2^n$  integrals.

TABLE II. Our results for  $f_2^n$ ,  $F_E$  and  $F_B$  compared to model calculations. The value for  $d_2^n$  is assumed to be zero in the Instanton model calculation, as it is much smaller than  $f_2^n$  [64].

| Group                   | $Q^2 \; ({\rm GeV^2})$ | $f_2^n$                           | $F_E \ ({\rm MeV/fm})$      | $F_B \ ({\rm MeV/fm})$     |
|-------------------------|------------------------|-----------------------------------|-----------------------------|----------------------------|
| E06-014                 | 3.21                   | $0.07623 \pm 0.00079 \pm 0.04014$ | $-51.85 \pm 1.32 \pm 29.90$ | $66.64 \pm 2.43 \pm 30.00$ |
| E06-014                 | 4.32                   | $0.07329 \pm 0.00083 \pm 0.04013$ | $-54.18 \pm 1.37 \pm 29.90$ | $55.39 \pm 2.53 \pm 30.00$ |
| Instanton $[64, 65]$    | 0.40                   | 0.038                             | -30.41                      | 30.41                      |
| QCD sum rule $[18, 19]$ | 1                      | $-0.013 \pm 0.006$                | $54.25 \pm 15.52$           | $79.52 \pm 30.06$          |
| QCD sum rule $[20]$     | 1                      | $0.010 \pm 0.010$                 | $29.73 \pm 16.62$           | $81.75 \pm 30.64$          |
| MIT Bag $[17]$          | 1                      | 0.000                             | 0.000                       | 0.000                      |

To extract the average electric and magnetic color forces,  $f_2^n$  needs to be determined 276 first. To this end we followed the analysis of  $f_2$  described in [14] but with updated  $a_2^n$  and 277  $d_2^n$  values as well as using data from JLab RSS experiment [62]. The singlet axial charge, 278  $\Delta\Sigma$ , was determined from values of  $\Gamma_1^n$  at  $Q^2 > 5$  GeV<sup>2</sup> to be 0.375  $\pm$  0.052, in excellent 279 agreement with that found in [63]. A summary of our  $f_2^n$  and average color force values, 280 along with comparisons to several models can be found in Table II.

In summary, we have measured the DSA and absolute cross sections from a polarized <sup>282</sup> <sup>3</sup>He target. This allowed for the precision measurement of the neutron  $d_2$  at two  $\langle Q^2 \rangle$ <sup>283</sup> values of 3.21 and 4.32 GeV<sup>2</sup>. We find that  $d_2^n$  is in general small, and negative at lower <sup>284</sup>  $\langle Q^2 \rangle$ , while consistent with zero at our higher  $\langle Q^2 \rangle$  measurement. In contrast with previous <sup>285</sup> results we find values consistent with the lattice QCD prediction [26], and various nucleon <sup>286</sup> structure models. We used our  $d_2^n$  measurements to extract the twist-4 matrix element  $f_2^n$ <sup>287</sup> and performed a neutron average electric and magnetic color forces decomposition. Our <sup>288</sup> results show that  $f_2^n$  is much larger then  $d_2^n$ , leading to the electric and magnetic color forces 289 to be nearly equal in magnitude but with opposite sign in the neutron.

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- <sup>296</sup> [1] J. D. Bjorken, Phys. Rev. **148**, 1467 (1966).
- <sup>297</sup> [2] J. D. Bjorken, Phys. Rev. D 1, 1376 (1970).
- [3] C. A. Aidala, S. D. Bass, D. Hasch and G. K. Mallot, Rev. Mod. Phys. 85, no. 2, 655 (2013)
   [arXiv:1209.2803 [hep-ph]].
- <sup>300</sup> [4] E. V. Shuryak and A. I. Vainshtein, Nucl. Phys. B **201**, 141 (1982).
- <sup>301</sup> [5] R. L. Jaffe, Comments Nucl. Part. Phys. **19**, 239 (1990).
- <sup>302</sup> [6] R. L. Jaffe and X. -D. Ji, Phys. Rev. D 43, 724 (1991).
- <sup>303</sup> [7] V. N. Gribov and L. N. Lipatov, Sov. J. Nucl. Phys. **15**, 438 (1972) [Yad. Fiz. **15**, 781 (1972)].
- <sup>304</sup> [8] G. Altarelli and G. Parisi, Nucl. Phys. B **126**, 298 (1977).
- <sup>305</sup> [9] Yu. L. Dokshitzer, Sov. Phys. JETP **46**, 641(1977).
- <sup>306</sup> [10] S. Wandzura and F. Wilczek, Phys. Lett. B **72**, 195 (1977).
- <sup>307</sup> [11] B. W. Filippone and X. -D. Ji, Adv. Nucl. Phys. **26**, 1 (2001) [hep-ph/0101224].
- <sup>308</sup> [12] M. Burkardt, arXiv:0810.3589 [hep-ph].
- <sup>309</sup> [13] M. Burkardt, Nucl. Phys. A **735**, 185 (2004) [hep-ph/0302144].
- 310 [14] Z. -E. Meziani, W. Melnitchouk, J. -P. Chen, S. Choi, T. Averett, G. Cates, C. W. de Jager
- and A. Deur *et al.*, Phys. Lett. B **613**, 148 (2005) [hep-ph/0404066].
- 312 [15] M. Osipenko, W. Melnitchouk, S. Simula, P. E. Bosted, V. Burkert, M. E. Christy, K. Griffioen
- and C. Keppel *et al.*, Phys. Lett. B **609**, 259 (2005) [hep-ph/0404195].
- <sup>314</sup> [16] A. V. Sidorov and C. Weiss, Phys. Rev. D 73, 074016 (2006) [hep-ph/0602142].
- <sup>315</sup> [17] X. -D. Ji and P. Unrau, Phys. Lett. B **333**, 228 (1994) [hep-ph/9308263].
- 316 [18] E. Stein, P. Gornicki, L. Mankiewicz, A. Schafer and W. Greiner, Phys. Lett. B 343, 369
- $_{317}$  (1995) [hep-ph/9409212].

- <sup>318</sup> [19] E. Stein, P. Gornicki, L. Mankiewicz and A. Schafer, Phys. Lett. B **353**, 107 (1995) [hep <sup>319</sup> ph/9502323].
- <sup>320</sup> [20] I. I. Balitsky, V. M. Braun and A. V. Kolesnichenko, Phys. Lett. B 242, 245 (1990) [Erratum <sup>321</sup> ibid. B 318, 648 (1993)] [hep-ph/9310316].
- 322 [21] B. Ehrnsperger and A. Schafer, Phys. Rev. D 52, 2709 (1995) [hep-ph/9505306].
- 323 [22] X. Song, Phys. Rev. D 54, 1955 (1996) [hep-ph/9604264].
- 324 [23] M. Stratmann, Z. Phys. C 60, 763 (1993).
- 325 [24] H. Weigel, L. P. Gamberg and H. Reinhardt, Phys. Rev. D 55, 6910 (1997) [hep-ph/9609226].
- <sup>326</sup> [25] H. Weigel and L. P. Gamberg, Nucl. Phys. A 680, 48 (2000) [hep-ph/0004057].
- M. Gockeler, R. Horsley, D. Pleiter, P. E. L. Rakow, A. Schafer, G. Schierholz, H. Stuben and
   J. M. Zanotti, Phys. Rev. D 72, 054507 (2005) [hep-lat/0506017].
- <sup>329</sup> [27] P. L. Anthony et al. [E155 Collaboration], Phys. Lett. B **553**, 18 (2003) [hep-ex/0204028].
- 330 [28] X. Zheng *et al.* [Jefferson Lab Hall A Collaboration], Phys. Rev. C 70, 065207 (2004) [nucl asymptotic ex/0405006].
- <sup>332</sup> [29] Jefferson Lab E07-003,
- https://userweb.jlab.org/~rondon/sane/.
- 334 [30] J. Alcorn, B. D. Anderson, K. A. Aniol, J. R. M. Annand, L. Auerbach, J. Arrington,
- <sup>335</sup> T. Averett and F. T. Baker *et al.*, Nucl. Instrum. Meth. A **522**, 294 (2004).
- 336 [31] Hall A Collaboration, JLab Hall A general operations manual,
- http://hallaweb.jlab.org/news/minutes/OSP/osp-27feb2011.pdf (2011).
- 338 [32] D. Parno, Ph.D. thesis, Carnegie Mellon University,
- http://hallaweb.jlab.org/experiment/E06-014/talks/DianaParno\_Dissertation.pdf#Diana
  (2011).
- <sup>341</sup> [33] F. R. P. Bissey, V. A. Guzey, M. Strikman and A. W. Thomas, Phys. Rev. C 65, 064317
   (2002) [hep-ph/0109069].
- 343 [34] M. Posik, Ph.D. thesis, Temple University (2014).
- <sup>344</sup> [35] X. Qian *et al.* [Jefferson Lab Hall A Collaboration], Phys. Rev. Lett. **107**, 072003 (2011)
   <sup>345</sup> [arXiv:1106.0363 [nucl-ex]].
- 346 [36] L. W. Mo and Y. -S. Tsai, Rev. Mod. Phys. 41, 205 (1969).
- 347 [37] Y. -S. Tsai, SLAC-PUB-0848.
- 348 [38] K. Slifer et al. [E94010 Collaboration], Phys. Rev. Lett. 101, 022303 (2008) [arXiv:0803.2267

349 [nucl-ex]].

- <sup>350</sup> [39] A. Amroun, V. Breton, J. M. Cavedon, B. Frois, D. Goutte, F. P. Juster, P. Leconte and
  J. Martino *et al.*, Nucl. Phys. A 579, 596 (1994).
- 352 [40] J. W. Lightbody and J. S. O'Connell, Comp. in. Phys. 2(3), 57 (1988).
- <sup>353</sup> [41] S. Stein, W. B. Atwood, E. D. Bloom, R. L. Cottrell, H. C. DeStaebler, C. L. Jordan, H. Piel
  <sup>354</sup> and C. Y. Prescott *et al.*, Phys. Rev. D **12**, 1884 (1975).
- 355 [42] I. V. Akushevich and N. M. Shumeiko, J. Phys. G 20, 513 (1994).
- <sup>356</sup> [43] I. Akushevich, A. Ilyichev, N. Shumeiko, A. Soroko and A. Tolkachev, Comput. Phys. Com <sup>357</sup> mun. **104**, 201 (1997) [hep-ph/9706516].
- <sup>358</sup> [44] P. E. Bosted, Phys. Rev. C **51**, 409 (1995).
- 359 [45] J. E. Amaro, M. B. Barbaro, J. A. Caballero, T. W. Donnelly, A. Molinari and I. Sick, Phys.
- 360 Rev. C **71**, 015501 (2005) [nucl-th/0409078].
- <sup>361</sup> [46] D. Drechsel, S. S. Kamalov and L. Tiator, Eur. Phys. J. A **34**, 69 (2007) [arXiv:0710.0306
   <sup>362</sup> [nucl-th]].
- <sup>363</sup> [47] D. de Florian, G. A. Navarro and R. Sassot, Phys. Rev. D **71**, 094018 (2005) [hep-ph/0504155].
- 364 [48] P. E. Bosted and V. Mamyan, arXiv:1203.2262 [nucl-th].
- <sup>365</sup> [49] P. L. Anthony *et al.* [E142 Collaboration], Phys. Rev. D **54**, 6620 (1996) [hep-ex/9610007].
- <sup>366</sup> [50] D. de Florian, R. Sassot, M. Stratmann and W. Vogelsang, Phys. Rev. Lett. **101**, 072001
   <sup>367</sup> (2008) [arXiv:0804.0422 [hep-ph]].
- <sup>368</sup> [51] C. Bourrely, J. Soffer and F. Buccella, Eur. Phys. J. C 23, 487 (2002) [hep-ph/0109160].
- <sup>369</sup> [52] C. Bourrely, J. Soffer and F. Buccella, Phys. Lett. B 648, 39 (2007) [hep-ph/0702221 [HEP<sup>370</sup> PH]].
- <sup>371</sup> [53] E. Leader, A. V. Sidorov and D. B. Stamenov, Phys. Rev. D 73, 034023 (2006) [hep <sup>372</sup> ph/0512114].
- <sup>373</sup> [54] T. Gehrmann and W. J. Stirling, Phys. Rev. D 53, 6100 (1996) [hep-ph/9512406].
- <sup>374</sup> [55] O. Nachtmann, Nucl. Phys. B **63**, 237 (1973).
- <sup>375</sup> [56] K. Kramer, D. S. Armstrong, T. D. Averett, W. Bertozzi, S. Binet, C. Butuceanu, A. Cam <sup>376</sup> sonne and G. D. Cates *et al.*, Phys. Rev. Lett. **95**, 142002 (2005) [nucl-ex/0506005].
- 377 [57] K. Abe et al. [E143 Collaboration], Phys. Rev. D 58, 112003 (1998) [hep-ph/9802357].
- 378 [58] K. Abe et al. [E154 Collaboration], Phys. Lett. B 404, 377 (1997) [hep-ex/9705017].
- <sup>379</sup> [59] P. L. Anthony *et al.* [E155 Collaboration], Phys. Lett. B **458**, 529 (1999) [hep-ex/9901006].

- <sup>380</sup> [60] S. Galster, H. Klein, J. Moritz, K. H. Schmidt, D. Wegener and J. Bleckwenn, Nucl. Phys. B
   <sup>381</sup> **32**, 221 (1971).
- 382 [61] P. Solvignon et al. [E01-012 Collaboration], arXiv:1304.4497 [nucl-ex].
- <sup>383</sup> [62] K. Slifer *et al.* [Resonance Spin Structure Collaboration], Phys. Rev. Lett. **105**, 101601 (2010)
   <sup>384</sup> [arXiv:0812.0031 [nucl-ex]].
- <sup>385</sup> [63] A. Accardi, J. L. Albacete, M. Anselmino, N. Armesto, E. C. Aschenauer, A. Bacchetta,
  <sup>386</sup> D. Boer and W. Brooks *et al.*, arXiv:1212.1701 [nucl-ex].
- 387 [64] J. Balla, M. V. Polyakov and C. Weiss, Nucl. Phys. B 510, 327 (1998) [hep-ph/9707515].
- <sup>388</sup> [65] N. -Y. Lee, K. Goeke and C. Weiss, Phys. Rev. D **65**, 054008 (2002) [hep-ph/0105173].



FIG. 1.  $x^2$  weighted  $g_2^{^{3}\text{He}}$  plotted against x. Panel a) illustrates the increased precision of our results compared to the world data [28, 49, 56, 58]. All error bars in the world data are statistical and systematic uncertainties added in-quadrature. Panel b) is zoomed by a factor of 10 in the vertical scale and excludes some of the world data for clarity. The error bars on the E06-014 data are statistical only. The top (red) and bottom (blue) bands represent the systematic uncertainty associated with the E = 4.74 and 5.89 GeV data sets, respectively. The yellow band shows the  $g_2^{\text{WW},^{3}\text{He}}$  coverage from several global analyses [47, 50–54].



FIG. 2. Panel a): World  $\bar{d}_2^n$  (no elastic contribution) data plotted against  $Q^2$ . The E06-014 measured  $d_2^n$  without (with) low the low x contributions added are represented by blue solid circle (solid red up triangle) markers, and are offset in  $Q^2$  for clarity. The inner error bar ticks on the E06-014 measurements represent the systematic uncertainty, while the outer error bar ticks represent the statistical uncertainties. The world data [27, 28, 59, 61, 62] error bars represent the in-quadrature sum of the statistical and systematic uncertainties. Panel b): Shows the effect of adding the elastic contribution (x = 1 contribution already accounted for in the lattice QCD prediction). Panel c):  $d_2^n$  predictions from lattice QCD [26] (red up triangle markers are our final d2n values.), QCD sum rules [18, 20, 21], bag models [17, 22, 23], and chiral soliton models [24, 25].