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Transformation from invariant frame to lab frame and CM angle for the reaction $ep \rightarrow e'p'\gamma$.
Calculation of the Jacobian matrix determinant as a function of invariants and beam energy:

$$\frac{d\sigma}{dx_b dQ^2 dt d\Phi} = \frac{2\pi}{4EE'} \frac{2Mx_b^2}{Q^2} \frac{M^2 + \frac{Q^2}{x_b} - Q^2}{2M\sqrt{Q^2 - (\frac{Q^2}{2Mx_b})^2} Q^2 (\frac{1}{x_b} - 1)} \frac{d\sigma}{dE' d\Omega' d\cos(\Theta_{\gamma^* \gamma}^{CM}) d\Phi} \quad (1)$$

with $d\Omega' = \sin\theta(e')d\theta(e')d\phi(e')$ corresponding to the scattered electron solid angle. Using $x_b = \frac{Q^2}{2M(E-E')}$ with E and E' beam and scattered electron energies, Q^2 : photon virtuality, Φ leptons vs photons plane azimuthal angle, M: proton mass, $\Theta_{\gamma^* \gamma}$ polar angle of virtual to real photon in $\gamma^* p$ CM frame.