A Proposal to Jefferson Lab PAC53

Measurement of the Two-Photon Exchange Contribution in Electron-Neutron and Positron-Neutron Elastic Scattering

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Executive Summary

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Following up Letter-Of-Intent LOI12+24-008, we propose the measurement of the two-2 photon exchange contribution (TPE) in elastic positron-neutron and electron-neutron scat-3 tering at three four-momentum transfers Q^2 of 3.0, 4.5, and 5.5 (GeV/c)². This measure-4 ment purports to complete and extend the measurement of the two-photon exchange in 5 electron-neutron scattering submitted to and approved by PAC48 in 2020, and recorded in 6 2022 (experiment E12-20-010, currently under analysis). This program means to address the 7 open question of the discrepancy between G_E/G_M ratios measured in elastic electron-nucleon 8 scattering via Rosenbluth separation on the one hand and polarization transfer on the other 9 hand, often explained by a different sensitivity of each of the experimental methods to the 10 TPE contribution. The measurement of the positron-neutron over electron-neutron cross 11 section ratio provides a direct access to the TPE contribution, which can be compared to 12 the discrepancy between Rosenbluth slope measurements and polarization measurements. 13

The proposed experiment shall be performed with the Super BigBite Spectrometer (SBS), 14 combined with the BigBite (BB) spectrometer, installed in Hall C, and using the pro-15 posed positron beam upgrade for CEBAF. It will measure simultaneous neutron and pro-16 ton elastic scattering off deuterium, with positrons and electrons, at two beam energies of 17 3.3 and 4.4 GeV for $Q^2 = 3.0 \ (GeV/c)^2$, and 4.4 and 6.6 GeV for $Q^2 = 4.5 \ (GeV/c)^2$ and 18 ${\rm Q}^2=5.5~({\rm GeV/c})^2.$ For each of the measured ${\rm Q}^2$, the combination of electron and positron 19 data sets will provide positron/electron neutron cross section ratios $R_{2\gamma}^n$; the combination 20 of energy datasets will provide measurements of the Rosenbluth slope S^n on electrons and 21 positrons. Using the maximum proposed intensity of 1 μ A for unpolarized positrons, as well 22 as 1 μ A for electrons, this measurement requires 28.33 PAC days (14 on e^+ , 14 on e^-) on 23 a 15 cm cryogenic deuterium target, 10 PAC days (5 on e^+ , 5 on e^-) on a 15 cm cryogenic 24 hydrogen target for calibrations and equipment monitoring, distributed on all six settings, 25 1.33 PAC days with electrons at 5 and 10 μ A for special measurements (optics, neutron de-26 tection efficiency) and 9.33 PAC days for kinematic changes and accelerator reconfiguration 27 for positron/electron changes. The analysis of the proposed experiment will greatly benefit 28 on the return of experience of the ongoing analysis of E12-20-010. 29

I. INTRODUCTION

In 1950s, a series of experiments performed by R. Hofstadter [1] revealed that nucleons 31 have a substructure (which corresponds to our modern view in terms of quarks and gluons). 32 The experiment confirmed M. Rosenbluth's theory of electron scattering [2] based on the one-33 photon exchange approximation. In this so-called Born approximation, where the interaction 34 between the electron and the nucleon occurs via an exchange of one virtual photon (OPE), 35 the unpolarized e - N elastic cross section can be parameterized in terms of a nucleon 36 magnetic, G_M , and electric, G_E , form factors. These form factors describe the deviation 37 from a point-like scattering cross section, $\sigma_{\scriptscriptstyle Mott}$: 38

$$\left(\frac{d\sigma}{d\Omega}\right)_{eN \to eN} = \frac{\sigma_{Mott}}{\epsilon(1+\tau)} \left[\tau \cdot G_{M}^{2}(Q^{2}) + \epsilon \cdot G_{E}^{2}(Q^{2})\right],\tag{1}$$

where E and E' are the incident and scattered electron energies, respectively, θ is the electron scattering angle, $\tau \equiv -q^2/4M^2$, with $-q^2 \equiv Q^2 = 4EE' \sin(\theta/2)$ being the negative four-momentum transfer squared, M is the nucleon mass, and $\epsilon = [1 + 2(1 + \tau) \tan^2(\theta/2)]^{-1}$ is the longitudinal polarization of the virtual photon. We define the reduced cross section as the total cross section divided by the Mott Cross section:

$$\sigma_r \equiv \left(\frac{d\sigma}{d\Omega}\right) \cdot \frac{\epsilon(1+\tau)}{\sigma_{_{Mott}}} = \tau \cdot G_{_M}^2(Q^2) + \epsilon \cdot G_{_E}^2(Q^2) = \sigma_T + \epsilon \cdot \sigma_L, \tag{2}$$

where σ_L and σ_T are the cross sections for longitudinally and transversely polarized virtual photons, respectively.

The linear ϵ dependence of the cross section is due to the σ_L term. The ratio σ_L/σ_T is the so-called Rosenbluth slope related to G_E/G_M (in OPE), see Fig. 1. The fits of world data displayed in this figure show a strong disagreement between the G_E^p/G_M^p ratio from Rosenbluth measurements on the proton (shown as the solid line on Fig. 1) and the G_E^p/G_M^p ratio from polarization transfer measurements (shown as the blue dot-dashed line in Fig. 1).

The nucleon electromagnetic form factors can reveal a lot of information about the nucleon internal structure, as well as the quark distribution. The form factors depend only on Q²,



FIG. 1. The square root of Rosenbluth slope, corrected for kinematical factor $\sqrt{\tau}$ and μ_p , observed in elastic electron-proton scattering, adapted from Ref. [3]. The black markers show the latest Rosenbluth slope measurements from Ref. [3]. The black and red curves shows the global fit of Rosenbluth measurements at high Q²respectively with and without the data published in [3]. The blue curve shows the global fit of polarization transfer. Note: since this global fit includes mostly data in the Q² range of 1 to 8.8 (GeV/c)², the global Rosenbluth slope fit does not represent well the very low Q² of 1 (GeV/c)².

defined earlier. In the limit of large Q², perturbative QCD (pQCD) provides well-motivated 53 predictions for the Q^2 -dependence of the form factors and their ratio, which is predicted to be 54 independent of Q^2 (scaling). Studies show that pQCD validity will require a very large Q^2 of 55 the order of 100 $(\text{GeV/c})^2$ [4–6]. It was discovered at JLab, using the double polarization 56 methods, that the proton electric and magnetic form factors behave differently starting at 57 $Q^2 \approx 1 \ (GeV/c)^2$. Experimentally, the nucleon form factors can be measured using one 58 of two techniques: the polarization transfer technique and the aforementioned Rosenbluth 59 technique. The polarization method examines the polarization transfer from longitudinally 60

polarized electron to the recoiling nucleon and determine the resulting azimuthal asymmetry 61 distribution using a polarimeter. Alternatively, one can use a polarized electron beam and 62 polarized target. In the Rosenbluth method, the electric and magnetic from factors can 63 be separated by making two or more measurements with different ϵ values (*i.e.* different 64 beam energies and angles), but with same Q^2 value. The Rosenbluth technique requires an 65 accurate measurement of the cross section and suffers from large systematic uncertainties 66 arising from several factors, for instance the need for a precise determination of the scattering 67 angle. Additionally, for a measurement of the neutron form factors, accurate knowledge of 68 the neutron detector efficiency is required, which is particularly hard to achieve. These 69 uncertainties can be greatly reduced by measuring the ratio of e - n and e - p quasi-elastic 70 cross sections. 71

⁷² When comparing the values of G_E^p/G_M^p obtained from both techniques, a significant dis-⁷³ crepancy was observed (see Fig. 1). Such a discrepancy implies a potential problem in our ⁷⁴ understanding of the nucleon substructure. Many efforts were made to explain this effect, ⁷⁵ and it is believed that the inconsistency is due to the contribution of two-photon exchange ⁷⁶ (TPE) in e - N elastic scattering process [7, 8], but, as we will discuss next, this remains an ⁷⁷ open debate.

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One of the properties of TPE is its sensitivity to the lepton charge i.e. the respective 80 TPE contributions to the cross section of e^-N and e^+N are of opposite size. Based on 81 this, several experiments measured elastic cross section ratios $\sigma_{e^+p}/\sigma_{e^-p}$ ratios. Both meta 82 analysis of old elastic e^+p/e^-p data [10] and more recent measurement of $R_{2\gamma} = \sigma_{e^+p}/\sigma_{e^-p}$ 83 Q^2 up to 2 (GeV/c)² from Olympus [9] (shown on Fig 2) and CLAS [11] have not managed to 84 evidence the existence of TPE beyond their respective experimental uncertainties.¹ Higher 85 \mathbf{Q}^2 measurements with positrons and electrons on the proton have been proposed for the 86 future Jefferson Lab positron upgrade, including measurements of $R_{2\gamma}$ up to 10 (GeV/c)² on 87 the proton with CLAS12 [13], and super-Rosenbluth measurements of the proton cross sec-88

¹ While the discrepancy shown in Fig. 1 looks already quite sharp at modest Q^2 values, the global fit does note include very low Q^2 data from Mainz [12], which does not observe a significant discrepancy between Rosenbluth and polarization transfer data.



FIG. 2. Measurements of $R_{2\gamma} = \sigma_{e^+p}/\sigma_{e^-p}$ from Olympus [9] for Q²< 2 (GeV/c)², showing the absence of a significant TPE contribution in this Q² range.

tion up to 5.5 (GeV/c)² in Hall C with HMS/SHMS [14]. Such measurements will greatly
improve our understanding of the TPE contribution to the proton cross section.

While most neutron electric form factor measurements use a double polarization tech-91 nique [15, 16] or a recoil polarization technique [17], the evaluation of the TPE contribution 92 on the neutron remains important, as it may be a non-negligible correction to neutron form 93 factor measurements such as the recently recorded GMn measurements in Hall A [18] and 94 Hall B [19]. The experimental knowledge on the TPE contribution on the neutron is ex-95 tremely reduced. The only experiment attempting to measure this quantity is the nTPE 96 experiment E12-20-010 [20], which analysis is ongoing. This experiment performed a mea-97 surement of the Rosenbluth slope in e^-n at $Q^2 = 4.5 \ (\text{GeV/c})^2$. While the analysis of this 98 experiment (and especially the careful determination of the systematic uncertainties) is still 99 ongoing, we believe that the comparison of this upcoming result with the existing SBS fit the 100

¹⁰¹ upcoming polarization transfer measurement at $Q^2 = 4.5 \text{ (GeV/c)}^2$ from GEn-RP [17] Pre-¹⁰² dictions made for the electron-neutron case shown in Fig. 3, adapted from [21] shows a very ¹⁰³ modest contribution at lower Q², but growing significantly from Q² = 3 (GeV/c)² onwards. In



FIG. 3. Projected impact of TPE on G_E^n/G_M^n using LT separation, according to Ref. [21]. Blue hollow circles show old G_E^n/G_M^n polarization transfer measurements from [22]. Red solid squares show a *prediction* of this ratio with from a Rosenbluth measurement between $\epsilon = 0.2$ and $\epsilon = 0.9$. Green solid circles show a *prediction* of this ratio with from a Rosenbluth measurement between $\epsilon = 0.5$ and $\epsilon = 0.8$.

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the following we propose to measure of the neutron TPE contribution with positron-neutron to electron-neutron cross section ratios $R_{2\gamma}^n$, along with Rosenbluth separated cross sections for both positron-neutron to electron-neutron quasi-elastic scattering, at three Q² values of 3, 4.5, and 5.5 (GeV/c)². The proposed measurements will test of the predictions from [21] and provide a very valuable insight on the TPE contributions in neutron form factor measurements.

II. PHYSICS MOTIVATION

A. Form factor measurements at high Q^2

The nucleon plays the same central role in hadronic physics that the hydrogen atom does 114 in atomic physics and the deuteron in the physics of nuclei. The structure of the nucleon 115 and its specific properties, such as charge, magnetic moment, size, mass; the elastic electron 116 scattering form factors, resonances; and structure functions in DIS, are of fundamental sci-117 entific interest. Isospin is a fundamental property of the nucleon, so both the proton and 118 neutron investigations are important to do. By using data on the proton and neutron form 119 factors, the flavor structure could be explored [23]. It has already provided the most direct 120 evidence for a diquark correlation in the nucleon [24-26]. 121

Hadron structure, as seen in elastic electron scattering, in the one-photon exchange approximation, is defined by two functions of four momentum transfer square. They are: the helicity conserving Dirac form factor, F_1 , which describes the distribution of the electric charge, and the helicity non-conserving Pauli form factor, F_2 , which describes the distribution of the magnetic moment. These two form factors are the ingredients of the hadronic current. They contain information on the transverse charge distribution for an unpolarized and transversely polarized nucleon, respectively, in the infinite momentum frame [27, 28].

The Sachs form factors, G_E and G_M , the ratio of which will be extracted directly from the data, are related to F_1 and F_2 by

$$F_1 = \frac{G_E + \tau G_M}{1 + \tau} \text{ and } F_2 = \frac{G_M - G_E}{\kappa (1 + \tau)},$$
 (3)

¹³¹ where κ is the nucleon anomalous magnetic moment.

Already twenty-four years ago, an important development in QCD phenomenology has been the exploration of the generalized parton distribution (GPD) formalism [29–31], which provides relations between inclusive and exclusive observables. The nucleon elastic form factors F_1 and F_2 are given by the first moments of the GPDs

$$F_1(t) = \sum_q \int_0^1 H^q(x,\xi,t,\mu) dx \text{ and } F_2(t) = \sum_q \int_0^1 E^q(x,\xi,t,\mu) dx, \tag{4}$$

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where H^q and E^q are two of the generalized parton distributions, x is the original momentum 136 fraction of the parton x, ξ is the "skewdness" of the reaction², t is the four-momentum 137 transferred by the electron, μ is a scale parameter necessary for the evolution over Q^2 , 138 analogous to DIS parton distributions, and the sum is over all quarks and anti-quarks. 139 GPDs may be accessed through processes such as deeply virtual Compton scattering, where 140 the interaction is factorized into a hard part with the virtual photon/photon interactions 141 with an individual quark and a soft part of the residual system where the GPD information 142 is contained. 143

A fundamental nucleon feature, the spin, is related to GPDs, as shown by X. Ji [30]. The moments of GPDs can yield information, according to Ji's Angular Momentum Sum Rule, on the contribution to the nucleon spin from quarks and gluons, including both the quark spin and orbital angular momentum.

At present, experimental measurements of GPDs are still scarce. Until high Q^2 DVCS 148 data becomes available, work has been done to attempt to parameterize these GPDs, which 149 rely heavily on data from electromagnetic form factors and parton distributions from DIS as 150 constraints [32]. Data at high Q^2 for G_E^n would contribute significantly in the development 151 of these models. As we presented above, nucleon elastic form factors provide important 152 input for the modeling of GPDs. At the same time, the measured cross section of elastic 153 e - p scattering at high Q^2 is significantly larger than predicted by Born-approximation 154 calculations [33], indicating that TPE effects play a critical role in the high- Q^2 region and 155 therefore must be well understood before conclusions about GPDs can be drawn. 156 157

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B. The role of two-photon exchange in form factors

As we presented above, the form factors are important components for the study of the nucleon structure. However, the puzzle of the form factor ratio G_E/G_M at higher Q² partly blurs our understanding of the measurements. Such an observation underlines the importance of the understanding of the two-photon exchange for hadron physics.

 $^2 -x \le \xi \le x$ get integrated with the integration on x

There are two different contributions of the two photon-exchange. The first one is the 163 "soft" two-photon exchange, where one of the photons energy is very small compared to the 164 other, which is usually included in radiative correction calculations such as those of Mo and 165 Tsai [34]. This soft contribution being calculated in radiative corrections prescriptions and 166 corrected for in our cross sections, it is not the subject of our measurement. The "hard" 167 two-photon exchange, where both photons have a significant energy, and that we intent 168 to measure, is the contribution remaining after the "soft" radiative corrections have been 169 applied. The leading order contribution of the two-photon exchange to the elastic lepton-170 nucleon scattering is the interference term between the one-photon amplitude term $\mathcal{M}_{1\gamma}$ and 171 the two-photon amplitude term $\mathcal{M}_{2\gamma}$: 172

$$\sigma_{eN} \propto |\mathcal{M}_{1\gamma}|^2 \pm 2\Re e[\mathcal{M}_{1\gamma}\mathcal{M}_{2\gamma}]. \tag{5}$$

This interference term depends on the cube of the charge of the lepton involved, *i.e.* at first 173 order the sign of the two-photon exchange contribution is naively expected to flip from $e^- - N$ 174 to $e^+ - N$. This means that the deviation from 1 of the ratio of quasi-elastic cross sections 175 $R_{2\gamma}^N = e^+ - N/e^- - N$ is directly proportional to the TPE contribution. This statement 176 above does not account for the interference of lepton- hadron-bremsstrahlung which also 177 contributes to the ratio of positrons/electrons cross section. However, this contribution 178 can be calculated and corrected for using the appropriate radiative correction prescriptions 179 which do not neglect this contribution such as [34, 35]. In addition, the comparison between 180 G_E/G_M from $e^+ - N$ Rosenbluth measurements, $e^- - N$ Rosenbluth measurements, and 181 G_E/G_M from polarization transfer measurements will allow to test more effectively whether 182 the difference between the latter two (observed for the proton, to be confirmed for the 183 neutron) is due solely to the TPE. The measurement presented in this document proposes 184 to measure the ratio of positron-neutron to electron-neutron quasi-elastic cross-section $R_{2\gamma}^n$, 185 which is directly proportional to the two-photon exchange contribution: 186

$$R_{2\gamma}^n = \frac{\sigma_{e^+n}}{\sigma_{e^-n}}.$$
(6)

This simple and straightforward measurement is combined with a measurement of the Rosenbluth slope in electron- and positron-neutron scattering. Combined with the upcoming result

on electron-neutron scattering from nTPE experiment E12-20-010 under analysis and compared to the upcoming GEN and GEn-RP measurements of G_E^n with polarization techniques, will provide an independent estimation of the two-photon exchange in neutron quasi-elastic scattering.

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III. TECHNIQUE

This proposal uses the same instrumentation, simulation, and analysis development as the past GMn/nTPE experiments (E12-09-019/E12-20-010) [18, 20]. The GMn/nTPE experiments are one of several form factor experiments using the Super BigBite Spectrometer (SBS), and have run during Fall 2021 and Winter 2022.

The neutron form factors are challenging to be determine experimentally especially be-198 cause there is no free neutron target. However, since deuterium is a loosely bound system, 199 it can be viewed as the sum of a proton target and a neutron target. In fact, quasi-elastic 200 scattering from deuterium has been used to extract the neutron magnetic form factor, G_{M}^{n} , 201 at modestly high Q^2 for decades [36, 37] in single arm (e,e') experiments. In those experi-202 ments, the proton cross section needs to be subtracted by applying a single-arm quasi-elastic 203 electron-proton scattering. This "proton-subtraction" technique suffers from a number of 204 systematic uncertainties e.g. contributions from inelastic and secondary scattering processes. 205 Many years ago, L. Durand [38] proposed the so-called "ratio-method" based on the 206 measurement of both D(e, e'n) and D(e, e'p) reactions. In this method, many of the system-207 atic errors are canceled out. Several experiments [39–41] have applied the ratio-method to 208 determine the neutron magnetic form factor. 209

This measurement will record simultaneous D(e, e'n) and D(e, e'p) reaction with electron beams and positron beams. The measurement with each beam (e^{\pm}) provides the ratio R' of neutron over proton yields:

$$R'_{n/p} = \frac{N_{e,e'n}}{N_{e,e'p}} \tag{7}$$

²¹³ $R'_{n/p}$ needs to be corrected to extract the ratio of quasi-elastic scattering cross section ratio ²¹⁴ from nucleons $R_{n/p}$:

$$R_{n/p} = \frac{\sigma_{en}}{\sigma_{ep}} = f_{corr} \times R'_{n/p},\tag{8}$$

where the correction factor f_{corr} takes into account the hadron efficiencies, the radiative corrections, the absorption in path from the target to the detector, and small re-scattering correction. Measurements of $R_{n/p}$ for positron and electrons provide the positron-over-electron super-ratio ρ_{\pm} which depends directly on $R_{2\gamma}^n$ and $R_{2\gamma}^p$

$$\rho_{\pm} = \frac{\sigma_{e^+n}}{\sigma_{e^+p}} / \frac{\sigma_{e^-n}}{\sigma_{e^-p}} = \frac{R_{2\gamma}^n}{R_{2\gamma}^p} \tag{9}$$

Our measurement of the super-ratio ρ_{\pm} combined with the projected CLAS measurements of $R_{2\gamma}^p$ proposed to PAC51 [13] approved allows to straightforwardly obtain $R_{2\gamma}^n$:

$$R_{2\gamma}^n = \rho_{\pm} \times \left(R_{2\gamma}^p \right)_{Meas} \tag{10}$$

Our experiment also plans to measure $R_{n/p}$ at the same Q^2 and different beam energies 221 provides a way to access the Rosenbluth slope of quasi-elastic electron-neutron and positron-222 neutron cross section. Applying the Rosenbluth technique from the measurement of the 223 absolute e - n cross section to measure G_E^n requires a very accurate measurement of the 224 cross section and suffers from large uncertainties. Extracting the value of G_E^n from the ratio 225 of quasi-elastic yields, $R_{n/p}$ from a deuteron target allows us to overcome this issue. The 226 nTPE experiment [20] has taken elastic $e^- - n$ scattering at $Q^2 = 4.5 \ (\text{GeV/c})^2$ and two 227 beam energies to measure the Rosenbluth slope and extract (in OPE approximation) the 228 neutron electric form factor, G_{E}^{n} , at one value of momentum transfer. This new experiment 229 also proposes to perform a similar measurement with positrons at the same Q^2 and two 230 additional Q^2 values of 3 and 5.5 $(GeV/c)^2$. 231

Writing $R_{n/p}$ at two values of ϵ using $S^{n(p)} = \sigma_L^{n(p)} / \sigma_T^{n(p)}$ as:

$$R_{n/p,\ \epsilon_1} = \frac{\epsilon_1 \sigma_L^n + \sigma_T^n}{\epsilon_1 \sigma_L^p + \sigma_T^p} \qquad \qquad R_{n/p,\ \epsilon_2} = \frac{\epsilon_2 \sigma_L^n + \sigma_T^n}{\epsilon_2 \sigma_L^p + \sigma_T^p}$$

In these two equations there are two unknown variables: σ_L^n and σ_T^n . We remind here that proton and neutron measurements are made simultaneously with the same apparatus. Thanks to this, the dominant contribution to the uncertainty of the Rosenbluth slope of the reduced cross section vs. ϵ , $S^n = \sigma_L^n / \sigma_T^n$, will come from the uncertainty of S^p . The resulting equation for S^n is:

$$A = B \times \frac{1 + \epsilon_1 S^n}{1 + \epsilon_2 S^n} \approx B \times (1 + \Delta \epsilon \cdot S^n),$$

with $\Delta \epsilon = \epsilon_1 - \epsilon_2$, and where the variable $A = R_{n/p,\epsilon_1}/R_{n/p,\epsilon_2}$ will be measured with statistical precision of 0.1%. Assuming, for this estimate, equal values of Q² for two kinematics, the τ and σ_T for two kinematics are canceled out, and the variable *B* depends on the proton Rosenbluth slope S^p :

$$B = (1 + \epsilon_2 S^p) / (1 + \epsilon_1 S^p) \tag{11}$$

For electron measurements, the current knowledge of the $e^- - p$ elastic scattering cross section obtained in the single arm H(e,e')p and H(e,p)e' experiments, compiled in the latest global analysis of e - p cross section [3], will be also used for precision determination the experiment kinematics at 3, 4.5, and 5.5 (GeV/c)². For positron measurements, we may rely on the positron-proton Rosenbluth slope measured from the Super-Rosenbluth experiment proposed in Hall C at PAC51 [14].

For actual small range of ϵ and small value of the slope, $B \approx (1 - \Delta \epsilon \cdot S^p)$. We note here onwards S^n_{\pm} the Rosenbluth slope for $e^{\pm}n$. In the simplest model, the Rosenbluth slope S^n_{\pm} is a sum of the slope due to G^n_E/G^n_M and the neutron two-photon exchange contribution to the Rosenbluth slope S^{TPE} (under the hypothesis that the polarization transfer measurements aren't affected by TPE):

$$S_{\pm}^{n} = (G_{E}^{n}/G_{M}^{n})^{2}/\tau \mp S^{\text{TPE}},$$
(12)

²⁵³ From which the extraction of S^{TPE} becomes straightforward:

$$S^{\text{TPE}} = \mp (S_{\pm}^n - (G_E^n / G_M^n)^2 / \tau), \qquad (13)$$

²⁵⁴ or, combining both measurements:

$$S^{\text{TPE}} = (S_{-}^{n} - S_{+}^{n})/2.$$
(14)

This value of S^{TPE} can then be compared to the value of nTPE obtained with Eq. 10. The uncertainties for these measurements are discussed in the section dedicated to systematic uncertainties. 258

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IV. PROPOSED MEASUREMENTS AND EXPERIMENTAL SETUP

We propose to use the same experimental setup of the past E12-09-019/E12-20-010 ex-259 periments. We have three Q^2 values with two beam energy each: $Q^2 = 3.0 \ (GeV/c)^2$ at 260 3.3 GeV/1.5 pass and 4.4 GeV/2 pass), $Q^2 = 4.5 \ (GeV/c)^2$ at 4.4 GeV/2 pass and 261 $6.6~{\rm GeV}/3$ pass, and ${\rm Q}^2$ = 5.5 $({\rm GeV}/{\rm c})^2$ at 4.4 ${\rm GeV}/2$ pass and 6.6 ${\rm GeV}/3$ pass, obtaining 262 two ϵ values for each \mathbf{Q}^2 value. Each of these kinematics will be run with both unpolarized 263 positron beams and unpolarized electron beams, at the maximum intensity available for un-264 polarized positrons in Hall C, *i.e.* 1μ A. Using the same intensity for positrons and electrons 265 will minimize the uncertainties associated with the luminosity for the ratio $\rho_{\pm} = R_{n/p}^{e+}/R_{n/p}^{e-}$ 266 This will allow us to measure: 267

• the super ratio of quasi-elastic neutron/proton cross section ratios for positrons and electrons;

• the effective Rosenbluth slope for positrons and electrons.

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Table. I displays the kinematic settings of the proposed experiment.

Kinematic	e^+/e^- - I_{beam}	Q^2	Е	E^{\prime}	θ_{BB}	p'	θ_{SBS}	ϵ
	(μA)	$({\rm GeV/c})^2$	(GeV)	(GeV)	degrees	$({\rm GeV/c})$	degrees	
1+/-	$e^{+/-}$ (1.0)	3.0	3.3	1.71	42.8	2.35	29.5	0.638
2+/-	$e^{+/-}$ (1.0)	3.0	4.4	2.81	28.5	2.35	34.7	0.808
3+/-	$e^{+/-}$ (1.0)	4.5	4.4	2.00	41.9	3.20	24.7	0.600
4+/-	$e^{+/-}$ (1.0)	4.5	6.6	4.20	23.3	3.20	31.2	0.838
5+/-	$e^{+/-}$ (1.0)	5.5	4.4	1.47	54.9	3.75	18.7	0.420
6+/-	$e^{+/-}$ (1.0)	5.5	6.6	3.67	27.6	3.76	26.9	0.764

TABLE I. Kinematic settings of the proposed experiment.

This experiment will study electron scattering from a 15 cm long liquid Deuterium target held in a vacuum. The scattered electron will be detected in the BigBite spectrometer as configured for GMn/nTPE E12-09-019/E12-20-010. This configuration for the proposed experiment will be strictly the same as the configuration for GMn/nTPE and includes:

• GEM detectors for a 1% momentum resolution tracking;

• a lead glass preshower and shower for trigger, energy measurement, and PID;

• a Cherenkov detector for pion rejection;

• an hodoscope for optimize timing resolution.

The neutron arm is arranged with a dipole magnet 48D48 (SBS) and a segmented sampling 281 hadron calorimeter (HCal) to detect and reconstruct the hadron position. The SBS magnet 282 sweeping quasi-elastic protons upwards, the comparison between the expected position of the 283 reconstructed hadron allows to separate protons and neutrons as illustrated in Fig. 4. This 285 setup is identical to the GMn/nTPE experiment setup which ran succesfully in 2021/2022 286 and will be installed in Hall C. The experimental setup installed in Hall C is illustrated in 287 Fig. 5. More details on the experimental setup have been put on Appendix A. The SBS 288 spectrometer was funded by DOE with large contributions provided by the collaborating 289 institutions from USA, Italy, UK, and Canada. 290

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B. Running conditions for this experiment compared to E12-20-008

This section will compare the running conditions for the proposed experiment with the running conditions for GMn/nTPE experiment E12-20-008.

a. BigBite and SBS in Hall C GMn/nTPE was run in Hall A, which features the largest floor space/clearance. Provided the future experimental program of Hall A with the Moller [42] experiment followed up by SoLID [43], we have decided to propose this experiment in Hall C. One of the main potential issues would be the lack of space in Hall C.



FIG. 4. Distribution of difference between the position expected in HCal (from the electron information) x_{expect} and the reconstructed position in HCAL x_{HCal} , for hydrogen data (red) and deuterium data (blue) evidencing the proton (shifted upwards *i.e.* negative in transport coordinates) and neutron peaks (centered at zero).



FIG. 5. Layout of the experimental setup, including the BigBite spectrometer, the SBS magnet, and the Hadron Calorimeter (HCal) in Hall C. The HMS and SHMS do not participate to the measurement and are pushed back to their maximum angle.

The Hall C engineering team checked for us that the different setups we will require will not interfere with the HMS and SHMS once pushed back to their largest angle. Hall C being equipped with a overhead crane, we do not anticipate any additional difficulty changing settings compared to Hall A.

³⁰³ b. Beam intensity GMn/nTPE was originally planned to run at 30 μ A. Due to issues ³⁰⁴ with the GEMs explained in Appendix A and resolved since, GMn/nTPE run at a fraction ³⁰⁵ of this current, from 5 to 10 μ A. In the experiment we propose, the beam intensity will ³⁰⁶ be limited to 1 μ A by the maximum intensity for the positron beam. The trigger rates ³⁰⁷ and detector occupancies which were handled by the detectors during the GMn/nTPE data ³⁰⁸ taking at 5 to 10 μ A will be down significantly, and will therefore be essentially a non-issue.

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V. SYSTEMATIC UNCERTAINTIES

In this section the contributions to the systematic uncertainties for this experiment are listed and discussed. The uncertainties on the ratio of neutron-to-proton cross section ratios $R_{n/p}$ are discussed first. The uncertainties on the quantities of interest $R_{2\gamma}^n$ and S^n are discussed next.

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A. Systematic uncertainties on $R_{n/p}$, ρ_{\pm} , A

A majority of the potential sources of systematic uncertainties (Fermi motion, nuclear 315 corrections, accidentals, target density, etc) cancel in the ratio $R_{n/p}$, which is one of the 316 strengths of this experimental method. The remaining systematic uncertainties from the ex-317 perimental setup have been partially evaluated in the GMn/nTPE experiment. The sources 318 of systematics include radiative corrections, HCal detection efficiency, inelastic contamina-319 tion, and neutron-proton charge exchange in final state interactions (FSI). The evaluation 320 of $R_{2\gamma}^n$ also includes an uncertainty on the luminosity to normalize the electron and positron 321 data samples with respect to each other. The sources of uncertainties as well as their *prelim*-322 *inary* evaluation for each kinematic is provided in Table. II. The method to evaluate these 323 is discussed in the next paragraphs. The errors for $\Delta \rho_{\pm}/\rho_{\pm}$ are calculated as such: 325

$Q^2 \ (({\rm GeV/c})^2)$	3.0	4.5	5.5	$\delta_{cov, e+/e-}$	$\delta_{cov, \epsilon_1/\epsilon_2}$
Radiative corrections [*]	0.77	1.11	1.26	+0.80	0.0
Inelastic contamination	0.33	0.75	0.84	+0.5	0.0
Nucleon detection efficiency [*]	0.7	0.7	0.7	+0.95	+0.5
Nucleon charge exchange in FSI	0.04	0.01	0.02	+0.95	0.0
Selection stability	0.16	0.15	0.40	+1.00	0.0
$\Delta R_{n/p}$	1.10	1.52	1.72	-	-
$\Delta \rho_{\pm} / \rho_{\pm}$	0.44	0.74	0.83	-	-
$\Delta A/A$	1.40	2.03	2.32	_	_

TABLE II. Estimated^{*} and preliminary contributions to the systematic error on $R_{n/p} = \sigma_{en}/\sigma_{ep}$ from the GMN analysis (in percent). The total systematic errors on $R_{n/p}$ is the quadratic sum of all other errors. We made the assumption that the systematics for the two beam energies for the same Q² are of similar size. $\delta_{cov, e+/e-}$ and $\delta_{cov, \epsilon_1/\epsilon_2}$ are the assumed correlation between the uncertainties for the e^+ and e^- measurements and the ϵ_1 and ϵ_2 measurements respectively. For the calculation of $\Delta \rho_{\pm}/\rho_{\pm}$ and $\Delta A/A$, we added all uncertainties accounting for the assumed correlations as described in equation 15.

$$\frac{\Delta\rho_{\pm}}{\rho_{\pm}} = \left(\sum_{corr} \left(\left.\frac{\Delta R_{n/p}}{R_{n/p}}\right|_{corr}^{e^+}\right)^2 + \left(\left.\frac{\Delta R_{n/p}}{R_{n/p}}\right|_{corr}^{e^-}\right)^2 + 2\left.\frac{\Delta R_{n/p}}{R_{n/p}}\right|_{corr}^{e^+} \left.\frac{\Delta R_{n/p}}{R_{n/p}}\right|_{corr}^{e^-} \left(1 - \delta_{cov, e^+/e^-}\right)\right)^{1/2}$$
(15)

where "corr" is the considered correction (RC, inelastic, etc), and $\delta_{cov, e^+/e^-}$ is the correlation factor listed in Table II. $\Delta A/A$ would write similarly to Eq. 15 by substituting ρ_{\pm} with Aand $\delta_{cov, e^+/e^-}$ with $\delta_{cov, \epsilon_1/\epsilon_2}$. We discuss and justify the values of $\delta_{cov, e^+/e^-}$ and $\delta_{cov, \epsilon_1/\epsilon_2}$ for each of the corrections in their respective paragraphs.

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a. Radiative corrections For the GMn/nTPE analysis, the radiative corrections have been included in the Monte Carlo samples generated with SIMC, which uses the radiative calculations by Mo and Tsai [34] with peaking approximation. This generator provides the option to include only the electron radiative tails for both D(e, e'p) and D(e, e'n) events, or to include electron radiative tails and proton radiative tails for D(e, e'p). The first case treats both proton and neutron as chargeless point particles, which represents an extreme case. The second case is more realistic, only treating the neutron as chargeless, but also neglects its structure. The systematic uncertainty is evaluated as the difference of $R_{n/p}$ obtained following each of these two prescriptions for D(e, e'p) and D(e, e'n) Monte Carlo samples.

As mentioned above, the radiative correction prescription implemented for SIMC applies 340 the peaking approximation which essentially eliminates the contribution from the lepton-341 hadron bremsstrahlung interference. This can be considered somewhat satisfactory for the 342 GMn measurement and to a lesser extent for the nTPE measurement. However, if not 343 corrected for, the lepton-hadron bremsstrahlung interference becomes non-negligible in the 344 $R_{2\gamma}$ ratio as other contributions cancel out. Fortunately, there are many other prescriptions 345 available to correct for this effect, including Mo and Tsai without the peaking approximation, 346 other prescriptions [35, 44]. While we quote and use the preliminary radiative corrections 347 systematic uncertainty from the GMn analysis, we plan to extract Rn/p, $R_{2\gamma}^n$ and S^{TPE} with 348 all models quoted above for our analysis. Combining the values of those quantities obtained 349 with all radiative corrections prescriptions may reduce our systematic uncertainties by up to 350 a factor two. The values quoted in Table II are the preliminary uncertainty extracted from 351 the GMn/nTPE analysis divided by a factor three to account for the margin of progress that 352 we potentially have. 353

Since most of the contributions from the radiative corrections cancel in the ρ_{\pm} ratio, with the exception of the interference between lepton and hadron bremsstrahlung, we may therefore consider a correlation $\delta^{RC}_{cov, e^+/e^-}$ of 80% for the contribution to the radiative corrections. In the *A* ratio, since the incident and outgoing electron have different energies, the radiative corrections may not be correlated at all between each other. Therefore we set the correlation $\delta^{RC}_{cov, \epsilon_1/\epsilon_2}$ to zero.

³⁶⁰ b. Inelastic contamination The distribution of Monte Carlo generated D(e, e'p) and ³⁶¹ D(e, e'n) samples distributions in Δx are normalized to the LD2 data sample distribution

in Δx , together with a distribution to model the inelastic contamination. This distribution 362 can be an analytic function which parameters are fitted together with the normalization of 363 the Monte Carlo samples to the LD2 data sample. Three different analytic functions have 364 been considered: a two-order polynomial, a three-order polynomial, and a gaussian. The 365 background function can also be a distribution of Δx of the same LD2 data sample with an 366 "anti-selection" applied on Δy (all other selection parameters being the same as for quasi-367 elastic selection) The last function combines an inelastic Monte Carlo sample generated using 368 the Christy-Bosted parametrization [45], combined with a distribution of Δx of the same 369 LD2 data sample with an anti-selection applied on Δt the time difference between HCal and 370 BigBite. This parametrization, shown in 6 provides the best adjustment. The systematic 371 uncertainty is provided by the standard deviation between all inelastic contamination func-372 tions. 373





FIG. 6. Left: Global fit of Monte Carlo D(e, e'p) (blue), D(e, e'n) (green) and inelastic D(e, e'X) inelastic Monte Carlo sample function, adjusted to the data (black markers). Right: LD2 data distribution in W^2 (blue), compared with D(e, e'p) and D(e, e'n) Monte Carlo samples (black) and D(e, e'X) inelastic Monte Carlo sample (red).

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therefore, we cannot assume a perfect cancellation of errors in the ρ_{\pm} ratio. Nonetheless, correlation $\delta_{cov, e^+/e^-}^{Inel}$ of 50% for the contribution to the inelastic contamination in this ratio should be conservative. However, in the A ratio, since many parameters are different (beam energy, active HCal area) we anticipate a much smaller correlation $\delta_{cov, \epsilon_1/\epsilon_2}^{Inel}$ which we set to zero.

c. Nucleon detection efficiency The understanding of the HCal detection efficiency is one of the key parameters for this experiment. A full discussion of the HCal detection efficiency analysis is provided in Appendix B.

To summarize, there are several contributions to the neutron detection efficiency systematics. 385 The first contribution comes from the HCal non-uniformity. It is estimated extracting $R_{n/p}$ 386 with and without correcting for the non-uniformity (as described in $4 \, d$), which bring a cor-387 rection of 0.2 to 0.5%. The second contribution in the st the uncertainty on the uncertainty 388 of proton detection efficiency due to inelastic contamination. This effect becomes significant 389 in the GMn analysis at higher Q^2 of 7.5 $(GeV/c)^2$ and beyond. At the Q^2 we are considering, 390 we estimate that this effect accounts for less that 0.2%. The third contribution comes from 391 the gain variation of HCal. This gain variation can be kept in control by regularly taking 392 LH_2 data to evaluate the relative response of HCal over time. The analysis from GMn/nTPE393 showed a very modest gain variation over the span of the data taking time. We also provision 394 to take LH2 data with different SBS magnet settings to cover all the HCal coverage. We 395 provision to take about one hour of LH_2 data for every three hours of LD_2 data on average. 396 The last contribution comes from the absence of data sets to obtain direct neutron detection 397 efficiency for HCal. This problem can be solved for the proposed experiment by requesting 398 additional beamtime to perform a neutron detection efficiency measurement described in the 399 next paragraph. 400

In the ρ_{\pm} ratio, the kinematics are the exact same from one beam species to the other, therefore the HCal area involved in the measurement should be the same and the beam efficiency should in theory cancel entirely. We set the correlation $\delta_{cov, e^+/e^-}^{HCal}$ to 95% to account for small gain variations. In the A ratio, the HCal area involved in the detection is quite different from one kinematic to the other. Nevertheless, in the nTPE/E12-20-010, we observed a clear correlation of the HCal response between both kinematics. While we have yet to determine rigorously the actual correlation coefficient, we estimate that a correlation ⁴⁰⁸ factor of 0.5 should be reasonable and achievable.

Neutron detection efficiency measurement Along with this new experiment, we will have a great opportunity to measure the HCal neutron detection efficiency to validate the neutron efficiency estimated by Monte Carlo. The elected channel for this measurement is $\gamma p \rightarrow \pi^+ n$. The LH2 target will be used, with 6% radiation length copper radiator mounted upstream to increase real photon generation. This will be combined with a 5 μ A intensity electron beam. The BigBite magnet polarity will be reversed to select π^+ and deflect electrons. This measurement can be performed with the "3-" kinematic setting *i.e.*



FIG. 7. Projected footprint and counting rates of $\gamma p \to \pi^+$ (BigBite)n(HCal) for 16 hours of data taking at 5 μ A on 15 cm LH₂ with 6% Cu radiator upstream, with the "3-" kinematic setting (Q²= 4.5 (GeV/c)², low energy/2pass).

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⁴¹⁸ $Q^2 = 4.5 \ (\text{GeV/c})^2$, low energy/2pass. Strict kinematic requirements on the pion and real ⁴¹⁹ photon reconstructed energy will be applied to select the $\gamma p \to \pi^+ n$. The selected kinematic ⁴²⁰ allows to cover a sizeable fraction of the HCal surface, as shown on Fig 7. This data will ⁴²¹ used for the validation of the neutron detection efficiency with Monte Carlo, therefore it is ⁴²² not required to cover the entirity the HCal surface. Our simulation of $\gamma p \to \pi^+ n$ in the ⁴²³ BigBite+SBS indicates that the rates of *clean* $\gamma p \to \pi^+ n$ is over 5000 per hour. A data ⁴²⁴ taking of 16 hours (two shifts) at this setting will provide 80 thousands $\gamma p \to \pi^+ n$ events to estimate our calorimeter response to the neutron with a precision better than 0.4%. This measurement combined our existing and upcoming studies shall allow us to achieve an uncertainty on the HCal detection efficiency of the order of better than 0.7%. We do request an additional 16 hours of beam time with 5 μ A on liquid hydrogen target combined with a 6% radiation length copper plate. This request is included in Table VII.

d. Nucleon charge exchange in FSI The symmetry of the deuterium nucleus means that the respective probabilities of charge exchange from proton-neutron and neutron-proton in FSI are expected to be mostly equal, and therefore the systematic uncertainty is expected to mostly cancel. The uncertainty on proton/neutron charge exchange had been provided to us by M. Sargsian [46]. According to his calculations, the effect should contribute to the cross proton and neutron section by less than 5%, and the uncertainty is better than 0.1%.

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B. Systematic uncertainties on $R_{2\gamma}^n$

$Q^2 \; (({\rm GeV/c})^2)$	3.0	4.5	5.5
$\Delta \rho_{\pm}/\rho_{\pm} \ (\text{stat})$	0.28	0.25	0.58
$\Delta \rho_{\pm}/\rho_{\pm} \text{ (syst)}$	0.44	0.74	0.83
$\Delta R^p_{2\gamma}/R^p_{2\gamma} \ [13]$	0.78	0.42	0.79
$\Delta R_{2\gamma}^n/R_{2\gamma}^n$ (syst)	0.93	0.89	1.28

438 The systematic uncertainties contributing $R_{2\gamma}^n$ are compiled on Table. III. This table also

TABLE III. Preliminary contributions to the systematic error on $R_{2\gamma}^n = \sigma_{e^+n}/\sigma_{e^-n}$ (in percent). The total systematic errors on $R_{2\gamma}^n$ is the quadratic sum of all other errors.

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⁴⁴¹ provides the statistical accuracy for ρ_{\pm} . The calculations of the uncertainties on ρ_{\pm} have been ⁴⁴² explained in Sec. V A and copied from Table II. In both this measurement and the Rosenbluth ⁴⁴³ measurement, the luminosity does not directly play a role, as for each kinematic we measure a ratio of cross section which does not depend on the total integrated luminosity. The uncertainties on $R_{2\gamma}^p$ have been taken from the estimations from [13]. All these systematics have been added quadratically.

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C. Systematic uncertainties on S^n

Table. IV lists the estimated contributions to systematic errors on the Rosenbluth slope measurement. The values and uncertainties for S^p come from the uncertainties of the data fits

${\rm Q}^2(({\rm GeV/c})^2)$	$3.0 \ (e^-)$	$3.0 \ (e^+)$	$4.5 \ (e^-)$	$4.5 \ (e^+)$	$5.5 \ (e^-)$	$5.5 \ (e^+)$
$\Delta A/A \ (\text{stat}, \ \%)$	0.32	0.32	0.40	0.40	0.58	0.58
$\Delta A/A \text{ (syst, \%)}$	1.40	1.40	2.03	2.03	2.32	2.32
S^{p} [3, 14]	0.1056	-0.0267	0.0616	-0.0608	0.0478	-0.0773
$\Delta S^p \ [3, 14]$	0.0160	0.0114	0.0165	0.0164	0.0170	0.0254
ΔS^n	0.100	0.096	0.103	0.103	0.087	0.094

TABLE IV. Estimated contributions to the statistical and systematic uncertainties on the measured Rosenbluth slopes for this experiment. The calculations of the total uncertainty is explained in the text.

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from the latest Rosenbluth publication from Christy *et al.* [3] for e^- and from the uncertainty estimations from [14] for e^+ . The calculations of the uncertainties on $A = R_{n/p}^{\epsilon_1}/R_{n/p}^{\epsilon_2}$ have been explained in Sec. VA and copied from Table II. The error on ΔS^n writes:

$$\Delta S^n = 1/\Delta \epsilon (\Delta A/A + \Delta B/B^2 + ADSp/(1 - DeSp)2), \tag{16}$$

with $B = (1 + \epsilon_2 S^p)/(1 + \epsilon_1 S^p)$ and therefore $\Delta B = \Delta S^p \Delta \epsilon/(1 + \epsilon_1 S^p)$.

VI. PROJECTED RESULTS

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A. Quasi-elastic counting rates

The signals for this experiment have been generated using the G4SBS elastic/quasi-elastic generator. We generated a reasonably large sample of quasi-elastic events N_{Gen} for each kinematics, within a solid angle $\Delta\Omega_{Gen}$ that was larger than the detector acceptance. To

Point	Beam/	Q^2	E_{beam}	I_{beam}	n rates	p rates	beam time	n counts	p counts
	Target	$({\rm GeV/c})^2$	(GeV)	(μA)	(Hz)	(Hz)	(h)	(×1000)	(×1000)
1+/-	$e^{+/-}/\text{LD2}$	3.0	3.3	1.0	2.55	7.44	24×2	220	643
1+/-	$e^{+/-}/LH2$	3.0	3.3	1.0	-	7.44	12×2	-	322
2+/-	$e^{+/-}/\text{LD2}$	3.0	4.4	1.0	4.00	11.67	16×2	230	672
2+/-	$e^{+/-}/LH2$	3.0	4.4	1.0	-	11.67	16×2	-	672
3+/-	$e^{+/-}/\text{LD2}$	4.5	4.4	1.0	0.49	1.54	96×2	169	532
3+/-	$e^{+/-}/LH2$	4.5	4.4	1.0	-	1.54	32×2	-	177
4+/-	$e^{+/-}/\text{LD2}$	4.5	6.6	1.0	0.94	3.11	48×2	162	537
4+/-	$e^{+/-}/LH2$	4.5	6.6	1.0	-	3.11	16×2	-	89
5+/-	$e^{+/-}/\text{LD2}$	5.5	4.4	1.0	0.186	0.541	120×2	80	234
5+/-	$e^{+/-}/LH2$	5.5	4.4	1.0	-	0.541	40×2	-	78
6+/-	$e^{+/-}/\text{LD2}$	5.5	6.6	1.0	0.576	1.980	36×2	75	256
6+/-	$e^{+/-}/LH2$	5.5	6.6	1.0	-	1.980	12×2	-	86

TABLE V. Quasi-elastic e-n and e-p counting rates, for each kinematic, proposed beam-on-target time and total statistics.

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evaluate the detector solid angle, we define simple criteria that each event has to pass, definedas follows:

• require a primary track, going through all 5 GEM layers (electron arm);

• require non-zero energy deposit in both the preshower and shower (electron arm);

• require non-zero energy deposit in HCal (hadron arm).

The quasi-elastic data rates and statistics are compiled for both kinematics in Table. V, along with the respective beam currents, beam/targets, and running times. This table includes the measurements on LH2 meant for HCal gain and systematic studies. The background/trigger rates on top of which this signal will sit is discussed for the different kinematics in Appendix C.

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B. Projected measurements

The projected results including statistics and systematic uncertainties for $R_{2\gamma}^n$ are presented for all kinematics on Fig. 8. The projected expected Rosenbluth slope measurement



FIG. 8. Projected values of $R_{2\gamma}^n$ plotted as a function of Q² for different beam energies: 3.3GeV (blue), 4.4 GeV (red), 6.6 GeV (green), including statistics and systematic uncertainties. The inner error bars is statistics only. The larger error bar shows the total of all systematics.

⁴⁷⁸ is presented on Fig. 9. This projection makes the assumption that the discrepancy be-⁴⁷⁹ tween the Rosenbluth slope of unpolarized measurements and polarization transfer measure⁴⁸⁰ ments is uniquely due to two-photon exchange. The *projected* Rosenbluth results (*including*



FIG. 9. Projected values of $\mu_n G_E^n/G_M^n$ from our proposed e^+n (cyan bullets) and e^-n (brown bullets) Rosenbluth slope measurements, along with the *projection* of nTPE E12-20-010 (brown square - under analysis). Shown with this is the projection of GEN-RP projection [17] (blue triangle - under analysis) and the *projection* of GEN-II [16] (red bullets - under analysis). Other G_E^n measurements with polarization are shown with black bullets. The solid black curve shows the latest global form factor fit from [47]. The other curves are selected models for form factors, detailed in the text.

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⁴⁸³ nTPE / E12-20-010, under analysis) are based on the estimation of the ratio $\mu_n G_E^n / G_M^n$ at ⁴⁸⁴ Q²=3 and 4.5 (GeV/c)² from the 2018 global fit from Ye *et al.* [47], and corrected by the ⁴⁸⁵ estimation of the two-photon exchange from [21]. Theoretical curves shown are the calcula-⁴⁸⁶ tions of Ref. [48] (Purple dot-dashed), Ref. [49] (Magenta dot-dashed), the GPD-based model ⁴⁸⁷ from Ref. [50] (Blue dashed), Ref. [51] (Green dot-dashed), Ref. [52] (Red dot-dashed), and ⁴⁸⁸ Ref. [53] (Black dot-dashed).

VII. BEAM TIME REQUEST

This experiment will take place in Hall C utilizing the BigBite spectrometer to detect electrons scattered off the liquid deuterium target, and HCal calorimeter to detect the recoiling neutron and proton. The set of instrumentation for the proposed measurement is identical to the one used in the past GMN/NTPE experiment. We provide a beam estimate our time to measure the ratio of quasi-elastic positron-neutron over quasi-elastic electronproton cross sections, as well as the Rosenbluth slopes on quasi-elastic positron-neutron and electron-neutron at $Q^2 = 3.0 (\text{GeV/c})^2$, 4.5 (GeV/c)², and 5.5 (GeV/c)².

We plan to record a total of 468 hours of data with positron beam at $I_{beam} = 1 \mu A$, including 497 340 hours on liquid deuterium (LD2) of length $l_{tgt} = 15$ cm and density $d_{tgt} = 0.169$ g.cm⁻³. 498 The other 128 hours of positron beam will be taken on liquid hydrogen (LH2) of length 499 $l_{tqt} = 15$ cm and density $d_{tqt} = 0.071$ g.cm⁻³ for calibrations and systematic studies. We 500 also plan to take 484 hours of data with electron beam total, including 340 hours on LD2 at 501 $I_{beam} = 1 \ \mu A, 112$ hours on LH2 at $I_{beam} = 1 \ \mu A, 16$ hours of electrons at $I_{beam} = 5 \ \mu A$ 502 on LH2 combined with a 6% radiation length copper radiator for our neutron detection 503 efficiency measurement, and 16 hours at $I_{beam} = 10 \ \mu A$ on optics target for calibration. 504 In addition to the beam time, we will also require 16 hours PAC time (two day shifts) 505 between each experimental configuration. This duration was the duration achieved during 506 GMn/nTPE, which required a grand total of seven configuration changes. Each configu-507 ration change includes the SBS magnet and the hadronic calorimeter (HCal) angle change 508 and the BigBite spectrometer angle and distance change, and also requires a survey of HCal 509 and the SBS magnet. Two of those configuration changes will also require a pass change, 510 which can be done during the magnet reconfiguration. For each kinematic we also require a 511 reconfiguration of the accelerator to go from electrons to positrons. We are working under 512 the assumption that this configuration change can be made in 24 hours, which remains to be 513 confirmed. Table. VII displays a tentative run plan for this experiment. The kinematics of 514 our measurements emphasize the same Q^2 range where TPE in e - p elastic scattering was 515 observed to dominate in Rosenbluth slope. Measuring at this high momentum transfers will 516

⁵¹⁷ provide unique input for testing TPE calculations [21].

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Kin	e^+ or e^-	E_{Beam} (pass)	$I_{\rm Beam}$	Q^2	θ_{BB} / θ_{SBS}	target	PAC Time
		(GeV)	μA	$({\rm GeV/c})^2$	(degrees)		(hours)
Optics	e^-	3.3 (1.5)	10.0	3.0	42.8/29.5	C-foil	16
1-	e^-	3.3(1.5)	1.0	3.0	42.8/29.5	LD2/LH2	24/12
Reconfiguration to positrons							24^{\dagger}
1+	e^+	$3.3~(3^*)$	1.0	3.0	42.8/29.5	LD2/LH2	24/12
	Pass	s change $+$ BE	B/SBS	magnet co	nfiguration c	hange	16
2+	e^+	4.4 (2)	1.0	3.0	28.5/34.7	LD2/LH2	16/16
		Recor	nfigura	tion to ele	ctrons		24^{\dagger}
2-	e^-	4.4(2)	1.0	3.0	28.5/34.7	LD2/LH2	16/16
		BB/SBS n	nagnet	configurat	ion change		16
3-	e^-	4.4(2)	1.0	4.5	41.9/24.7	LD2/LH2	96/16
NDE	e^-	4.4(2)	1.0	4.5	41.9/24.7	LH2+6% Cu Rad	16
		Recor	nfigura	tion to pos	sitrons		24^{\dagger}
3+	e^+	4.4(2)	1.0	4.5	41.9/24.7	LD2/LH2	96/32
BB/SBS magnet configuration change							16
5+	e^+	4.4(2)	1.0	5.5	54.9/18.7	LD2/LD2	120/40
Reconfiguration to electrons							24^{\dagger}
5-	e^-	4.4(2)	1.0	5.5	54.9/18.7	LD2/LH2	120/40
	Pass	s change $+$ BE	B/SBS	magnet co	nfiguration c	hange	16
4-	e^-	6.6(3)	1.0	4.5	23.3/31.2	LD2/LH2	48/16
Reconfiguration to positrons						24^{\dagger}	
4+	e^+	6.6(3)	1.0	4.5	23.3/31.2	LD2/LH2	48/16
BB/SBS magnet configuration change						16	
6+	e^+	6.6(3)	1.0	5.5	27.6/26.9	LD2/LH2	36/12
Reconfiguration to electrons							24^{\dagger}
6-	e^{-}	6.6(3)	1.0	5.5	27.6/26.9	LD2/LH2	36/12
Total beam						952	
Total	time req	uest					1176

TABLE VI. Tentative run plan for this experiment, including configuration changes. $^{\dagger}:$ TBC

Appendix A: Detailed Description of the Experimental Setup

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1. Parameters of the SBS

The 48D48 magnet from Brookhaven was acquired as part of the Super Bigbite project and will be available for this experiment. It consists of a large dipole magnet which provides a field integral of about 1.6 T \cdot m, allowing for quasielastic protons to be sufficiently deflected to allow clear differentiation from neutrons. The active field volume has an opening of 46× 25 vertical × horizontal), matching the aspect ratio of the neutron arm, and a depth of 48 cm.

The placement of this magnet will be 1.6 m away from the target, which would normally interfere with the beamline. To accommodate this, modifications were made to the iron yoke such that the beamline will pass through the magnet yoke area.

The field configuration will be such that positively charged particles will be deflected 607 upwards away from the hall floor. During the data taking of E12-20-010, we evaluated 608 the optimal SBS field to be 1.12 Tesla-m (which is 70% of the maximum SBS field). For 609 this setting, protons of momentum 3.2 GeV/c are deflected 72 mrad, which translates to 610 a displacement of 0.8 m on HCal, as illustrated on Fig. 4 in the main text. The presence 611 of the magnet also works to sweep low energy charged particles from the target away from 612 the neutron arm. Particles of momentum less than 1.3 GeV/c will be entirely swept outside 613 of the neutron arm acceptance. This greatly reduces the amount of charged low energy 614 background. 615

616

2. The BigBite Spectrometer

Scattered electrons will be detected in the BigBite spectrometer. The spectrometer consists of a single dipole magnet (with magnetic field approximately 0.9 T) and a detection system, see Fig. 10, composed of GEM detectors for tracking, a calorimeter for trigger and energy measurement, a timing hodoscope for timing, and a Cherenkov detector for particle identification. The detector package we plan to use for the new experiment is the exact same we have been using for the GMn/nTPE experiments in 2021/2022. We provide details on these detectors in Appendix A.



FIG. 10. The BigBite spectrometer with the upgraded detector stack.

a. GEM Chambers

To perform the tracking of charged particles under the high rates anticipated for this 627 experiment, the drift chambers were replaced with gas electron multiplier (GEM) detectors. 628 These detectors have proven to be capable of operating under luminosities of 25 kHz/mm^2 for 629 the COMPASS experiment at CERN. During the data taking of SBS experiments, the spatial 630 resolution of each of these chambers has been observed to be about 100 μ m in relatively high 631 background conditions, with their efficiencies being above 90%, as shown on Fig 11. There 633 will be two sets of GEMs placed on each side of the GRINCH Cherenkov detector. The 634 set of GEMs in front of the GRINCH is composed of four layers of GEMs. All four layers 635 were built by the SBS collaborators from UVA.³ They are composed of a single module 636

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 $^{^3}$ Originally two layers of three 40 $\,\times\,$ 50 cm^2 layers built by the SBS collaborators from INFN were installed.

However, issues in their construction meant that they had to be replaced during the GMn experiment.



FIG. 11. BigBite GEM efficiency profile for one of the GEM modules (left) and residuals (right).

measuring 40 × 150 cm², the long dimension again being vertical and along the dispersive direction. The readout of these modules are oriented in the u/v direction *i.e.* ± 30 degrees with respect to the horizontal direction. The set of GEMs behind the GRINCH has also been been built by the SBS collaborators from UVA. It is composed of a single layer composed of four modules measuring 50 × 60 cm², such that the layer covers 60 × 200 cm² (the long dimension again being along the dispersive direction). The readout of these modules are all oriented in the x/y direction.

The background levels in the GEMs have been evaluated, with the help of the G4SBS 644 simulation package ([54] and Sec. 0 f) for the G_M^n experimental readiness review. Those 645 evaluations have been compared with the data taken during GMn/nTPE. Fig. 12 shows the 647 comparison between BigBite GEM occupancies from the GMn/nTPE recorded data and the 648 Monte Carlo simulation, at several beam intensities of 3 μ A and 30 μ A. At low intensity of 649 $3 \,\mu\text{A}$ which is three times the intensity we plan to run, the MC occupancies are in reasonable 650 agreement with the data, and does not represent any challenge. At high intensity, an issue 651 of configuration of the GEM power supply induced a loss of gain correlated with the beam 652 intensity. This issue is illustrated in Fig. 13, which shows the response of the GEMs with 653 different types of power supplies. During GMn/nTPE, the BigBite GEMs were setup with 654



FIG. 12. Comparison between BigBite GEM occupancies from GMn/nTPE data (left plots) and Monte Carlo simulation (right plots), for beam intensity of 3 μ A.

the power supply shown by the grey curve. Therefore, their gain/efficiency was dramaticallyreduced at higher currents.

b. Shower/Preshower

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The electromagnetic calorimeter configuration consists of two planes of lead glass blocks which we call the preshower and shower. The preshower, located about 80 cm behind the first GEM chamber, consists of a 2×26 plane of $37 \text{ cm} \times 9$ cm blocks. The shower, about 1 m behind the first GEM chamber, consists of an 7×27 array of 8.5 cm \times 8.5 cm blocks. Sums over these blocks form the physics event trigger for the experiment.

⁶⁶⁴ The preshower signal can be used to provide an additional method of pion rejection.



FIG. 13. Comparison of GEM detector setup with different types of power supplies to different beam intensities. The "excess current draw" is a proxy for the detector effective gain. During GMn/nTPE, the BigBite GEMs were setup with the power supply shown by the grey curve.

With sufficient calibration, a pion rejection factor of 1:50 can be achieved by vetoing events with low pre-shower signals. The relative energy resolution for the detector compared to the momentum, shown on Fig. 14 is about $\sigma_{\delta E/p} = 7\%$.



FIG. 14. BigBite calorimeter energy resolution.

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c. Timing hodoscope

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The BigBite timing hodoscope has been built by the SBS collaborators from Glasgow to 671 replace the BigBite scintillator plane and used by all the SBS experiments using BigBite, 672 including GMn/nTPE. It is composed of 90 bars stacked in a plane, each with dimensions 673 1 in. \times 1 in. \times 60 cm. The paddle stack will be oriented such that the long dimension of the 674 bars is horizontal *i.e.* perpendicular to the dispersive direction. Signals from the PMTs are 675 processed by NINO front-end cards which, when the PMT pulse crosses the NINO threshold, 676 will produce a digital signal to be read out by CAEN 1190 TDCs which record a leading 677 time and a trailing time. Each of these elements are read out by a PMT on each side, 678 which provides measurement redundancy. This plane is primarily used to provide a signal 679 for nucleon time of flight reconstruction. The analysis of this detector has shown a time 680 resolution of the order of 500 ps, as shown in Fig 15. 681



FIG. 15. BigBite hodoscope time from which RF time is subtracted, exhibiting the beam bunch structure. A single beam "bunch" is resolved within 500 ps.

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d. GRINCH cherenkov detector

⁶⁶⁵ The main purpose of the GRINCH is to provide additional particle identification for offline ⁶⁶⁶ pion rejection. The GRINCH consists of a tank with a maximum depth of 88.9 cm, with ⁶⁸⁷ 4 cylindrical mirrors focusing the cherenkov light directly onto a 510 PMT array (60 lines ⁶⁸⁸ of PMTs, with lines of 9 PMTs alternating with lines of 8 PMTs) placed away from the ⁶⁸⁹ beam. The radiation gas is C_4F_8 , which is an acceptable compromise between light yield ⁶⁹⁰ for electrons and operating cost. With $n - 1 = 1.35 \times 10^{-3}$, the π threshold is only about ⁶⁹¹ 2.7 GeV, so the additional pion rejection will be most effective below this threshold.

Similar to the timing hodoscope, the signals from the GRINCH PMTs pulses are processed by NINO front-end cards which, when the PMT pulse crosses the NINO threshold, will produce a digital signal to be readout by VETROC TDCs, which for each PMT hit will record a leading time and a trailing time. The analog signal will not be recorded however, which means that for each PMT hit, the information of the number of photoelectrons is not directly available (although it can in theory be deduced from the time over threshold).

All of this implies that the electron selection relies on the number of GRINCH PMT firing, instead of relying on the signal amplitude. The position of the PMTs firing can be correlated with the position of the track, as illustrated on Fig. 16 to enhance selection and particle identification.

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3. Hadron Calorimeter (HCal)

The Hadron Calorimeter (HCal) has been designed specifically to measure the recoil nu-704 cleon for the SBS experiments. Specifically for this experiment (and for G_M^n), HCal combined 705 with the SBS (48D48) magnet provides identification of the recoil nucleon, as well as ad-706 ditional kinematic constraint and possibly timing information on the measured interaction. 707 Nucleon identification is illustrated on Fig. 4. This figure shows the difference between the 708 expected nucleon position in HCal x_{expect} (obtained from the electron information) and the 709 reconstructed HCal cluster position x_{HCal} in HCal, for protons and neutrons. The proton 710 distribution is being shifted upwards by about 0.8 m compared to the neutron. 711



FIG. 16. Correlation between position of GRINCH PMT hits (y-axis) and track position projected at the GRINCH (x-axis). Please note the two "side bands" that corresponds to the side mirrors which deflect the Cherenkov light in a slightly different direction and change the correlation.

The HCal (a CAD model of which is shown in Fig. 17) is composed of 288 modules arranged in an array of 12×24 . A 3/4 – inchsteel plate is installed just upstream of HCAL,



FIG. 17. CAD representation of HCal (right) with the SBS magnet (left) which serves two purposes:

• initiate the hadronic shower to optimize the calorimeter response;

• shield the modules from a fraction of the low energy secondaries;

Each of these modules measures $6 \times 6 \text{ in}^2$ section, for 3 ft length. They are composed of alternating tiles of scintillators and iron around a central light guide which collects the light generated in the scintillators by the hadronic shower, and guides it to the PMT at the end of the block. Cosmic tests have determined that the average light yield for the HCal modules is around 5 photoelectrons per MeV deposited in the scintillator tiles.

The PMTs are read out with FADC250 which sample the PMT signal every 4 ns and allow to reconstruct the PMT pulse shape, and hence its timing. They are also read out by TDCs which provide additional timing information. Thanks to this, the timing resolution can be about 1 ns. The energy resolution is intrinsically broad due mostly to the small fraction of energy from the hadronic shower actually measured by the scintillator tiles. A thorough discussion on the HCal efficiency is provided in Appendix B.

4. Potential hazards during the installation and operation of SBS and Bigbite

⁷³¹ The potential hazards of the operation of BigBite and Super BigBite include:

- the interactions between the magnetic fields of BigBite and Super Bigbite;
- the operations of high voltage for detectors;
- the use of high pressure gas bottles for certain detectors;
- working at heights for the installation and maintenance of the detectors.

These hazards have already been mitigated during the running of the GMn/nTPE experiments E12-09-018/E12-20-010. Nevertheless, we will expose the potential hazards and their mitigation methods in the following.

a. Bigbite and SBS magnetic fields The Bigbite and SBS magnets are large devices
generating magnetic fields of the order of one Tesla, and placed at distances of the order of
5 m, depending on the setting. This induces colossal forces that, if unmitigated, may induce
magnets movement and damage equipment. To counteract this, several measures have been

⁷⁴³ implemented during GMn/nTPE: the assessment of the interaction forces between the two ⁷⁴⁴ magnets; the reduction of the number of coils of SBS to lower its magnetic field intensity ⁷⁴⁵ and therefore the magnetic forces; and the construction of supports and struts with sufficient ⁷⁴⁶ strength to hold each of the magnets in place and prevent their movement. Would this ⁷⁴⁷ experiment come to run, the procedures described above will be implemented again.

⁷⁴⁸ b. Detectors High voltages All operating detectors requires high voltage to operate. ⁷⁴⁹ Those high voltages are conveyed through SHV cables with the appropriate insulation. The ⁷⁵⁰ installation of such cables will be performed by qualified personnel of staff, users, and stu-⁷⁵¹ dents with the appropriate electrical training *i.e.* SAF603N. This installation will be made ⁷⁵² while the high voltage power supplies being turned off and unplugged. Any maintenance ⁷⁵³ operation afterinstallation (cable swapping, high voltage module swapping, etc) will also ⁷⁵⁴ require the high voltage power supplies being turned off and unplugged.

c. Handling of high pressure gas bottles Detectors such as the GEM tracking detectors and the GRINCH Cherenkov detectors depend on a constant flow of gas to function. This gas is supplied with high pressure gas bottles. The handling of such gas bottles will be performed by trained personnel of staff, users, and students with the appropriate pressure systems training *i.e.* SAF130. The gas bottles will be setup with the adequate support to have them stand upwards.

Working at heights for the detector installation and maintenance d. The installation 761 and maintenance of both the Bigbite detector package and the HCal will require working 762 at heights. Four-feet tall guardrails will be installed on the Bigbite detector and HCal 763 platform. Personnel working on the detectors will require the appropriate fall protection 764 training SAF202. In addition, working on the upper part of the Bigbite and HCal detectors 765 will also require lift devices and fall protection equipment, plus the appropriate training 766 related to this equipment. 767

A crucial parameter for these measurements (both for the past GMn/nTPE and the proposed measurement alike) is the hadron calorimeter efficiency, which is expected to be slightly different for protons and neutrons, and which will contribute to the systematics budget.

Evaluation of HCal efficiency in Monte Carlo The efficiency of HCal in the Monte e.773 Carlo was evaluated in the following way. Simulations of protons and neutrons were generated 774 over the angular coverage of HCal, and over a wide momentum range from 1 to 9 GeV/c. The 775 energy from the clusters is reconstructed from the simulation as a function of the generated 776 momentum. We evaluate for each momentum the efficiency as the ratio of number of events 777 above a threshold that is 25% of the mean of the cluster energy peak over the total number 778 of events for each momentum. The result is shown on Fig. 18, zoomed in on a momentum 779 range from 2.0 to 5.5 GeV/c. Both proton and neutron detection efficiencies are above 90%780 for most of the momentum coverage. We also observe a pattern whereby the proton efficiency 781 is larger than the neutron efficiency for momenta up to 5 GeV/c, but dips under the neutron 782 efficiency for higher momenta. One of the current focuses of the ongoing nTPE analysis is 783 the reconciliation between the HCal efficiencies evaluated from Monte Carlo and data, which 785 are currently not in satisfactory agreement (see next). 786

Evaluation of HCal efficiency from data During the nTPE run, we recorded throughf. 787 out the run elastic H(e, e')p at different SBS magnet settings, in order to keep a strong handle 788 on the HCal efficiency. Indeed, the measurement of the Rosenbluth slope S^n can be affected 789 by the ratio of detection efficiencies of neutron and proton and its corresponding uncertainty. 790 The uncertainty on the ratio of efficiencies can be minimized as long as we control the stability 791 over the length of the measurement. This assertion is as valid for the past nTPE/E12-20-792 010 measurement as it will be for the proposed measurement, which is why we provision 793 hydrogen data taking throughout the run for the proposed experiment. The method to 794 obtain the HCal efficiency from elastic hydrogen is the following: Quasi-electrons electrons 795 are selected among our data sample based on their reconstructed kinematic and other data 796 quality criteria (track fit quality, etc.). Among those N_{el} elastic electron events, the HCal 797



FIG. 18. HCal efficiency as a function of nucleon momentum. The red curves with the red and blue error bands are respectively proton and neutron efficiencies evaluated using Monte Carlo, as described in paragraph 0 e. The markers show the proton efficiency analysis for $Q^2 = 3 (\text{GeV/c})^2$ and $Q^2 = 4.5 (\text{GeV/c})^2$ from the 2021-2022 GMn/nTPE LH2 data, as described in paragraph 0 f.

selection is applied, based on the difference between the predicted position x/y_{expect} of the 798 nucleon provided by the electron and the reconstructed position of the nucleon x/y_{HCal} . We 799 note this difference $\Delta x = x_{HCal} - x_{expect}$ and $\Delta y = y_{HCal} - y_{expect}$ in the dispersive and 800 non-dispersive direction respectively. Fig. 19 left illustrates the HCal selection process. The 801 HCal efficiency is then evaluated as the ratio of the number of elastic events N_{det} passing the 803 HCal selection over the total number of elastic events N_{el} . This analysis has been deployed 804 on the GMn/nTPE hydrogen data with several SBS magnetic field settings, in order to cover 805 the full HCal acceptance. The resulting efficiency map from this analysis has been presented 806 on Fig. 19, as a function of x_{expect} and y_{expect} . This map evidences a non-uniformity in 807 efficiency (due to some low efficiency HCal modules), which may be one of the sources of 808 disagreement between the HCal detection efficiency determined with the Monte Carlo and 809 the data. A similar analysis on deuterium has determined that the relative efficiency drop in 810 the "lower efficiency" areas is similar for neutrons and protons. The method that has been 812



FIG. 19. Left: Difference $\Delta x = x_{HCal} - x_{expect}$ and $\Delta y = y_{HCal} - y_{expect}$ between the expected position of the nucleon provided by the electron $x/y_{expected}$ and the reconstructed position of the nucleon in HCal x/y_{HCal} for Hydrogen data (corrected for the proton deflection). Right: HCal proton efficiency map over the full HCal x_{expect} , y_{expect} coverage, obtained analysis hydrogen data taken over different HCal magnetic fields during the GMn/nTPE experiment.



FIG. 20. HCal relative detection efficiency evaluated for protons (black) and neutrons (red) from LD_2 data. Please note the different range in $x_{HCAL,expect}$ from the left plot (SBS8, high energy) to the right (SBS9, low energy).

settled on to correct for this effect is to assign, for both proton and neutron Monte Carlo samples, a weight that correspond to the relative drop of efficiency in the data depending on the expected nucleon position x_{expect} , y_{expect} . Correcting the quasi-elastic proton and neutron Monte Carlo samples with the relative efficiency drop observed in the data corrects the neutron-proton cross section ratios by 0.2 to 0.5% depending on the kinematic.

Appendix C: Simulations, estimations of counting rates and accidentals

The estimates of accidental counting rates have been performed using G4SBS, the 820 GEANT4-based simulation package developed for the SBS experiment [54]. This pack-821 age includes a wide range of event generators, which allows us to evaluate the rates for 822 both quasi-elastic electron(positron)-proton and electron(positron)-neutron scattering and 823 other reactions such as inelastic electron(positron)-proton and electron(positron)-neutron 824 scattering and inclusive pion production. During the development of the NTPE/E12-20-010825 proposal, we had run extensive simulations to show that the trigger rates were manageable, 826 and that the backgrounds were tolerable for the experiment, which was originally planned 827 to run at 30 μ A, which is thirty times the luminosity of the positron kinematics for this 828 experiment. 829

830

1. Trigger rates

We have evaluated the trigger rates estimated for our all proposed kinematics. The main processes expected to contribute to the trigger rates for the BigBite spectrometer are:

- the inelastic electron nucleon scattering process;
- photons from inclusive π^0 production;
- and to a lesser extent, charged pions.

Fig. 21 presents the distributions of rate of energy deposit for the different processes involved in the BigBite trigger rates for two kinematics: $Q^2 = 4.5 (\text{GeV/c})^2$, $\epsilon = 0.838$, which is the smallest angle for Bigbite, and $Q^2 = 5.5 (\text{GeV/c})^2$, $\epsilon = 0.420$ which is the largest angle for BigBite but the lowest threshold. For the high (low) energy point, the rates are anticipated to be around 250 (500) Hz at a threshold of 3 (1.3) GeV.

The thresholds to apply to each arm are determined as a function of the elastic peak. For the electron arm, the threshold has been set at $\mu_E - 3\sigma_E$, μ_E and σ_E being respectively the position and width of the fitted elastic peak.



FIG. 21. Rates of the different process contributing to the BigBite electron arm trigger for positrons at $Q^2 = 4.5 \text{ (GeV/c)}^2$, $\epsilon = 0.838$, which is the smallest angle for Bigbite (left), and $Q^2 = 5.5 \text{ (GeV/c)}^2$, $\epsilon = 0.420$ which is the largest angle for BigBite but the lowest threshold (right). Quasi-elastic is in green, inelastic in magenta, π^0 in red, π^- in blue, and π^+ in dark blue.

Kin	threshold	Trigger rates
point	(GeV)	(Hz)
1	1.1	355
2	1.8	791
3	1.3	156
4	2.8	305
5	0.9	199
6	2.4	125

TABLE VII. Thresholds and trigger rates for each kinematics with $1\mu A$ on 15cm liquid deuterium target.

Those numbers can be compared to the rates observed for nTPE(E12-20-010). For the high energy setting, the BigBite spectrometer was registering 2.8 kHz of triggers at at a threshold estimated around 2.7 GeV for 5.5 μ A of triggers. This is to be compared to the 300 Hz at a threshold of 2.8 GeV for 1 μ A. Scaling for the luminosity and accounting for a slightly lower threshold, our simulation is off by about 40%. Even accounting for this, our ⁸⁴⁹ trigger rates remain manageable.