

Evaluation of the starting values
of hybrid baryon electrocouplings
 $A_{1/2}(Q^2)$, $A_{3/2}(Q^2)$, $S_{1/2}(Q^2)$ for
the simulation of K^+ exclusive
electroproduction events at protons. (1)

1. Objective: Determine the values of
 $A_{1/2}$, $A_{3/2}$, $S_{1/2}$ hybrid electrocouplings
at different Q^2 above
which signal from hybrid baryon
will be detected with the
CLAS12

2 Hybrid parameters:

Spin/Parity: $1/2^+$, $3/2^+$

Mass: $M_H = 2.20 \text{ GeV}$

(1) Full decay width: $\Gamma_H = 0.25 \text{ GeV}$

$\Gamma(H \rightarrow K^+)$ according Eq (4) p. 27
at LOI

$$\Gamma(H \rightarrow K^+) = \Gamma_{K^+} = \frac{1}{2} \cdot 0.25 \cdot 0.05 = 0.00625 \text{ GeV}$$

(2)

The values of $A_{1/2}$, $A_{3/2}$, $S_{1/2}$ electrocouplings of hybrid baryon above which the hybrid state will be detected with the CLAS12 should be determined at the grid of Q^2 :

(2) Q^2 : 0.05, 0.20, 0.40, 0.60, 0.8, 1.0 GeV^2

For hybrid at $3/2^+$, $1/2^+$ they should be determined varying single parameter A of Eq. (11) p. 28 of LOI

For the hybrid at $1/2^+$ in addition, electrocouplings should be determined varying $A_{1/2}$ with $S_{1/2} = 0$.

3. How to ~~determine~~ estimate the start values for $A_{1/2}$, $A_{3/2}$, $S_{1/2}$ before the event simulation

For different values of parameter A ($A_{1/2}$, $S_{1/2} = 0$ for $J^P = 1/2^+$) compute unpolarized differential cross sections

$d\sigma/d(-\cos\theta_K)_0$ without hybrid and

$d\sigma/d(-\cos\theta_k)_H$ with hybrid contribution ⁽³⁾

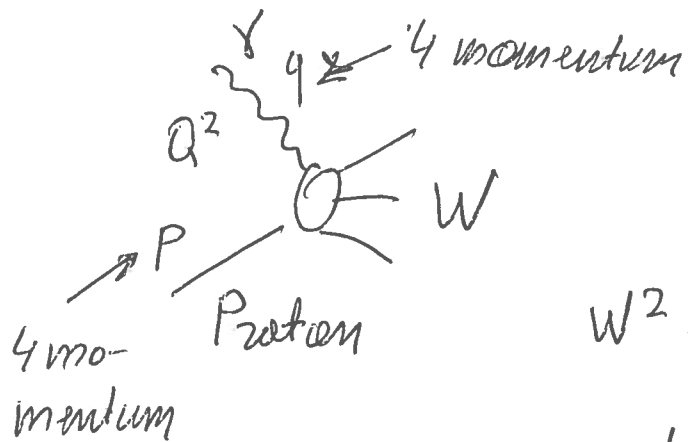
$$\frac{d\sigma}{d(-\cos\theta_k)_{0,H}} = \frac{d\sigma}{d\Omega_{k,0,H}} \cdot 2\pi \quad (3)$$

$$\frac{d\sigma}{d\Omega_{k,0,H}} = \frac{d\sigma_T}{d\Omega_{k,0,H}} + \varepsilon_L \frac{d\sigma_L}{d\Omega_{k,0,H}} \quad (4)$$

Two terms in Eq (4) can be evaluated both in JM or (Ghent) conventions employing the transformation factors for the non-resonant Ghent $\rightarrow$ JM (resonant JM $\rightarrow$ Ghent) amplitudes.

3a. Evaluation of ε_L

Should be done according to Eq (14), Eq (20) of LDI in pp. 29 and 30, respectively.
 $tg \frac{\theta_e}{2}$ and ν should be derived from the values of W and Q^2 and the initial electron beam energy $\bar{E}_0$ as:



$$V = \frac{qP}{M_N}$$

(4)

$$W^2 = (q + P)^2 = -Q^2 + M_N^2 + 2M_N V$$

$$V = \frac{W^2 + Q^2 - M_N^2}{2M_N} \quad (5)$$

$$Q^2 = 4E_0(E_0 - \nu) \sin^2 \frac{\theta_e}{2}$$

$$\sin^2 \frac{\theta_e}{2} = \frac{Q^2}{4E_0(E_0 - \nu)} \quad (6)$$

$$\cos^2 \frac{\theta_e}{2} = \left(1 - \sin^2 \frac{\theta_e}{2}\right) \quad (7)$$

$$\begin{aligned} \tan^2 \frac{\theta_e}{2} &= \frac{Q^2}{4E_0(E_0 - \nu) \left(1 - \frac{Q^2}{4E_0(E_0 - \nu)}\right)} \\ &= \frac{Q^2}{4E_0(E_0 - \nu) - Q^2} \quad (8) \end{aligned}$$

$$E_0 = 11.6 \text{ eV}$$

3b. Cross section grid and uncertainties

The differential cross sections (4) should be evaluated at each Q^2 of (2) at W grid

(9) W: 2.0, 2.1, 2.15, 2.20, 2.25, 2.30, 2.50 GeV

(10) ~~in~~ in 10 equal bins over θ_{12} from 0 to 180°

The $\chi^2/\text{d.p.}$ for the ~~cross diff~~ difference of differential cross sections computed with/without hybrid should be evaluated as:

$$\chi^2/\text{d.p.} = \frac{1}{N_{\text{d.p.}}} \sum_{W_i, \theta_j} \frac{\left[\frac{d\sigma}{d(-\cos\theta_{12})_H} - \frac{d\sigma}{d(-\cos\theta_{12})_0} \right]^2}{\delta_{i,j}^2} \quad (11)$$

at any given Q^2 ~~Q^2~~

the sum is running over all bins of ~~Q^2~~ W, and θ_{12} Eqs (2, 9, ~~10~~). $N_{\text{d.p.}}$ stands for the total number of the data points at given Q^2

$$\delta_{1/d} = \sqrt{\delta_H^2 + \delta_0^2} \quad (12)$$

$$\delta_H = \frac{d\sigma}{d(-\cos\theta_K)_H} \cdot \varepsilon_{\text{dat}} \quad (13)$$

$$\delta_0 = \frac{d\sigma}{d(-\cos\theta_{K0})} \cdot \varepsilon_{\text{dat}} \quad (14)$$

The cross section uncertainties

$$\varepsilon_{\text{dat}} = \begin{array}{ll} 5\% & \text{for } K^+ \\ 10\% & \text{for } K^- \end{array}$$

Varying parameter A of Eq (1) of LOI
(or $A_{1/2}$, $S_{1/2} = 0$ for $\sqrt{s} = 1/2^+$, in addition)
in each bin of Q^2 of (5) at write-up
independently to determine A -value
at which $\chi^2/\text{d.p.} > 2.0$

The minimal values $A_{1/2}(Q^2)$, $A_{3/2}(Q^2)$
 $S_{1/2}(Q^2)$ can be computed from A
(or $A_{1/2}$ determined directly for $\sqrt{s} = 1/2^+$
(in addition))