
The Λ weak decay constant
 α_+ at low energies



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GLUEX

Background

Λ BARYONS ($S = -1, I = 0$)

$$\Lambda^0 = uds$$

Λ

$$I(J^P) = 0(\frac{1}{2}^+)$$

Mass $m = 1115.683 \pm 0.006$ MeV
 $(m_\Lambda - m_{\bar{\Lambda}}) / m_\Lambda = (-0.1 \pm 1.1) \times 10^{-5}$ ($S = 1.6$)
Mean life $\tau = (2.632 \pm 0.020) \times 10^{-10}$ s ($S = 1.6$)
 $(\tau_\Lambda - \tau_{\bar{\Lambda}}) / \tau_\Lambda = -0.001 \pm 0.009$
 $c\tau = 7.89$ cm
Magnetic moment $\mu = -0.613 \pm 0.004 \mu_N$
Electric dipole moment $d < 1.5 \times 10^{-16}$ e cm, CL = 95%

Decay parameters

$$\begin{aligned} p\pi^- & \quad \alpha_- = 0.642 \pm 0.013 \\ \bar{p}\pi^+ & \quad \alpha_+ = -0.71 \pm 0.08 \end{aligned}$$

2018

Λ DECAY PARAMETERS

See the “Note on Baryon Decay Parameters” in the neutron Listings. Some early results have been omitted.

α_- FOR $\Lambda \rightarrow p\pi^-$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
0.642±0.013 OUR AVERAGE				
0.584±0.046	8500	ASTBURY	75	SPEC
0.649±0.023	10325	CLELAND	72	OSPK
0.67 ±0.06	3520	DAUBER	69	HBC From Ξ decay
0.645±0.017	10130	OVERSETH	67	OSPK Λ from $\pi^- p$
0.62 ±0.07	1156	CRONIN	63	CNTR Λ from $\pi^- p$

α_+ FOR $\bar{\Lambda} \rightarrow \bar{p}\pi^+$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
-0.71 ±0.08 OUR AVERAGE				
-0.755±0.083±0.063	≈ 8.7k	ABLIKIM	10	BES $J/\psi \rightarrow \Lambda \bar{\Lambda}$
-0.63 ±0.13	770	TIXIER	88	DM2 $J/\psi \rightarrow \Lambda \bar{\Lambda}$

- ❖ The $\Lambda \rightarrow p\pi^-$ decay is a weak decay and preserves some of the polarisation of the Λ
- ❖ α_- is the parameter that tells us how much of the polarisation is transferred from the Λ onto the proton \rightarrow “Self-analysing” decay
- ❖ In 2019 new BESIII result with huge discrepancy

2019

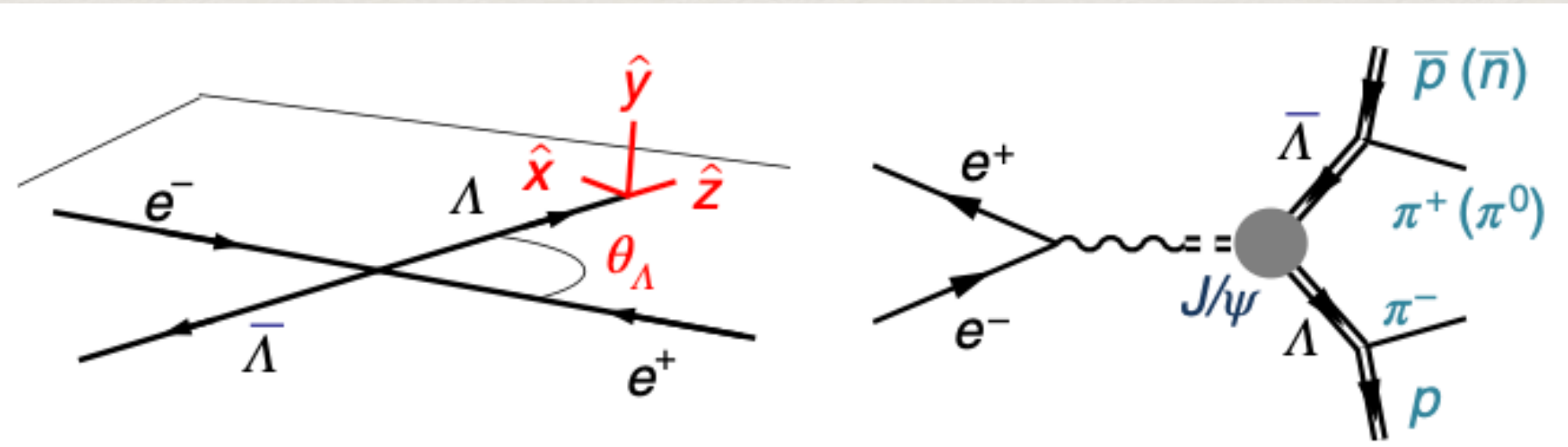
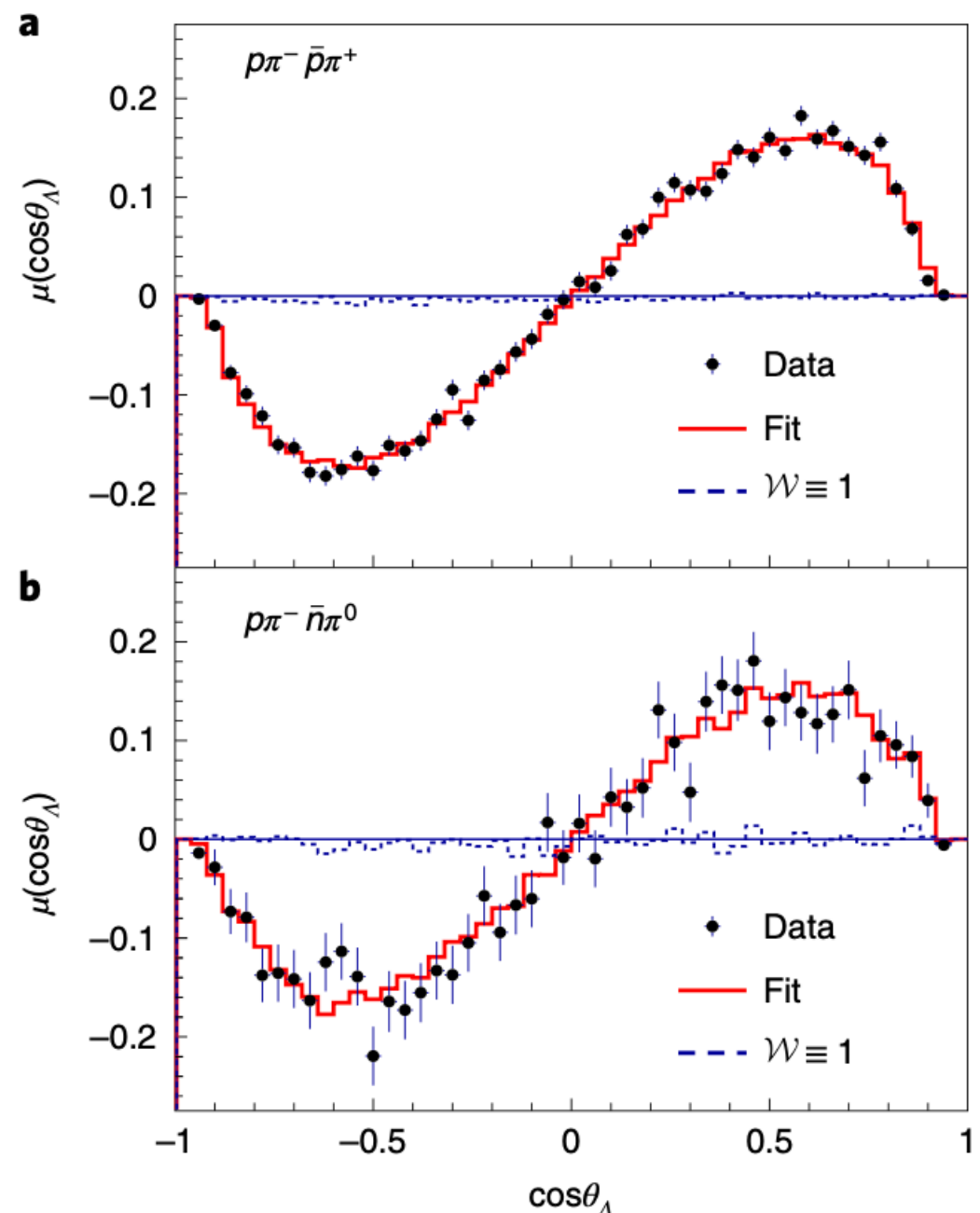


Table 1 | Summary of the results

Parameters	This work	Previous results
α_ψ	$0.461 \pm 0.006 \pm 0.007$	0.469 ± 0.027 (ref. ¹⁴)
$\Delta\Phi$	$42.4 \pm 0.6 \pm 0.5^\circ$	-
α_-	$0.750 \pm 0.009 \pm 0.004$	0.642 ± 0.013 (ref. ⁶)
α_+	$-0.758 \pm 0.010 \pm 0.007$	-0.71 ± 0.08 (ref. ⁶)



2019 - further work

D.G. Ireland et al

PHYSICAL REVIEW LETTERS **123**, 182301 (2019)

Kaon Photoproduction and the Λ Decay Parameter α_-

If the photon beam is circularly polarized we have

$$1 + \alpha_- \cos \theta_y P + (\alpha_- \cos \theta_x C_x + \alpha_- \cos \theta_z C_z) P_C^\gamma, \quad (2)$$

and if the photon beam is linearly polarized the distribution is

$$1 + \alpha_- \cos \theta_y P - \{\Sigma + \alpha_- \cos \theta_y T\} P_L^\gamma \cos 2\phi - \{\alpha_- \cos \theta_x O_x + \alpha_- \cos \theta_z O_z\} P_L^\gamma \sin 2\phi. \quad (3)$$

+ Fierz identities:

$$O_x^2 + O_z^2 + C_x^2 + C_z^2 + \Sigma^2 - T^2 + P^2 = 1$$
$$\Sigma P - C_x O_z + C_z O_x - T = 0$$

- ❖ Use data from three different publications from different beam times
- ❖ Extrapolate data to have data set with common kinematics
- ❖ Extract alpha from over-constrained set of equations
- ❖ Since then two more publications by BES3
- ❖ Old results ignored by PDG but slight tension between new results

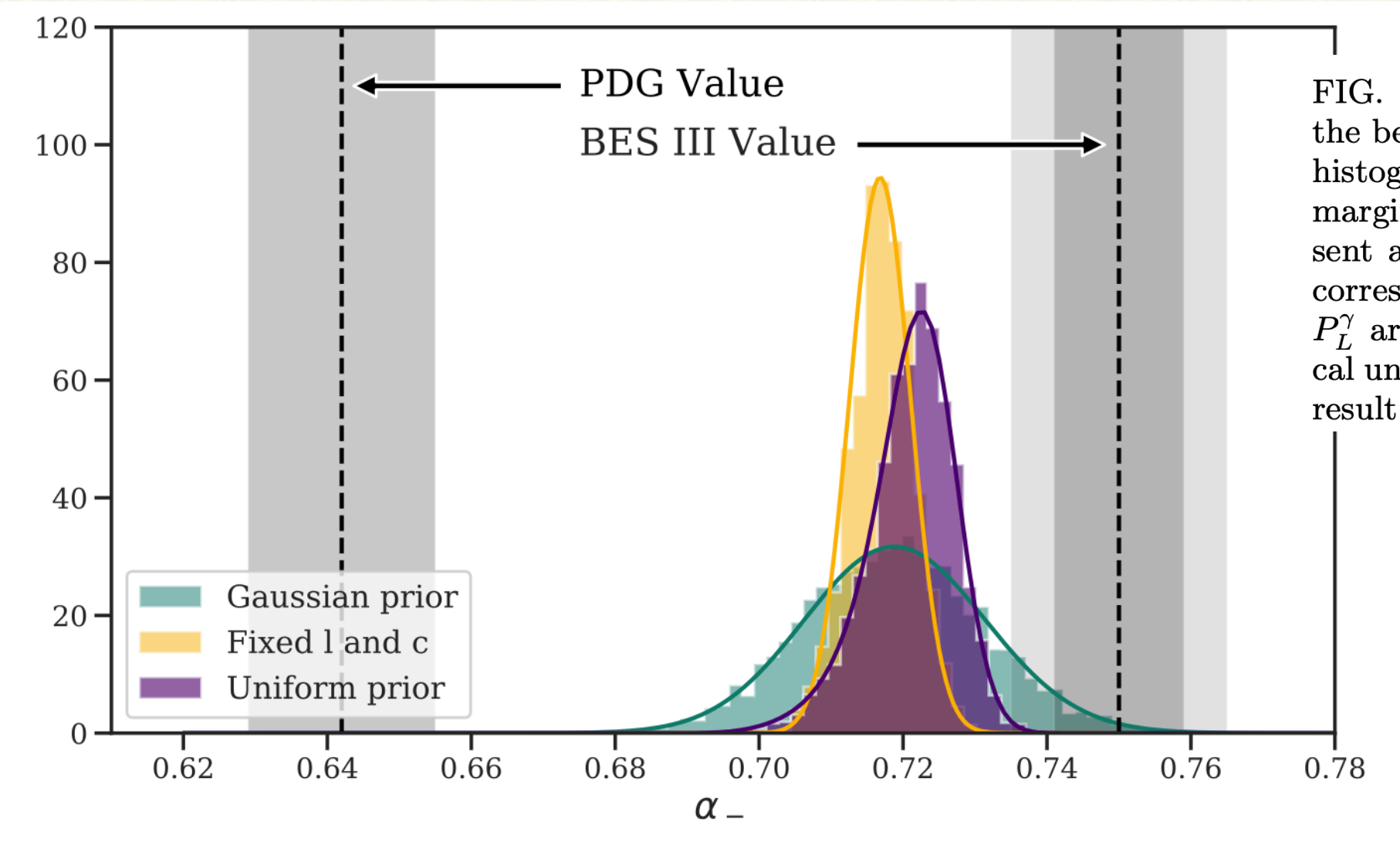
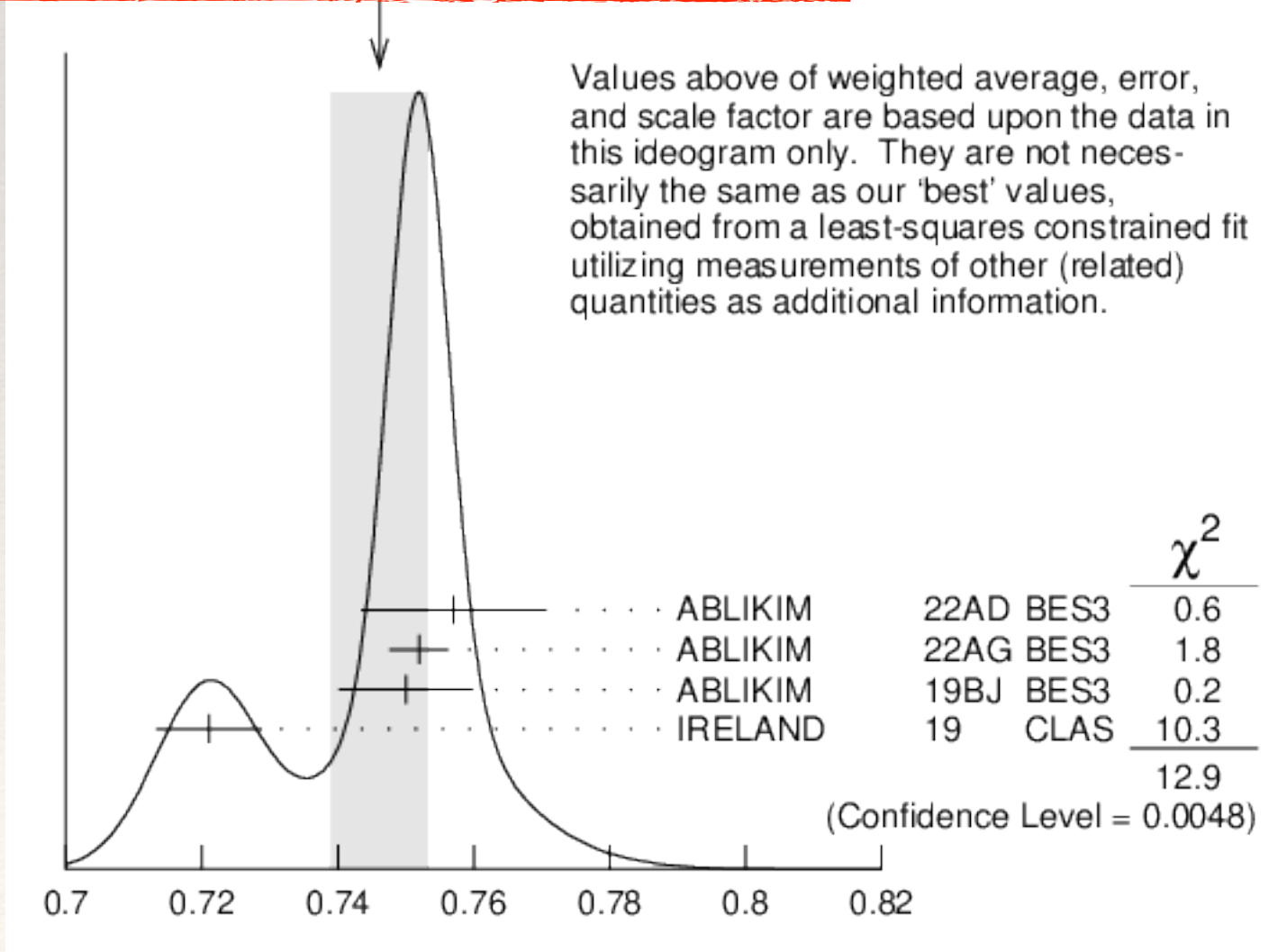


FIG. 1. Posterior densities for α_- , given different priors for the beam polarization calibration constants P_C^γ and P_L^γ . The histograms show the result of the MCMC sampling of the marginalized posterior densities while the solid lines represent a direct scan of the posteriors. For clarity, the results corresponding to the double width uniform priors for P_C^γ and P_L^γ are omitted. Dark grey vertical bands represent statistical uncertainty; the additional light grey bands on the BESIII result represent systematic uncertainty.

$$\alpha = 0.721(6)(5)$$

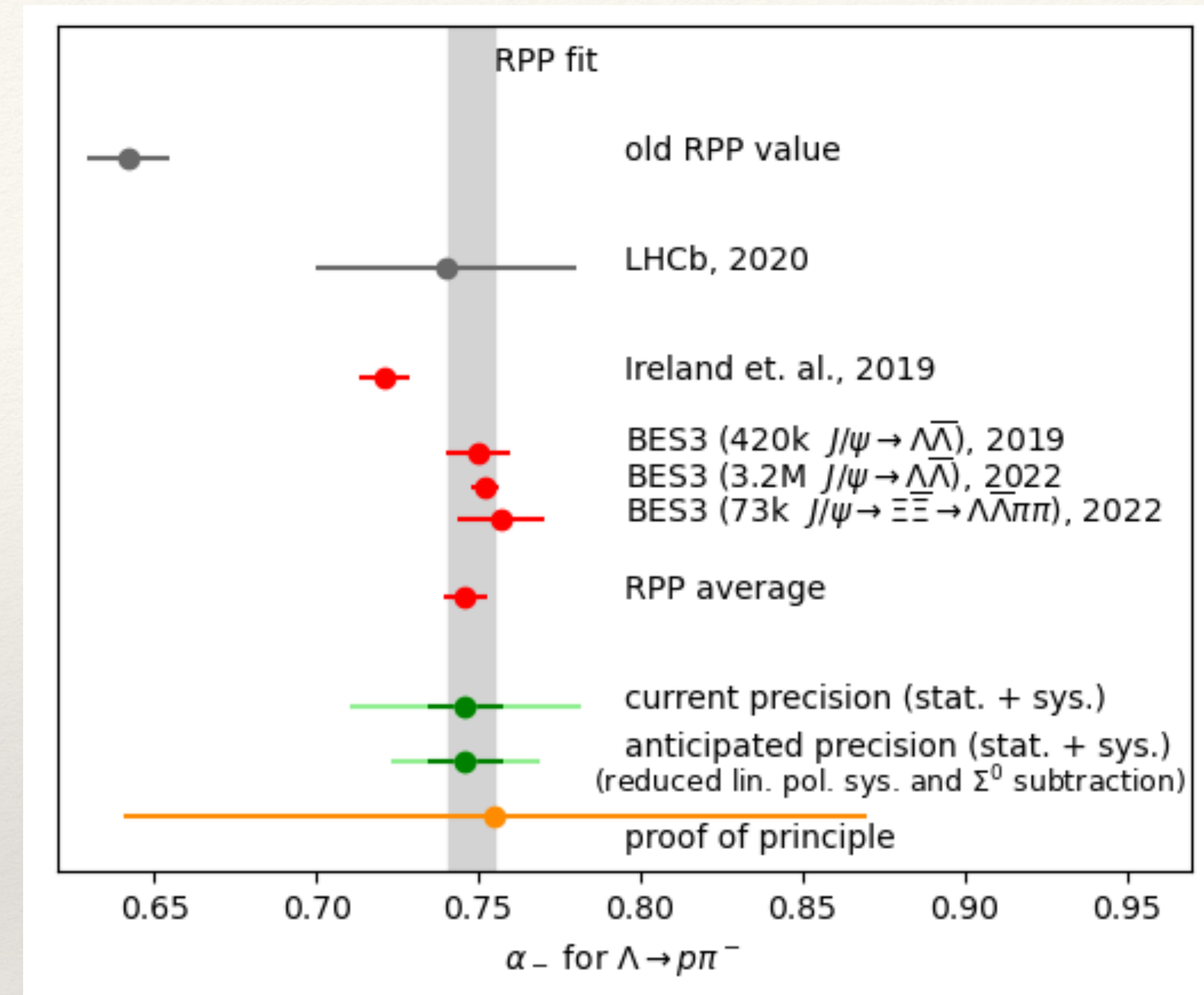
WEIGHTED AVERAGE
 0.746 ± 0.007 (Error scaled by 2.1)



What will we do in Hall D?

<https://arxiv.org/abs/2405.01288>

- ❖ We can use the same idea as Ireland et al but do it better!
- ❖ No need to interpolate between results from different experiments with different kinematics
- ❖ Measure $P, \Sigma, T, O_x, O_z, C_x, C_z$ all simultaneously for $\gamma p \rightarrow K^+ \Lambda$
 - ❖ Requirement: **Linear** + **circular** polarization in Hall D **simultaneously** (elliptical polarization)
- ❖ Since we are over constrained by Fierz identities: leave α_- as free parameter
- ❖ In practice: directly fit amplitudes to data instead of constrained polarisation observables \rightarrow automatically constrained
- ❖ **Approved by PAC52 as run group addition**

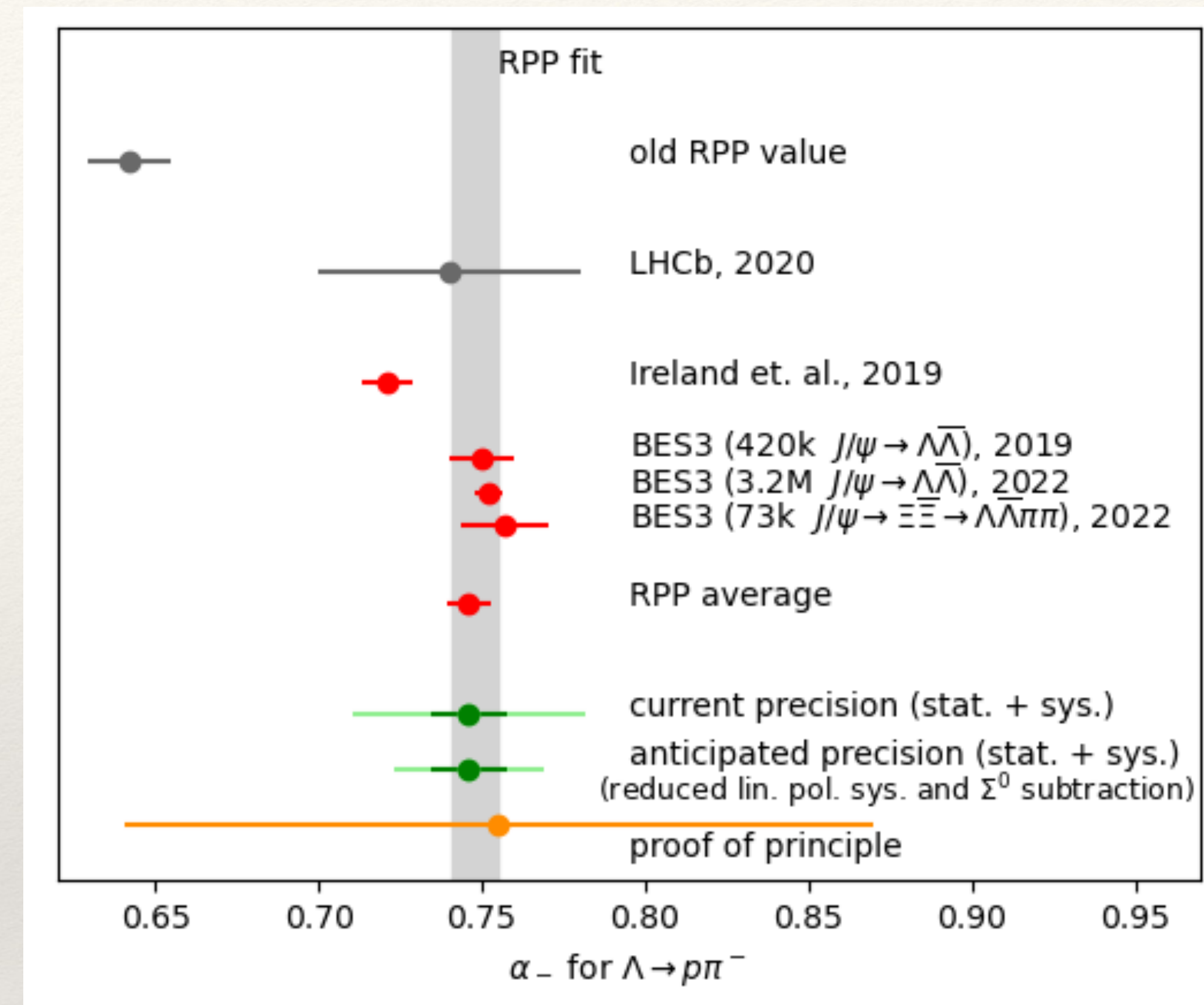


Main systematic for GlueX:

Photon beam linear polarization due to dominance of amplitudes depending on linear polarisation

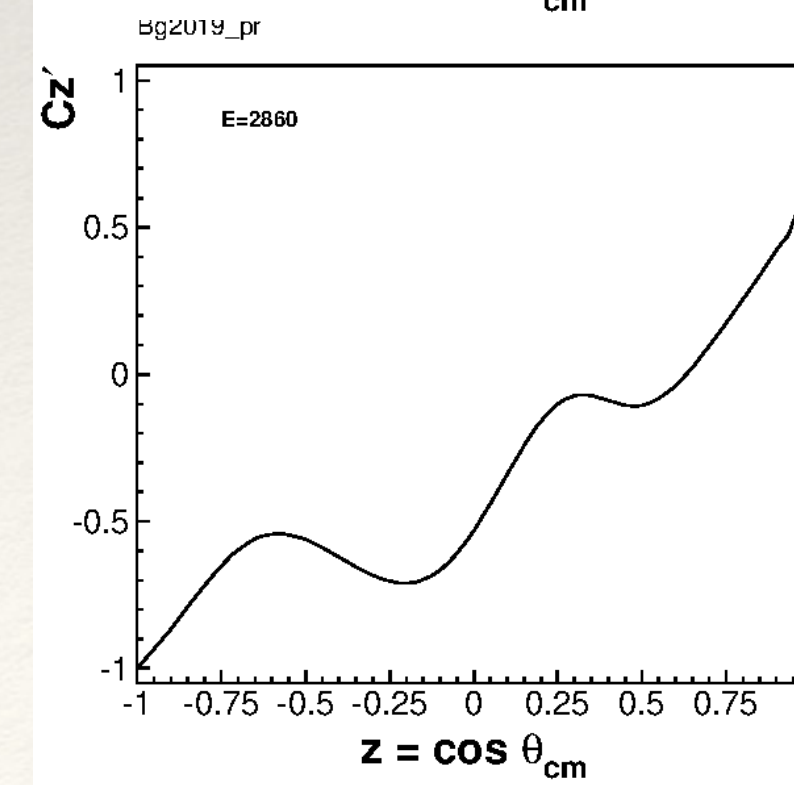
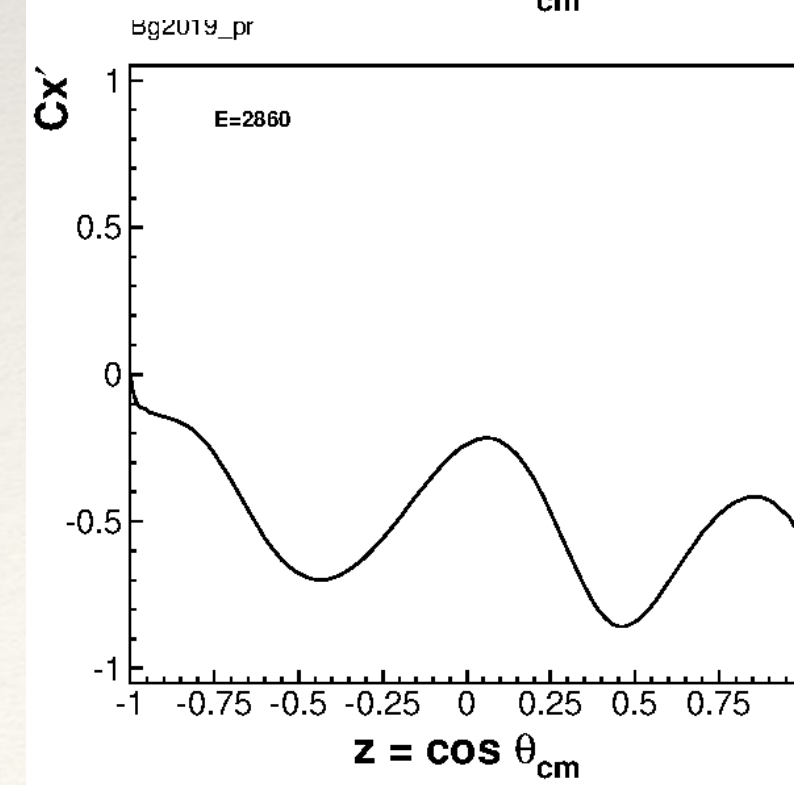
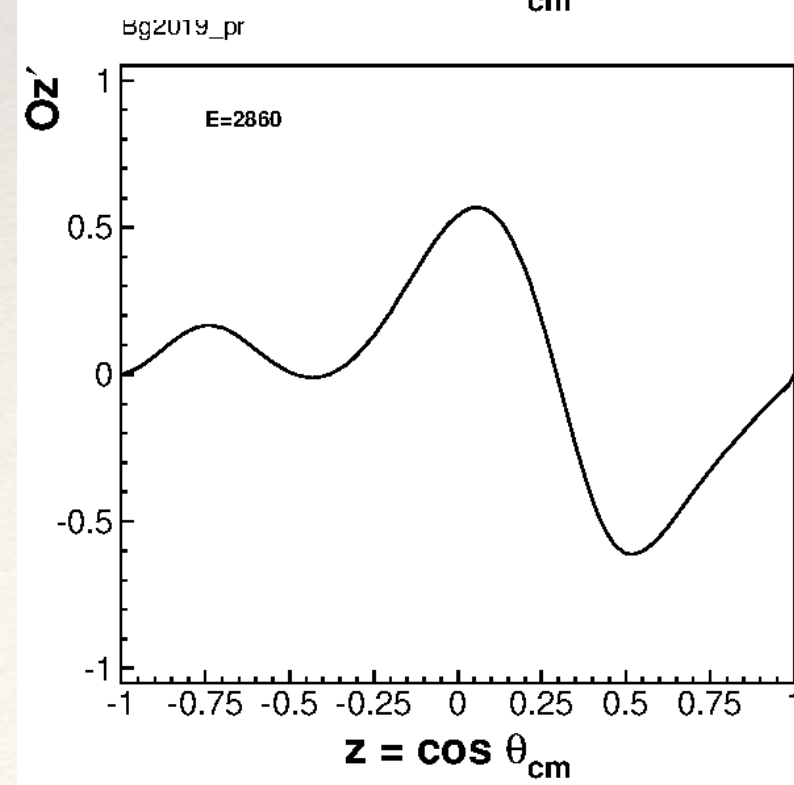
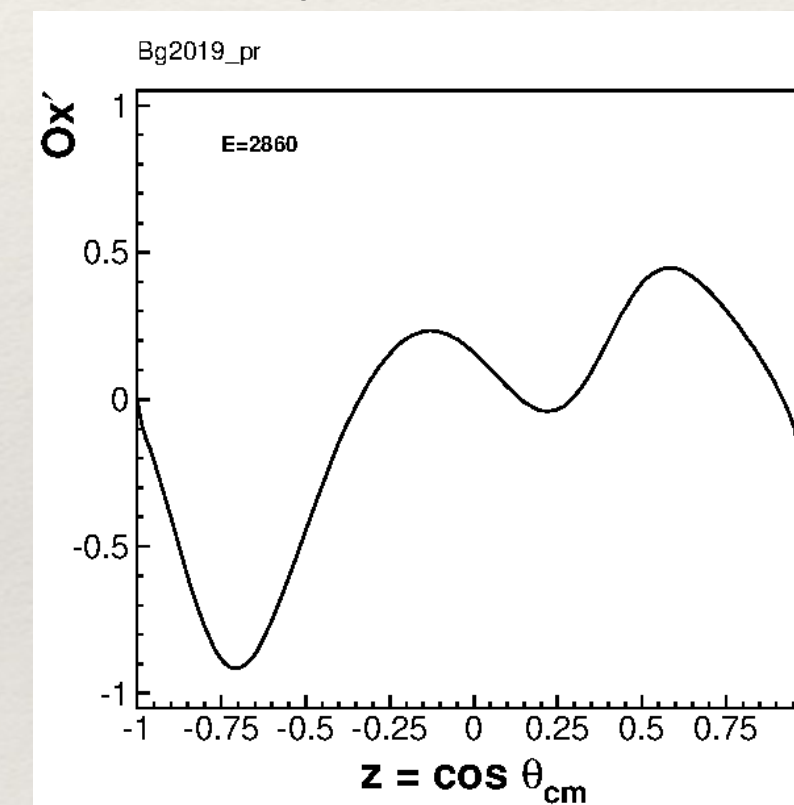
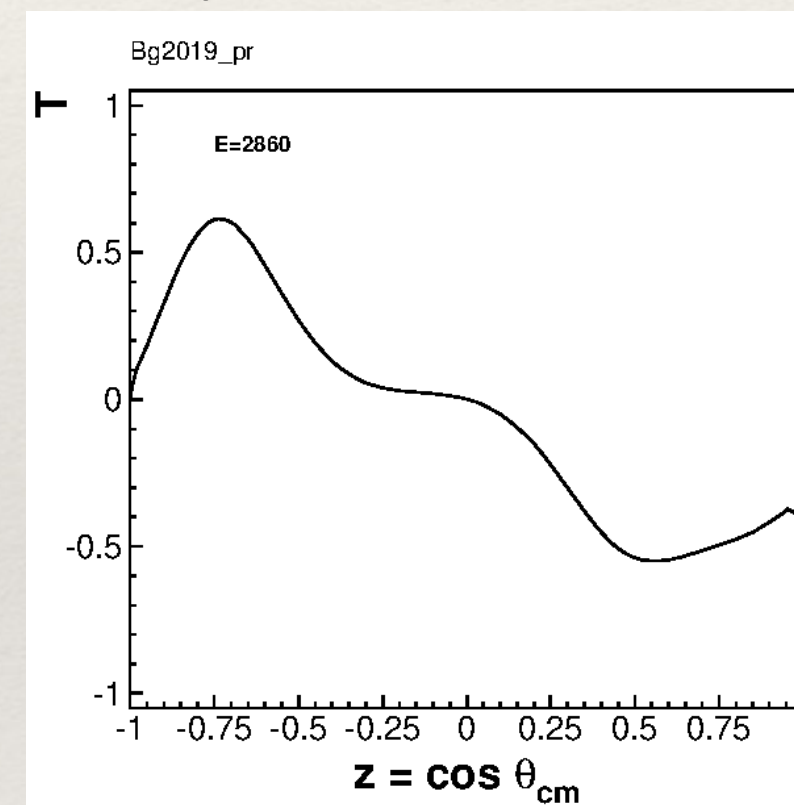
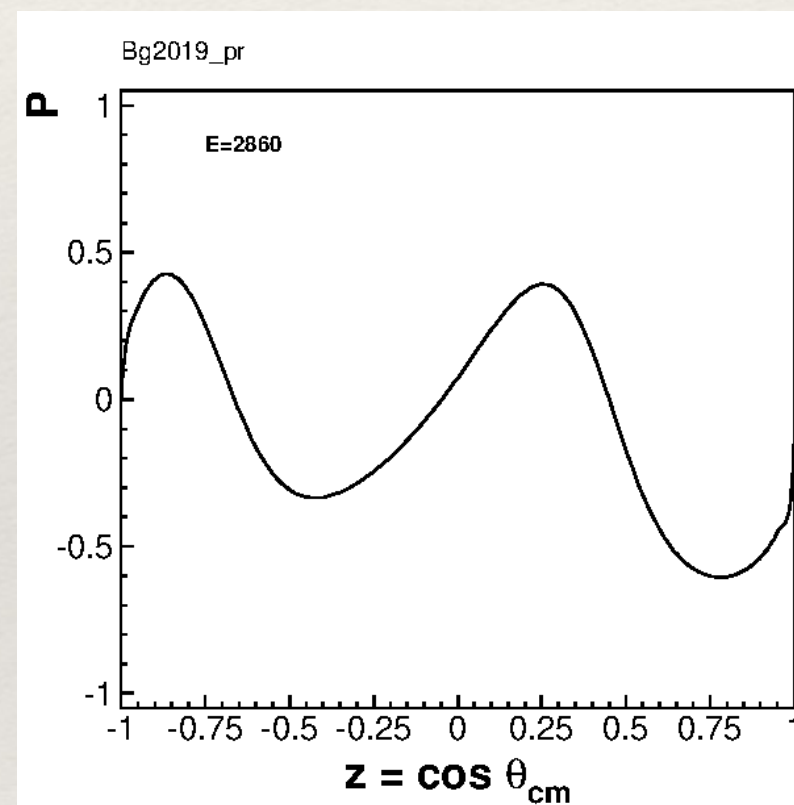
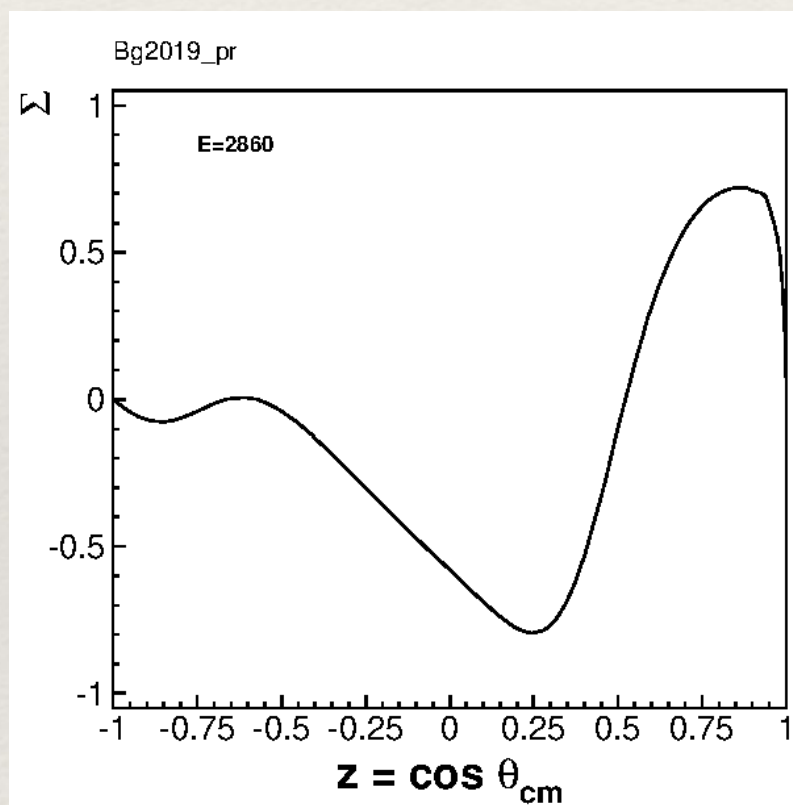
The advantage of lower energies

- ❖ Statistical precision:
 - ❖ Cross sections about factor 10 greater (SLAC: $\sigma \propto 1/E_\gamma^2$)
 - ❖ GlueX-II has about 220d left
 - we can double our statistics with ~3 weeks of running
 - a little over 60d would half our statistical uncertainty
- ❖ Systematic uncertainty:
 - ❖ One would not expect to improve the systematic uncertainty on the determination of degree of linear polarisation
 - ❖ At low energies different polarisation observables would dominate
 - ❖ Access to more central events in CMS
 - ❖ *Potentially* less reliant on linear polarisation



Preliminary study

- ❖ Use BnGa partial-wave analysis results for $E_\gamma = 2860$ MeV and re-run proposal studies
- ❖ Proposal : Σ : 0.9143 P: -0.4888 T: -0.5106 $O_{x'}$: -0.1856 $O_{z'}$: 0.2551 $C_{x'}$: 0.2886 $C_{z'}$: -0.0539
- ❖ $\cos \theta = -0.9$: Σ : -0.0701 P: 0.4081 T: 0.3279 $O_{x'}$: -0.4011 $O_{z'}$: 0.0626 $C_{x'}$: -0.1440 $C_{z'}$: -0.8663
- ❖ $\cos \theta = 0$: Σ : -0.5807 P: 0.0733 T: 0.0006 $O_{x'}$: 0.1596 $O_{z'}$: 0.5400 $C_{x'}$: -0.2374 $C_{z'}$: -0.5328
- ❖ $\cos \theta = 0.9$: Σ : 0.7110 P: -0.5361 T: -0.4183 $O_{x'}$: 0.0451 $O_{z'}$: -0.1310 $C_{x'}$: -0.4291 $C_{z'}$: 0.4227



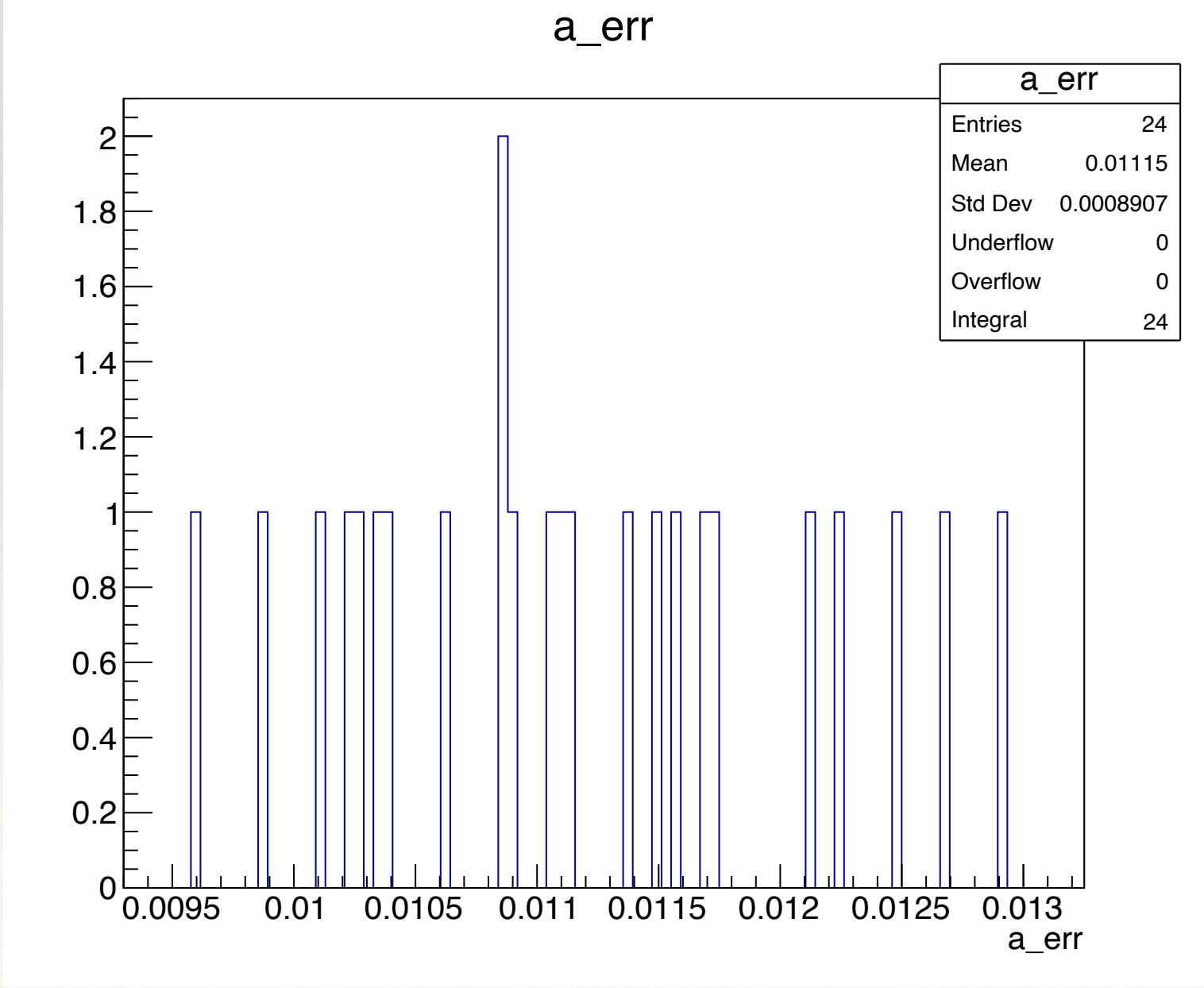
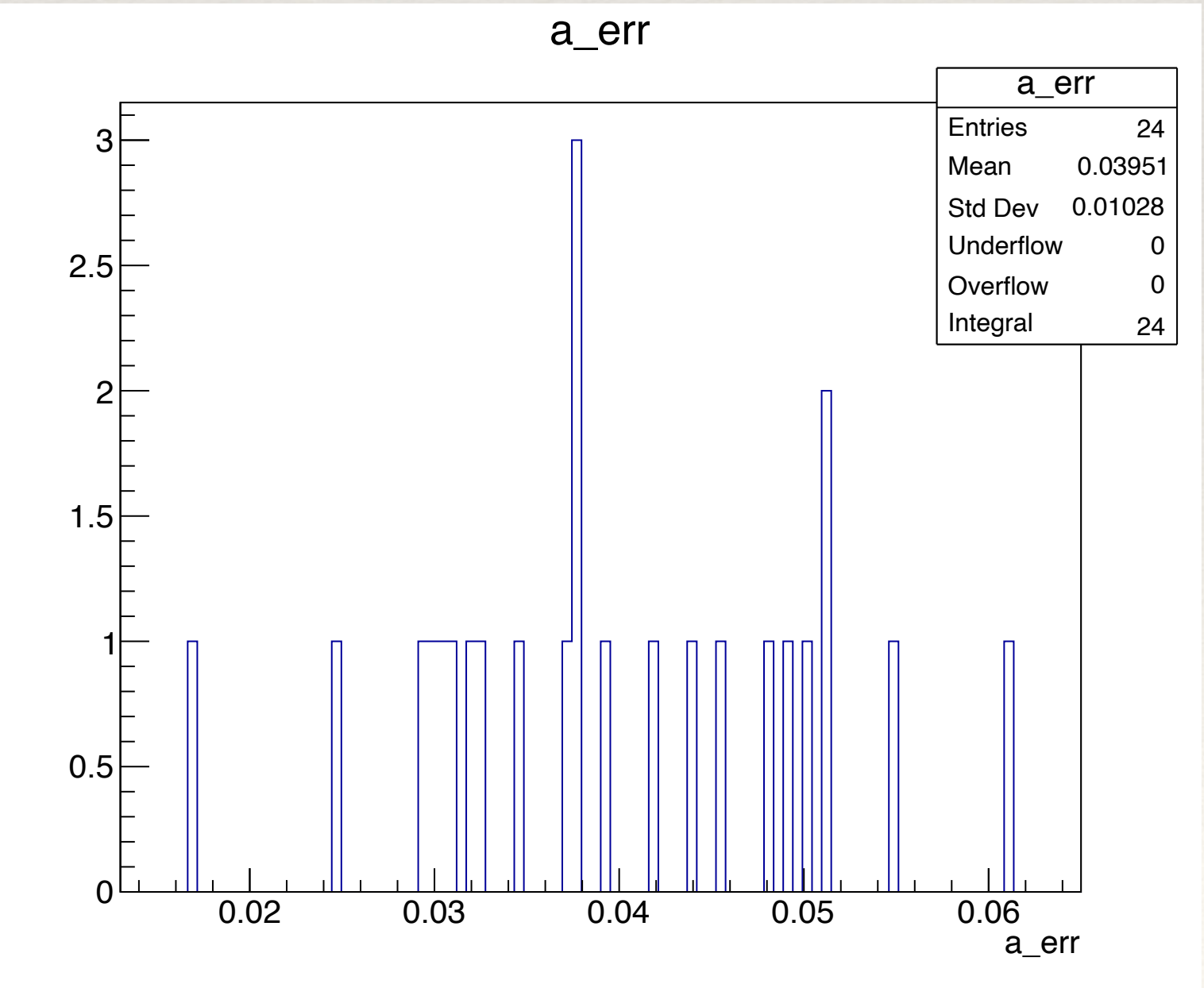
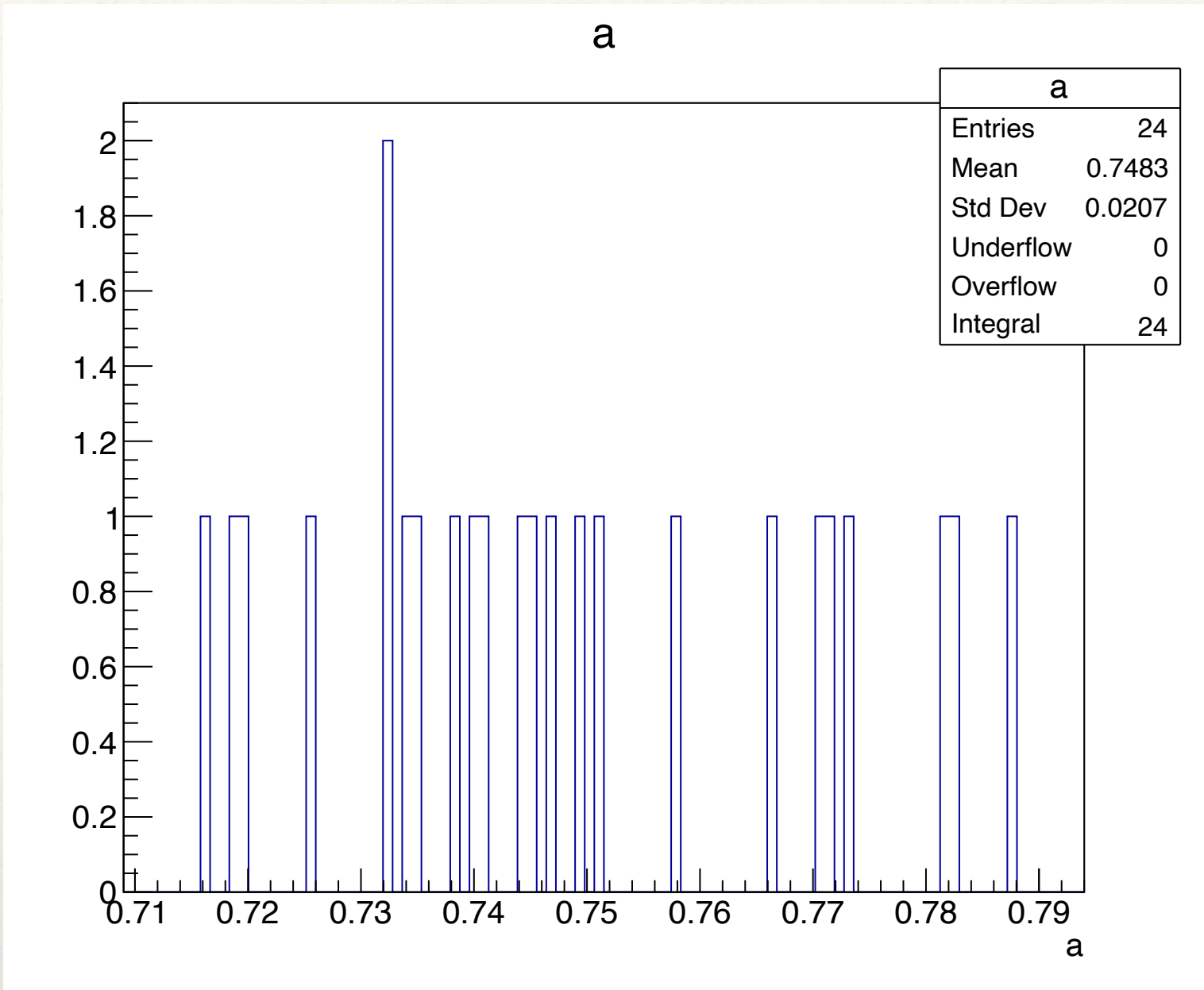
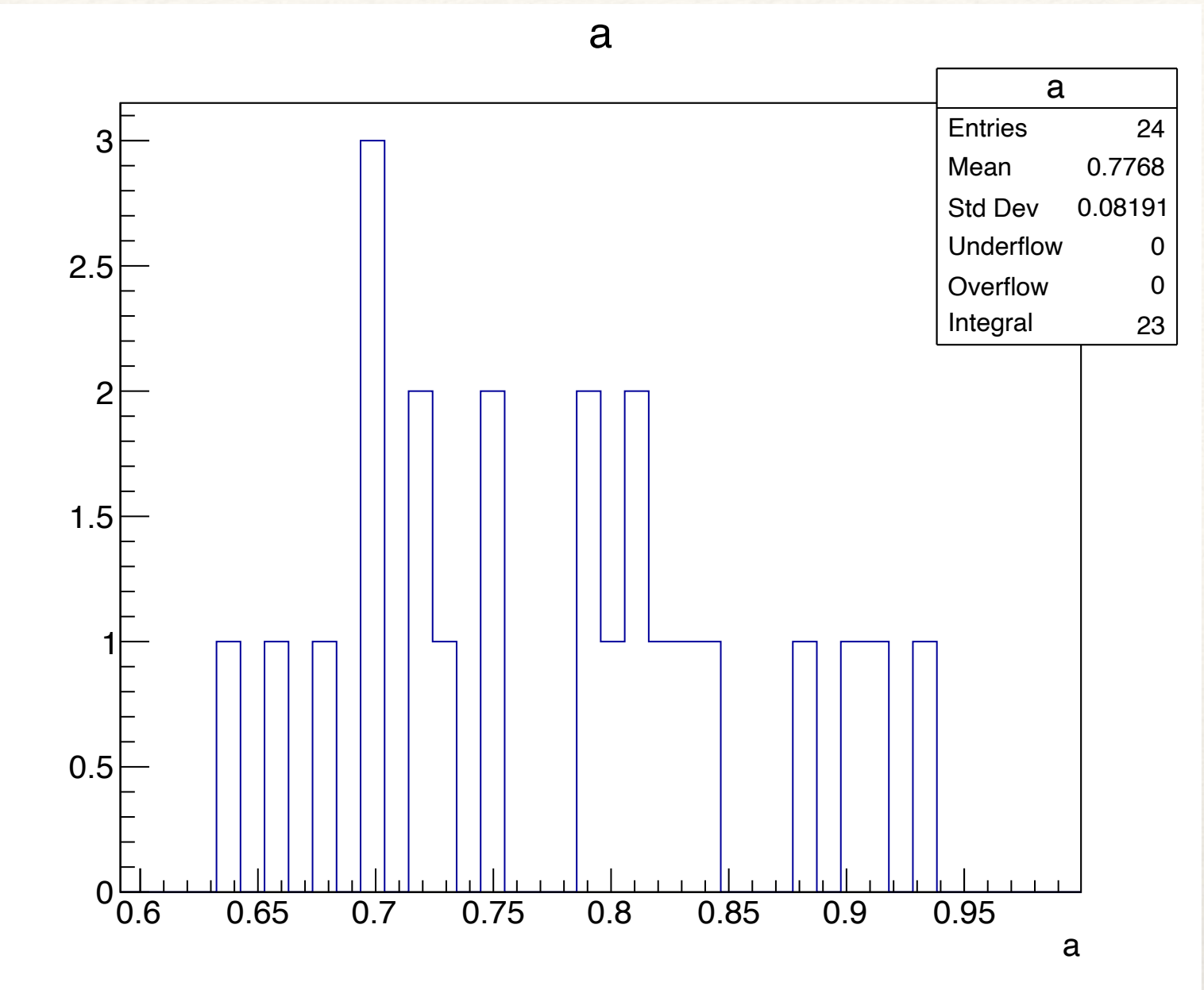
Preliminary study - 24 toys - results

Proposal values

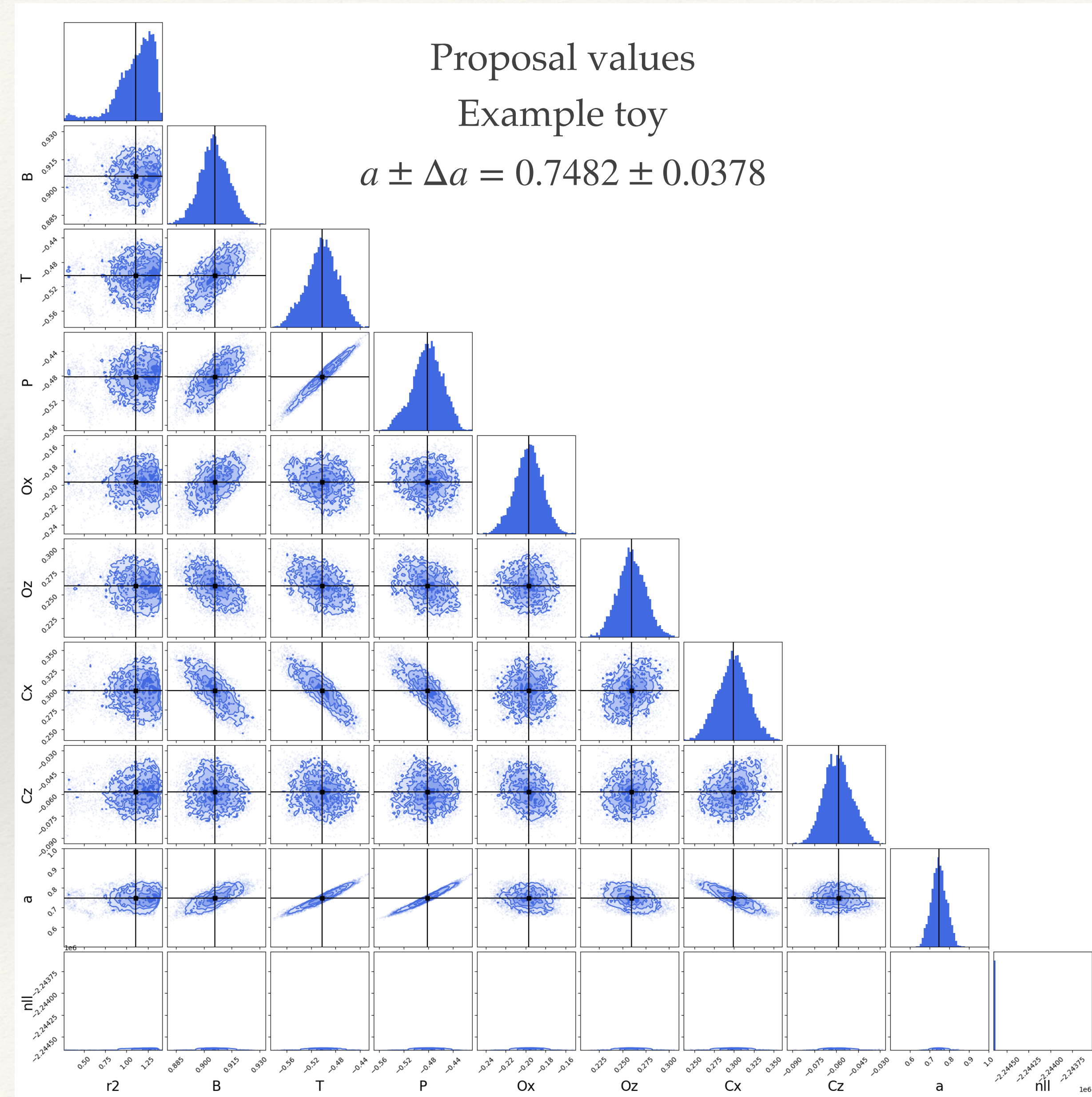
BnGa $\cos \theta = 0.9$

$$\bar{a} \pm \overline{\Delta a} = 0.7768 \pm 0.0395$$

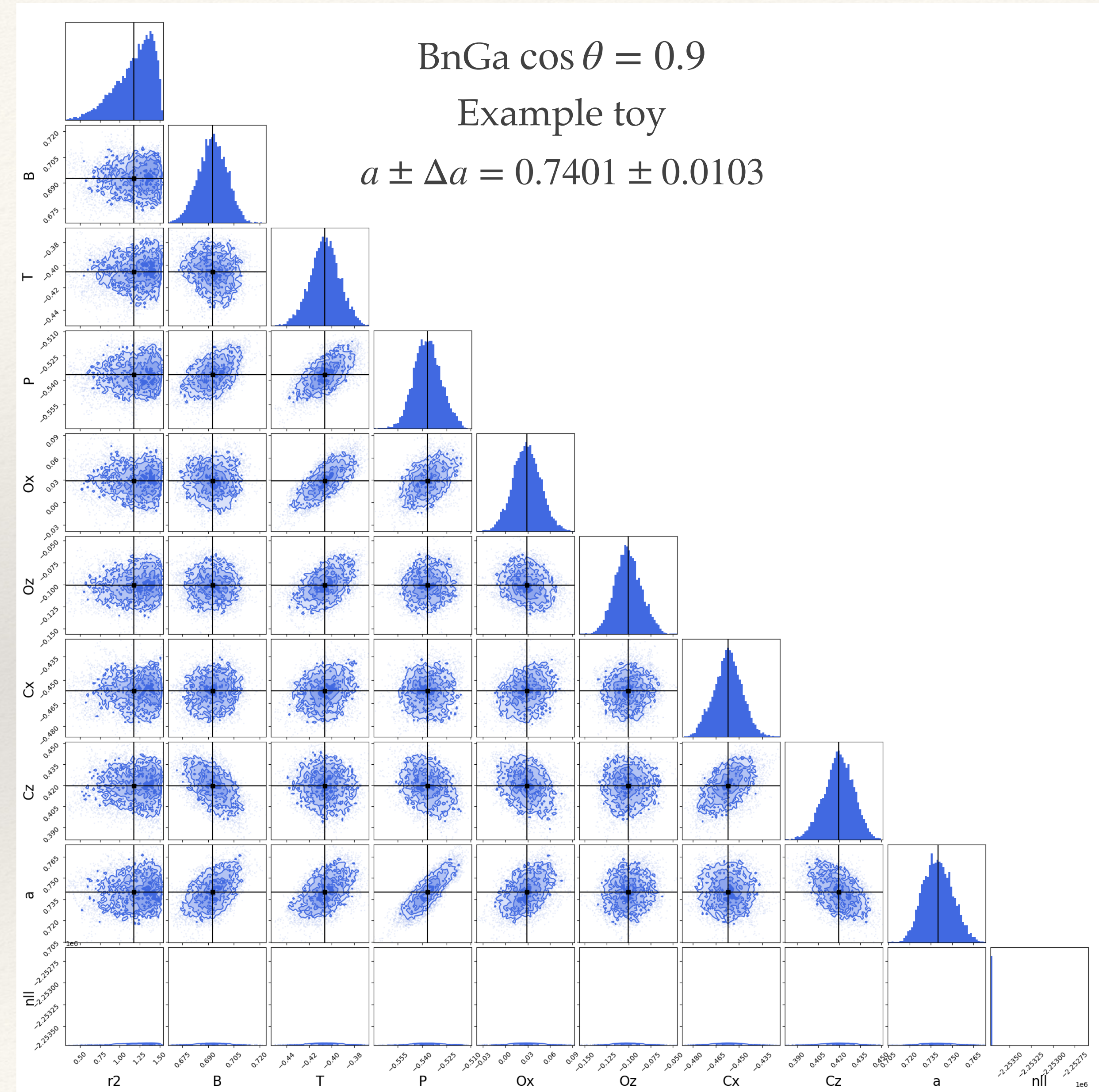
$$\bar{a} \pm \overline{\Delta a} = 0.7483 \pm 0.0112$$



Preliminary study - 24 toys - results



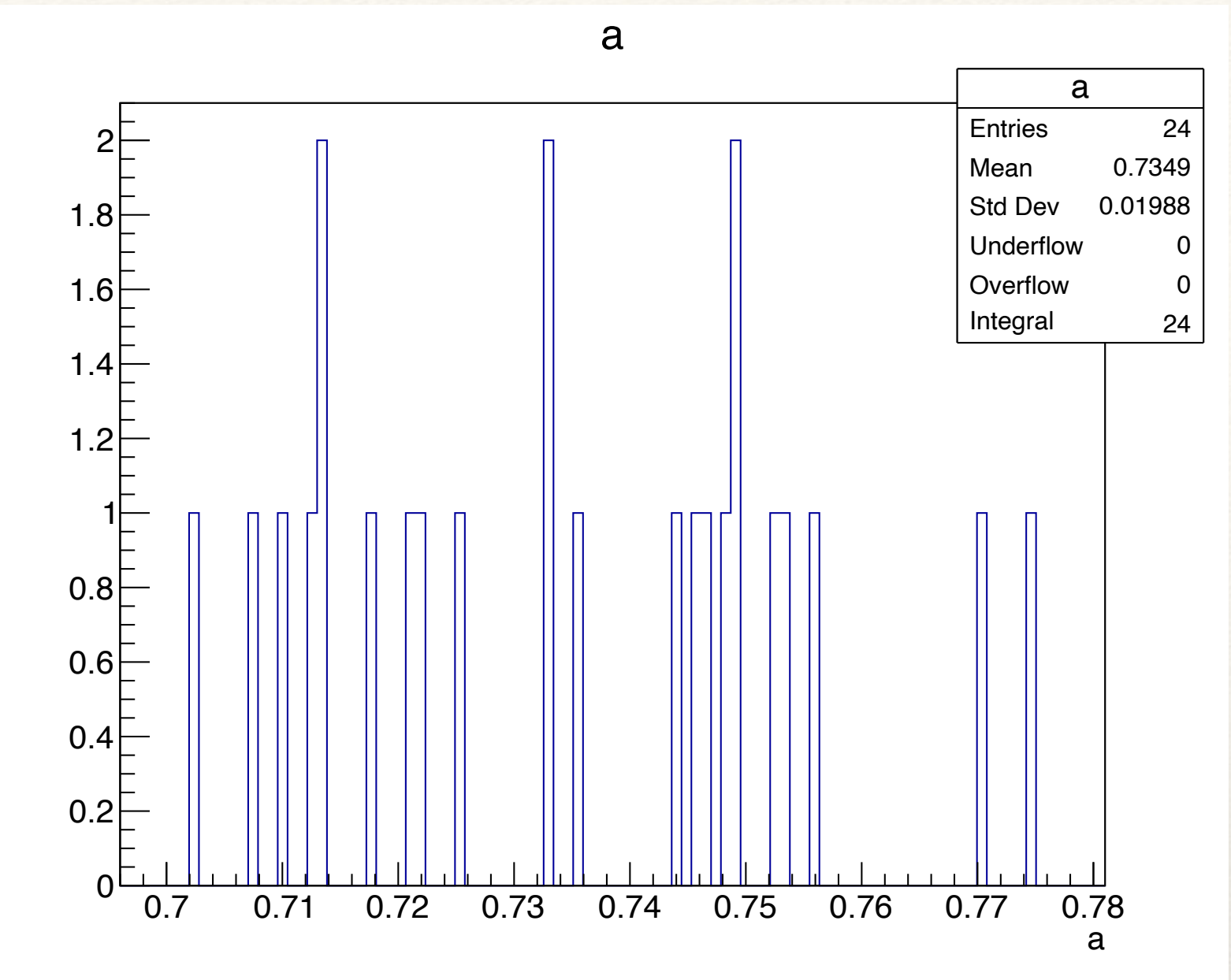
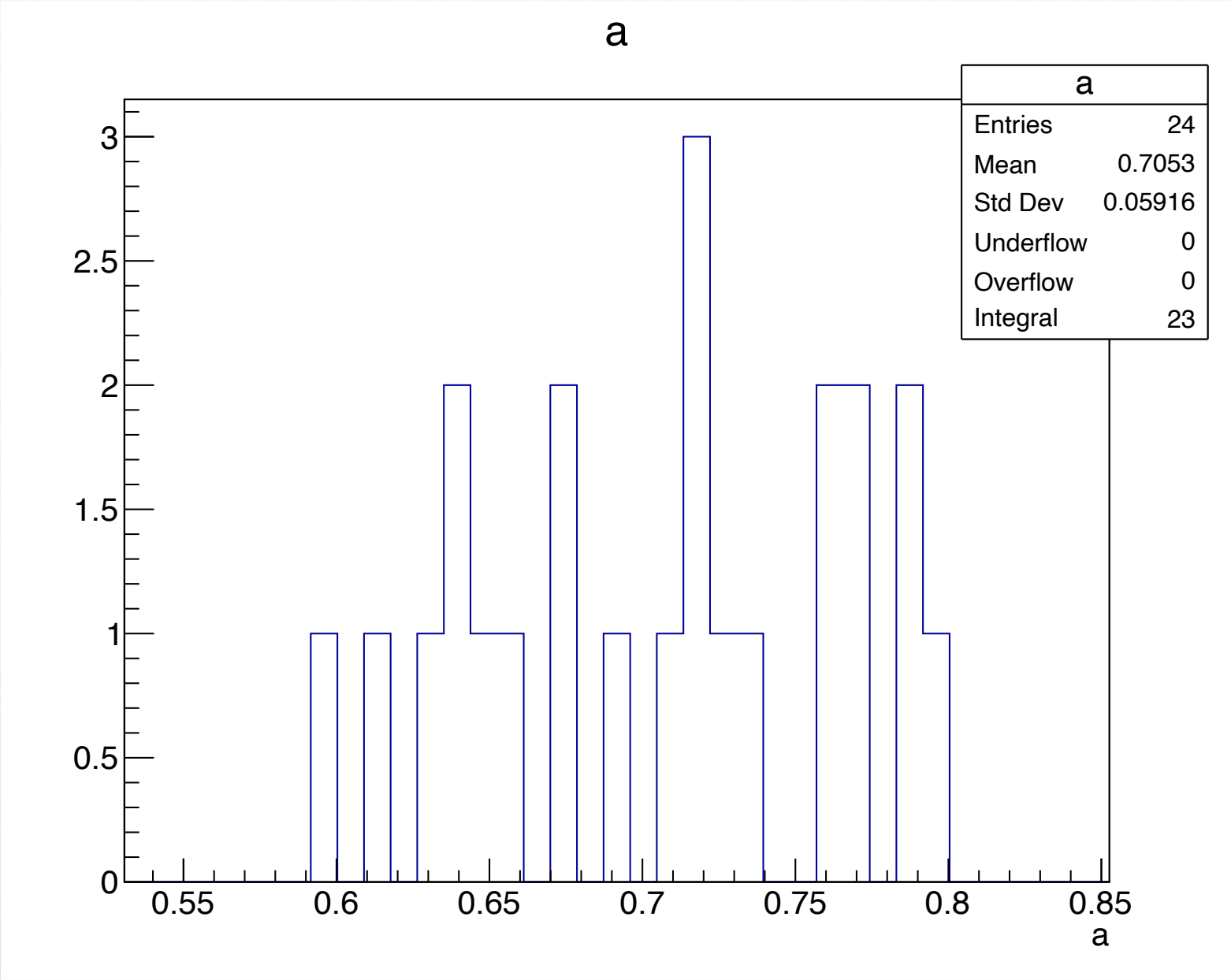
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Preliminary study - 24 toys with 1σ lin. pol. bias- results

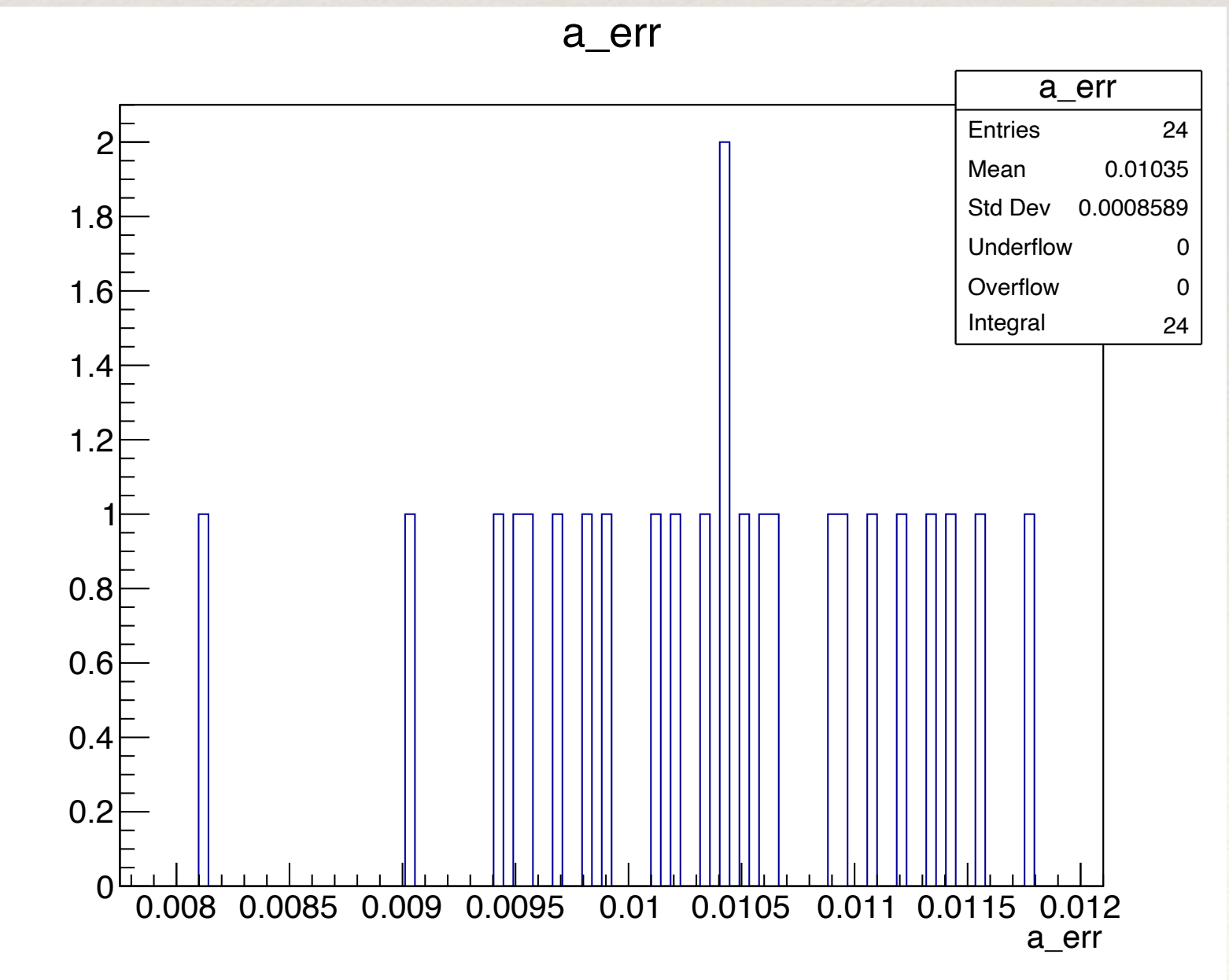
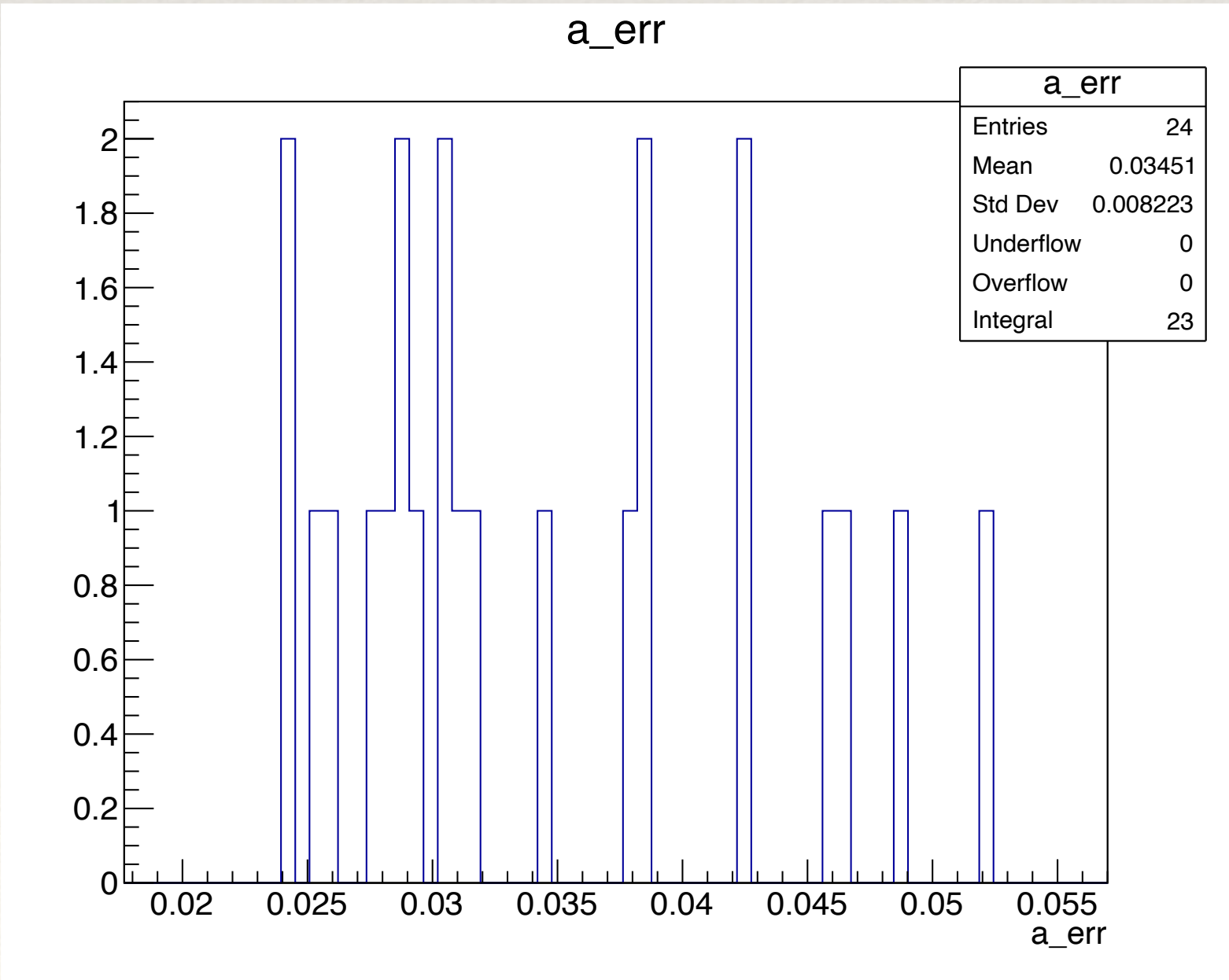
Proposal values

$$\bar{a} \pm \overline{\Delta a} = 0.7053 \pm 0.0345$$



BnGa $\cos \theta = 0.9$

$$\bar{a} \pm \overline{\Delta a} = 0.7349 \pm 0.0104$$



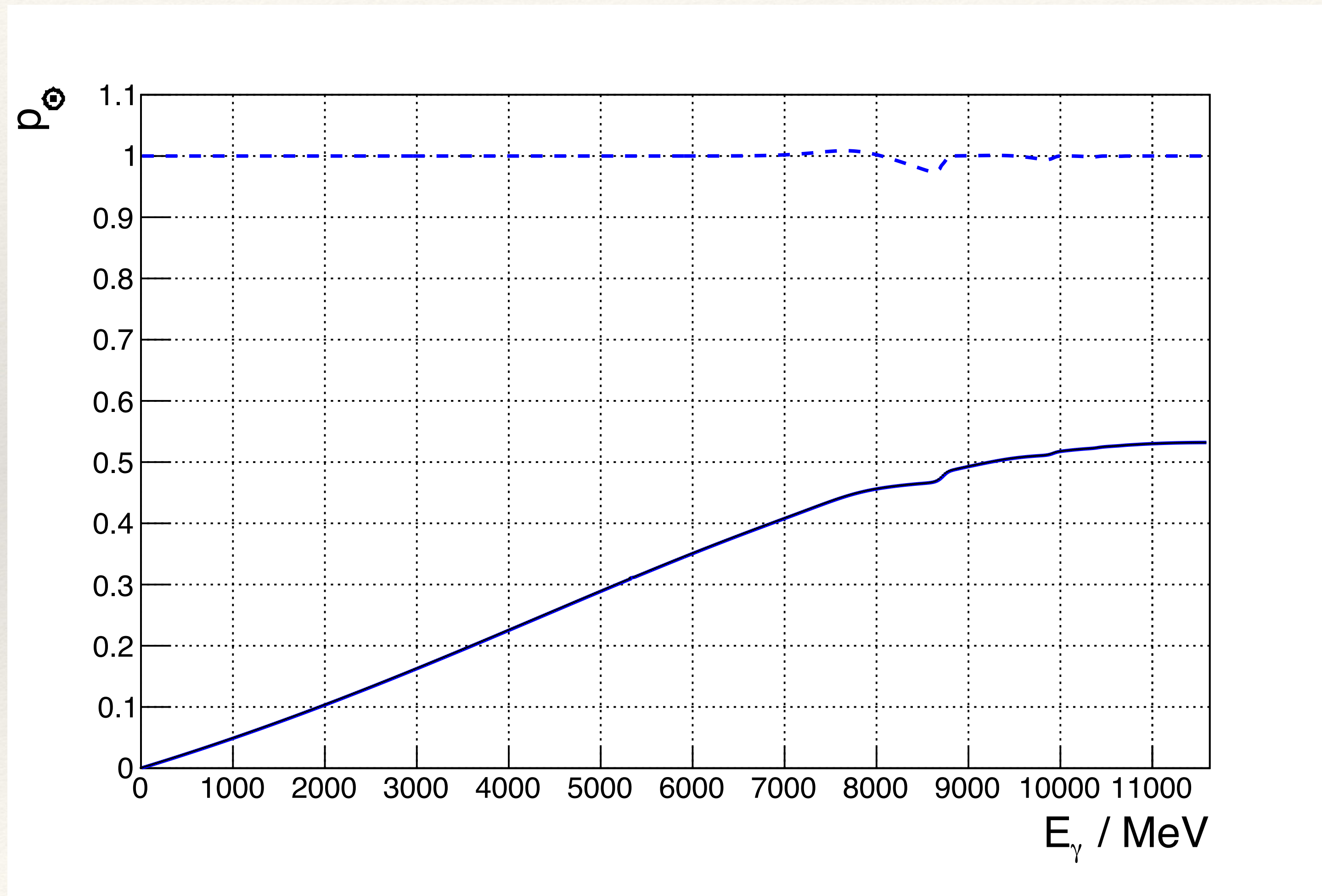
Summary

- ❖ α_+ is an important constant that recently saw large re-adjusting
- ❖ We will provide a “simple” single measurement of α_+ independent of the BESIII methodology and without the drawbacks of the Ireland et al measurement
 - ❖ run in parallel with remainder of GlueX-II
- ❖ At low energies we could
 - ❖ Quickly improve the statistical precision
 - ❖ Perform important systematic cross-checks
 - ❖ ~~Potentially~~ *Very likely* improve the systematics of the measurements significantly
 - ❖ Preliminary studies look very promising

Backup

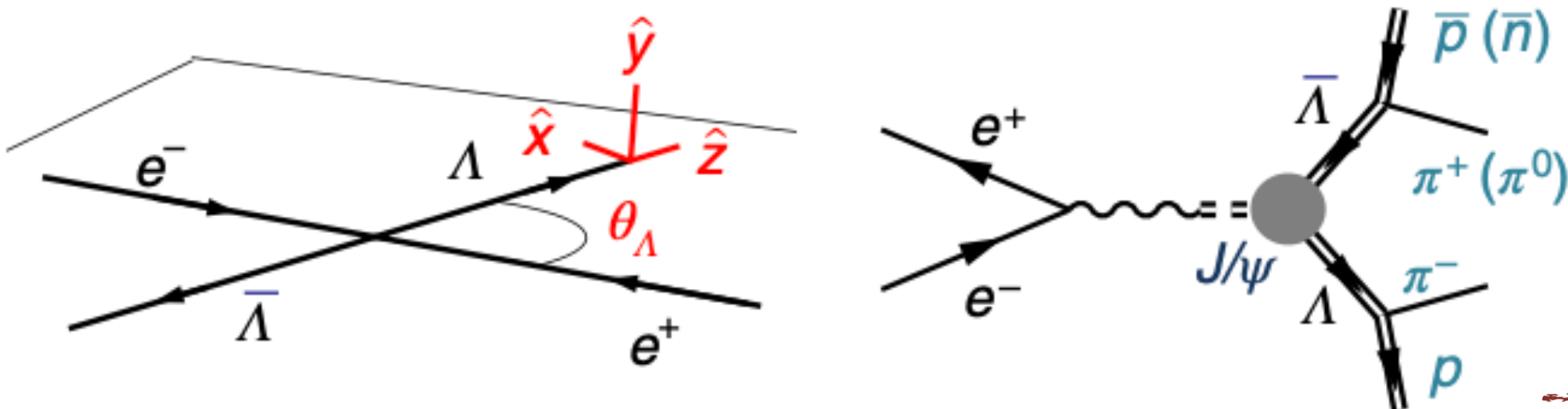
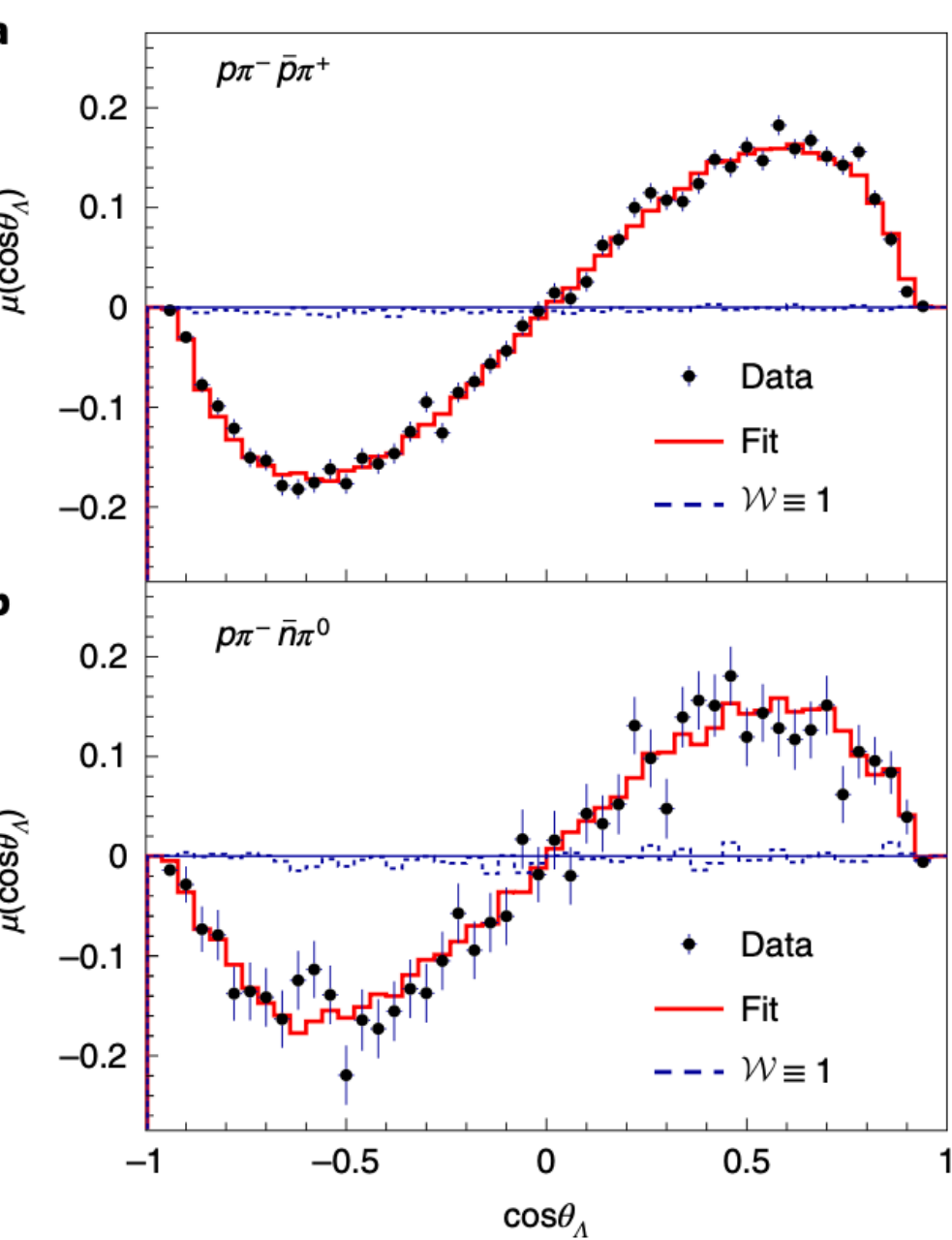
Influence of linear polarization

- ❖ Effect of linear polarisation on circular polarisation is well understood and shown to be small for standard GlueX running conditions



Polarization and entanglement in baryon-antibaryon pair production in electron-positron annihilation

The BESIII Collaboration*



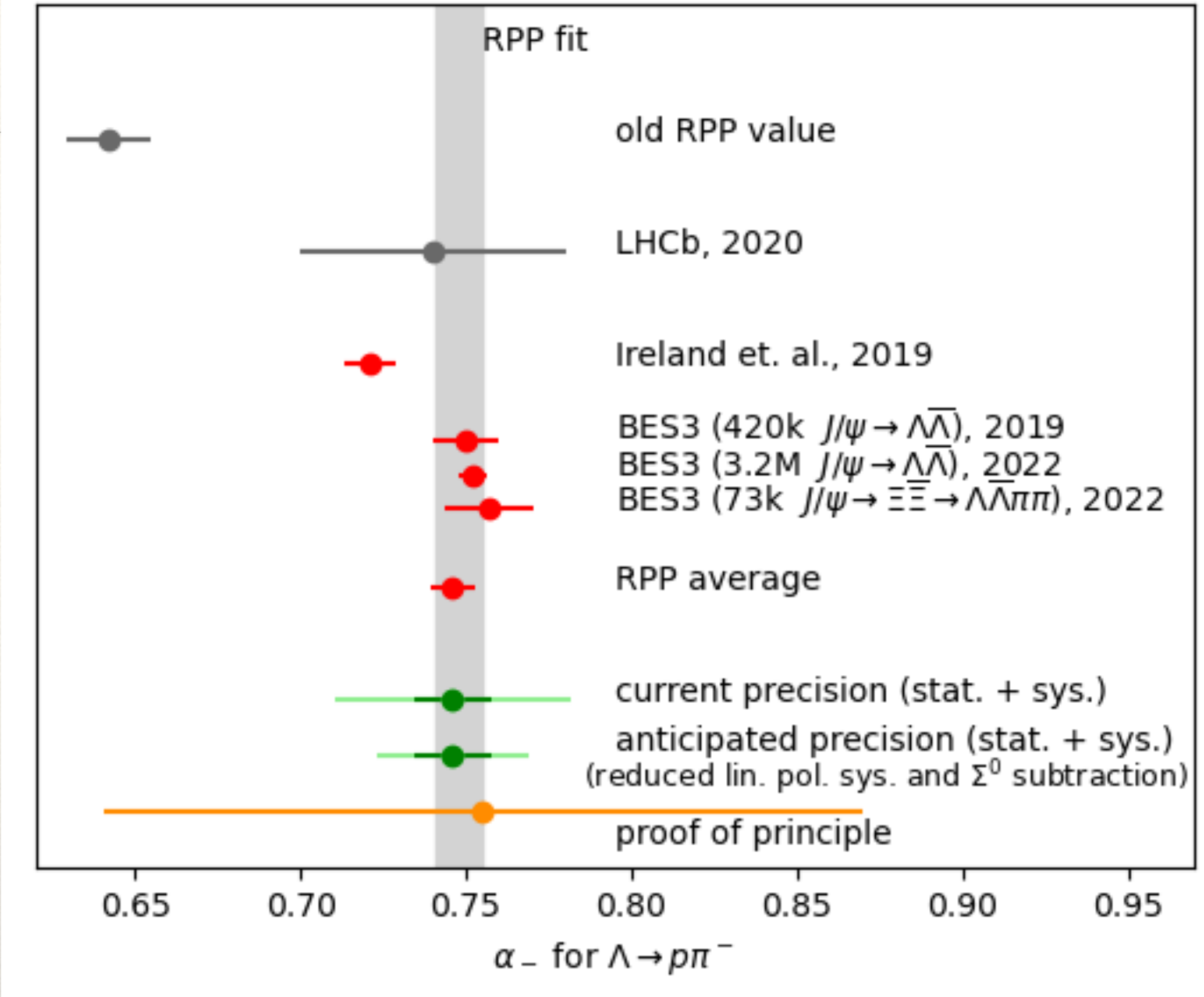
New measurement:
huge discrepancy

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α_-	$0.750 \pm 0.009 \pm 0.004$	0.642 ± 0.013 (ref. ⁶)
α_+	$-0.758 \pm 0.010 \pm 0.007$	-0.71 ± 0.08 (ref. ⁶)

A projection from GlueX data

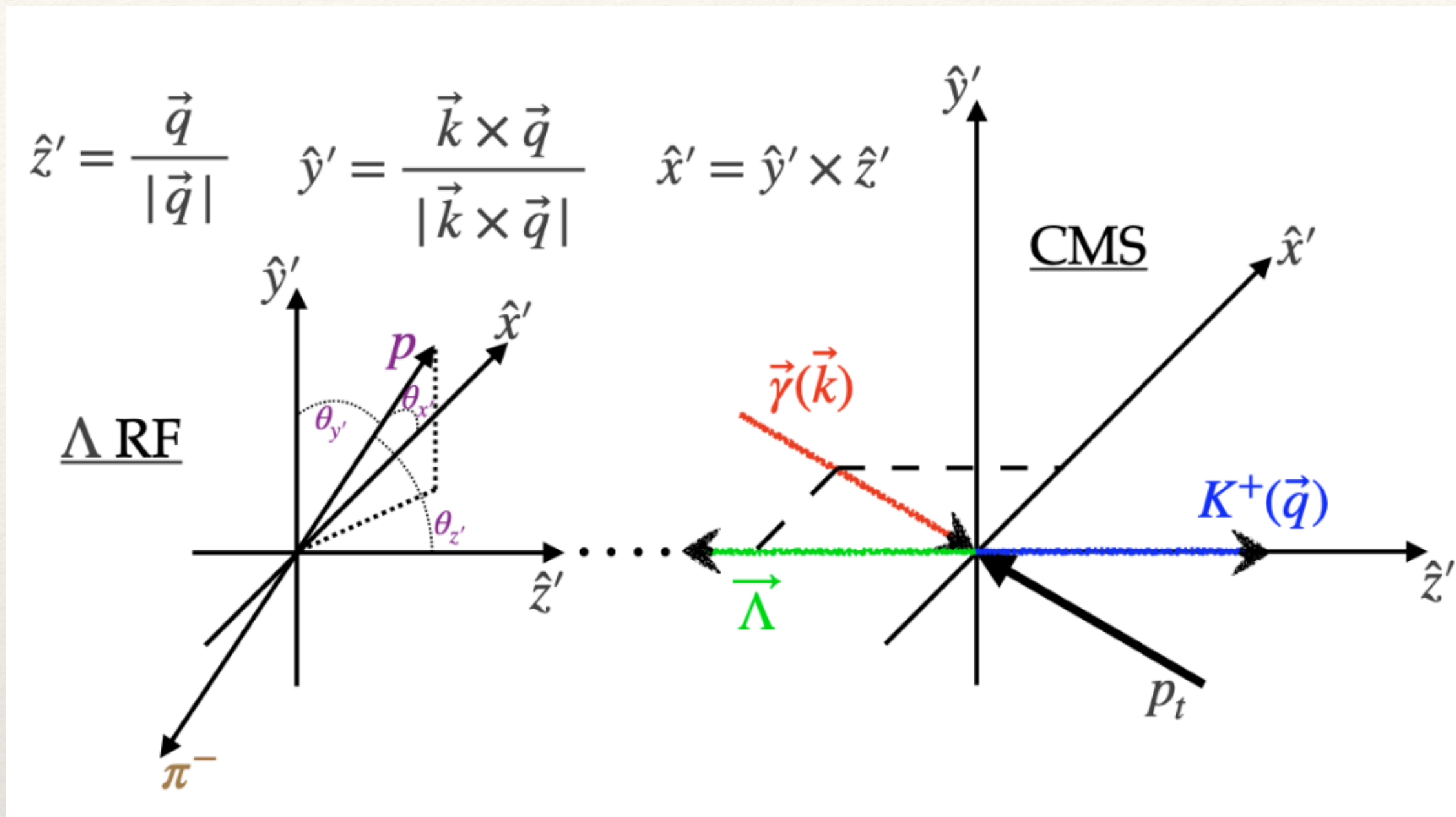
- ❖ Helicity bit was added to GlueX data stream ahead of Spring 2023 data taking
- ❖ Hall D happened to get 50-70% longitudinal polarization
 - ❖ Measured in Halls A/B and projected into Hall D via CEBAF Elegant model
- ❖ About 5% of data analysed for proof-of-concept (very preliminary, calibrations not complete yet)
- ❖ Identified $\sim 8.6\text{k } \gamma p \rightarrow K^+ \Lambda$ events, used to extract $\alpha_- = 0.755 \pm 0.115$ (sys. only)
- ❖ Used this result together with MC studies to estimate achievable precision with remainder of GlueX-II running with $\sim 80\%$ longitudinal polarization \rightarrow statistical precision comparable to previous results



- ❖ Anticipate some improvements to determination of linear polarization and subtraction of backgrounds
- ❖ Final anticipated uncertainties: 0.012 (stat) + 0.021 (sys)

	% uncertainty	% contribution	absolute contribution
Photon beam circular polarization	2%	<0.2%	<0.002
Photon beam linear polarization	<2%	<4%	<0.03
Acceptance	2%	2%	0.015
Σ contamination	<2.5%	<0.3%	<0.002
Total (current upper limit)		<4.5%	<0.034
Total (anticipated)		2.8%	0.021

Methodology



- ❖ Identify $\gamma p \rightarrow K^+ \Lambda$, $\Lambda \rightarrow p \pi^-$
- ❖ Measure $\Phi, \cos \theta_{x'}, \cos \theta_{y'}, \cos \theta_{z'}$
- ❖ Fit intensity function with α_- as free parameter, using transversity amplitudes

$$\begin{aligned} \frac{d\sigma}{dt} &= |b_1|^2 + |b_2|^2 + |b_3|^2 + |b_4|^2 \\ \Sigma \frac{d\sigma}{dt} &= |b_1|^2 + |b_2|^2 - |b_3|^2 - |b_4|^2 \\ T \frac{d\sigma}{dt} &= |b_1|^2 - |b_2|^2 - |b_3|^2 + |b_4|^2 \\ P \frac{d\sigma}{dt} &= |b_1|^2 - |b_2|^2 + |b_3|^2 - |b_4|^2 \\ O_{x'} \frac{d\sigma}{dt} &= -2 \operatorname{Re}(b_1 b_4^* - b_2 b_3^*) \\ O_{z'} \frac{d\sigma}{dt} &= -2 \operatorname{Im}(b_1 b_4^* + b_2 b_3^*) \\ C_{x'} \frac{d\sigma}{dt} &= 2 \operatorname{Im}(b_1 b_4^* - b_2 b_3^*) \\ C_{z'} \frac{d\sigma}{dt} &= -2 \operatorname{Re}(b_1 b_4^* + b_2 b_3^*) \end{aligned}$$

$$\begin{aligned} I = 1 &+ \alpha_- \cos \theta_{y'} P - P_\gamma \cos(2\Phi) (\Sigma + \alpha_- \cos \theta_{y'} T) \\ &- P_\gamma \sin(2\Phi) (\alpha_- \cos \theta_{x'} O_{x'} + \alpha_- \cos \theta_{z'} O_{z'}) \\ &- P_\odot (\alpha_- \cos \theta_{x'} C_{x'} + \alpha_- \cos \theta_{z'} C_{z'}) \end{aligned}$$