



1.0 Define Inputs

$b := 62.5\text{mm}$	Side of module
$a1 := 2 \cdot (28.14\text{mm})$	Distance between tension rods
$a2 := 2 \cdot (56.25\text{mm})$	
$n_L := 194$	Number of layers of lead
$n_s := 194$	Number of layers of scintillator
$t_L := 0.5\text{mm}$	Thickness of lead
$t_s := 1.5\text{mm}$	Thickness of scintillator
$t_{\text{gap}} := .24\text{mm}$	Thickness of gap

$$\rho_L := .011340 \cdot \frac{\text{kg}}{\text{cm}^3}$$

Density of lead

$$E_L := 2560 \text{ksi}$$

Modulus of lead

$$\rho_S := .001220 \cdot \frac{\text{kg}}{\text{cm}^3}$$

Density of scintillator

$$E_S := 460 \text{ksi}$$

Modulus of Scintillator

$$\mu := 0.1$$

Coefficient of Friction between layers

$$D_{\text{rod}} := 2.5 \text{mm}$$

Diameter of rods

$$F_y := 18000 \text{psi}$$

Yield Strength of brass rods

$$E_{\text{brass}} := 15000 \text{ksi}$$

Modulus of brass

$$E_{\text{steel}} := 30000 \text{ksi}$$

Modulus of steel

2.0 Calculate Properties of Calorimeter

$$\text{Length} := n_L \cdot t_L + n_S \cdot t_S = 388.00 \cdot \text{mm}$$

$$\text{Length} = 15.28 \cdot \text{in}$$

$$\text{Area} := 100 \text{cm}^2$$

$$\text{Weight} := n_L \cdot g \cdot \rho_L \cdot \text{Area} \cdot t_L + n_S \cdot g \cdot \rho_S \cdot \text{Area} \cdot t_S$$

$$\text{Weight} = 32.1 \cdot \text{lbf}$$

$$\text{Weight} = 142.7 \text{N}$$

$$q := \frac{\text{Weight}}{\text{Length}}$$

$$q = 2.10 \cdot \frac{\text{lbf}}{\text{in}}$$

$$A_{\text{rod}} := \frac{\pi \cdot D_{\text{rod}}^2}{4}$$

$$A_{\text{rod}} = 0.01 \cdot \text{in}^2$$

3.0 Pre-Loading

Assume a pre-load is applied to the stack and then four threaded rods are snugged to the stack and then the pre-load is released.

$$F_{\text{preload}} := 500 \text{kg} \cdot g = 1102.31 \cdot \text{lbf}$$

$$k_{\text{BrassRod}} := \frac{6A_{\text{rod}} \cdot E_{\text{brass}}}{\text{Length}} = 44827.75 \cdot \frac{\text{lbf}}{\text{in}}$$

$$k_{\text{SteelRod}} := \frac{6A_{\text{rod}} \cdot E_{\text{steel}}}{\text{Length}} = 89655.51 \cdot \frac{\text{lbf}}{\text{in}}$$

$$k_{\text{stack}} := \left(\frac{n_s \cdot t_s}{\text{Area} \cdot E_s} + \frac{n_L \cdot t_L}{\text{Area} \cdot E_L} \right)^{-1} = 587175.52 \cdot \frac{\text{lbf}}{\text{in}}$$

$$\Delta_{\text{stack1}} := \frac{F_{\text{preload}}}{k_{\text{stack}}} = 0.001877 \cdot \text{in}$$

$$\Delta_{\text{rod1}} := \frac{\Delta_{\text{stack1}} \cdot k_{\text{stack}}}{k_{\text{BrassRod}} + k_{\text{stack}}} = 0.00174 \cdot \text{in}$$

$$F_{\text{rod1}} := \Delta_{\text{rod1}} \cdot k_{\text{BrassRod}} = 78.19 \cdot \text{lbf}$$

Preload in rods due to initial applied load on stack

$$N_{\text{req}} := \frac{\text{Weight}}{\mu} = 320.77 \cdot \text{lbf}$$

Required normal force to carry the load in friction

Use a preload on the rods that is twice the required value for safety factor

$$N_{\text{preload}} := 2 \cdot N_{\text{req}} = 641.55 \cdot \text{lbf}$$

$$\Delta_{\text{rodN}} := \frac{N_{\text{preload}}}{k_{\text{BrassRod}}} = 0.014 \cdot \text{in}$$

$$\sigma_{\text{rod}} := \frac{N_{\text{preload}}}{6 \cdot A_{\text{rod}}} = 14053.15 \cdot \text{psi}$$

4.0 Calculate the increase in rod loading due to being cantilevered.

$$F_{\text{cantilever}} := \frac{q \cdot \text{Length}^2}{a2 + 2a1 \cdot \left(\frac{a1}{a2} \right)} = 73.73 \cdot \text{lbf}$$

$$F_{\text{rod}} := \frac{N_{\text{preload}}}{6} + F_{\text{cantilever}} = 180.65 \cdot \text{lbf}$$

$$\Delta_{\text{rodN}} := \frac{F_{\text{rod}}}{k_{\text{BrassRod}}} = 0.004 \cdot \text{in}$$

$$\sigma_{\text{rod}} := \frac{F_{\text{rod}}}{6 \cdot A_{\text{rod}}} = 3957.21 \cdot \text{psi}$$

$$\sigma_{\text{scintillator}} := \frac{F_{\text{rod}}}{\text{Area}} = 11.65 \cdot \text{psi}$$

Tensile stress in rods

$$\tau_{\text{rod}} := \frac{F_{\text{rod}}}{\pi \cdot D_{\text{rod}} \cdot \frac{3}{32} \text{in}} = 6231.82 \cdot \text{psi}$$

Shear stress in threads

Brass tensile yield strength of 18000psi and the shear yield strength of the threads is 9000psi so both stresses are ok